



Science yield modeling with the Exoplanet Open-Source Imaging Mission Simulator (EXOSIMS)

Christian Delacroix, KISS Workshop, August 2016

Collaborators:

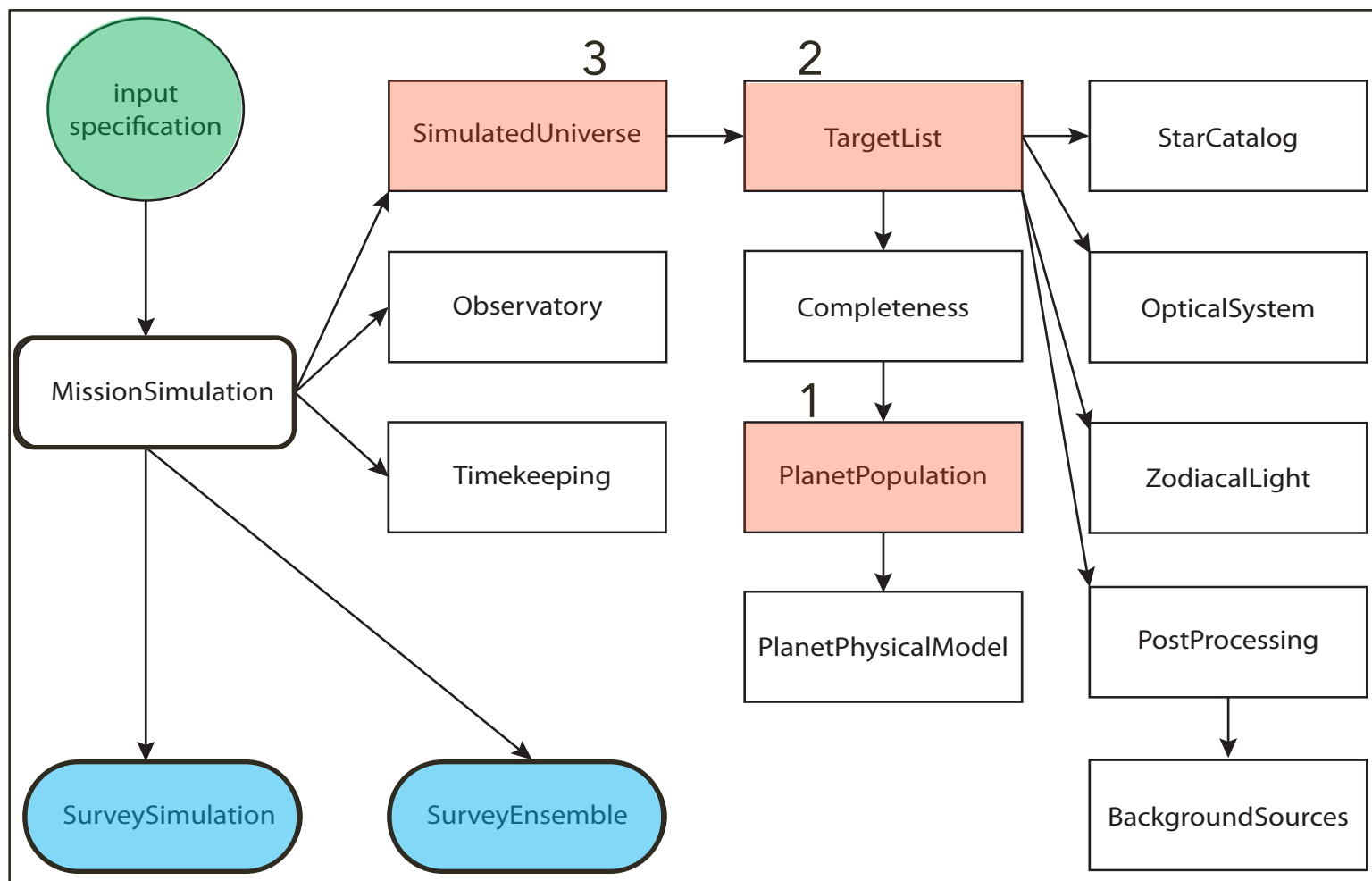
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NASA Grant Nos. NNX14AD99G (GSFC) and NNX15AJ67G (WPS).

EXoplanet Open-Source Imaging Mission Simulator

- EXOSIMS - developed as part of WFIRST Preparatory Science
- Performs ensembles of simulations to determine science yield distributions
- Modular architecture, allows multiple mission designs
- <https://github.com/dsavransky/EXOSIMS>

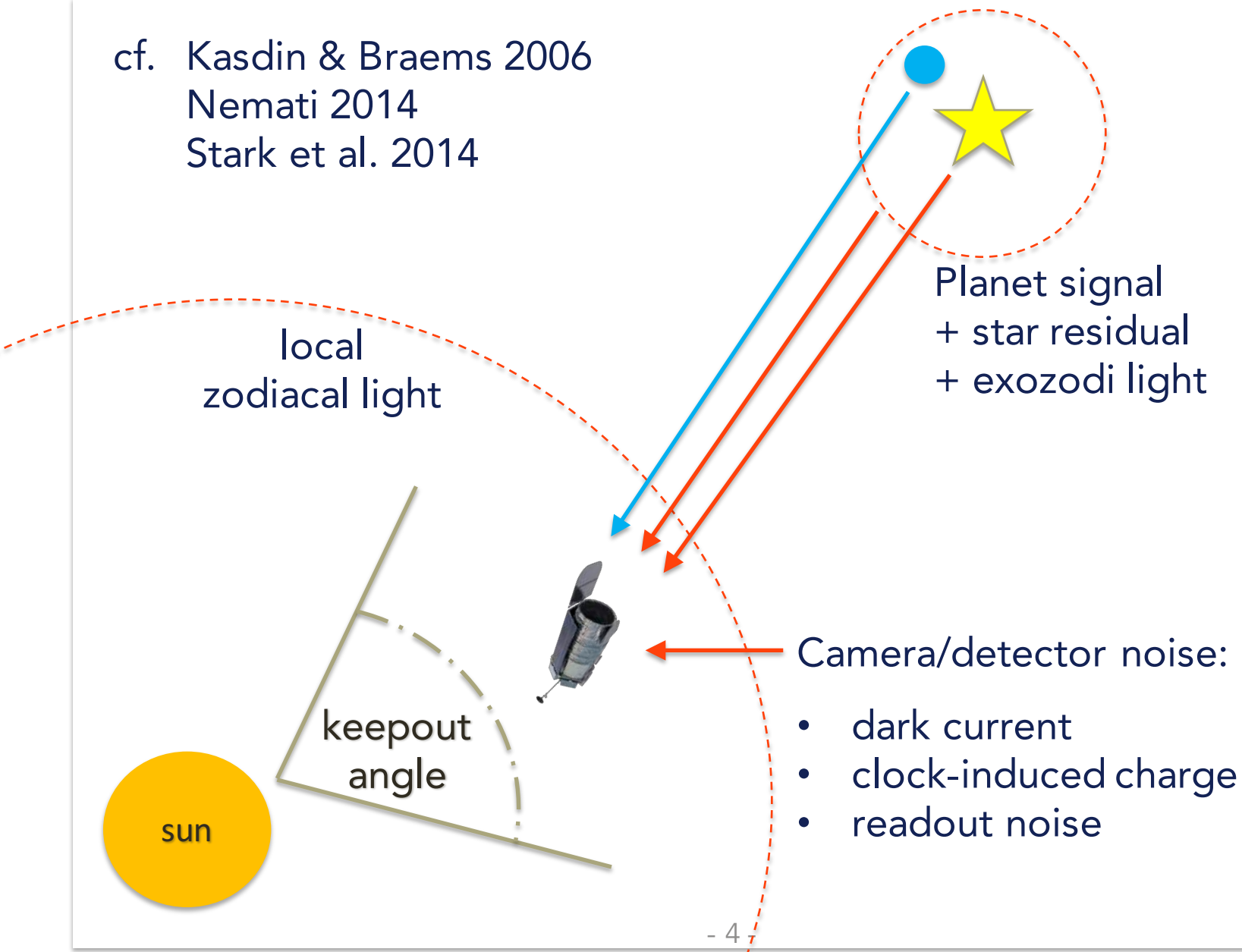


The Scheduler – which target to observe ?

- Find spacecraft orbital START positions and filter out unavailable targets (including settling time, occulter slew time)
- Calculate **integration times** for the preselected targets and filter out $t > \text{threshold}$ (arbitrary)
- Find spacecraft orbital END positions and filter out unavailable targets
- Filter out all previously visited targets, unless in revisit list (e.g. detected planets, but not yet characterized)
- From remaining, choose the target with **highest completeness**

Planet integration time – noise budget

cf. Kasdin & Braems 2006
Nemati 2014
Stark et al. 2014



How do we determine integration time?

- spectral flux density electron count rate

$$C_{\mathcal{F}_0}(\lambda) = \epsilon A \Delta\lambda \mathbf{T}(\lambda) \mathcal{F}_0(\lambda) \quad \text{with } \mathcal{F}_0(\lambda) = 10^{\left(4.01 - \frac{\lambda - 550}{770}\right)}$$

- planet signal

Total throughput

$$C_p(\lambda) = C_{\mathcal{F}_0}(\lambda) 10^{-0.4 (\text{vmag} + \Delta\text{mag})}$$

- star residual

$$C_{sr}(\lambda) = C_{\mathcal{F}_0}(\lambda) 10^{-0.4 \text{vmag}} \mathbf{Q}(\lambda)$$

- background noise

Instrument contrast

$$C_b(\lambda) = C_{sr}(\lambda) + C_{zl}(\lambda) + C_{dc} + C_{cc} + C_{rn}$$

zodiacal
light

dark
current

clock-induced
charge

read
noise

- SNR

$$SNR = \frac{C_p t}{\sqrt{C_p t + C_b t + (\mathbf{f}_{pp} C_{sr} t)^2}}$$

with \mathbf{f}_{pp} = post-processing factor

speckle residuals
(systematic error)

Implemented detection methods

- From Nemati SPIE 2014

$$t(\lambda) = \frac{(c_p + c_b) \text{SNR}^2}{c_p^2 - (\text{SNR} f_{PP} c_{sr})^2}$$

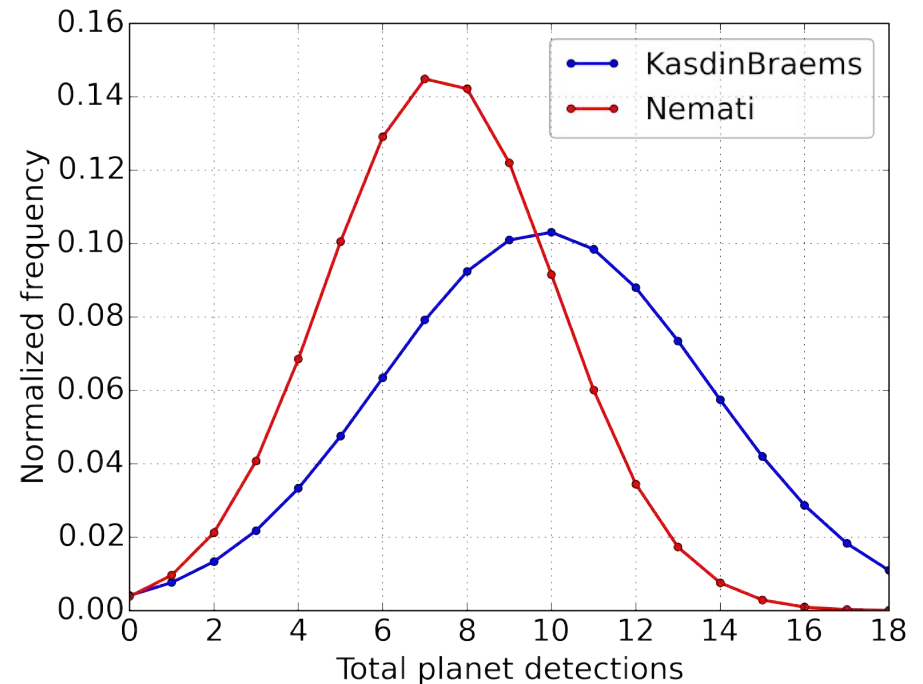
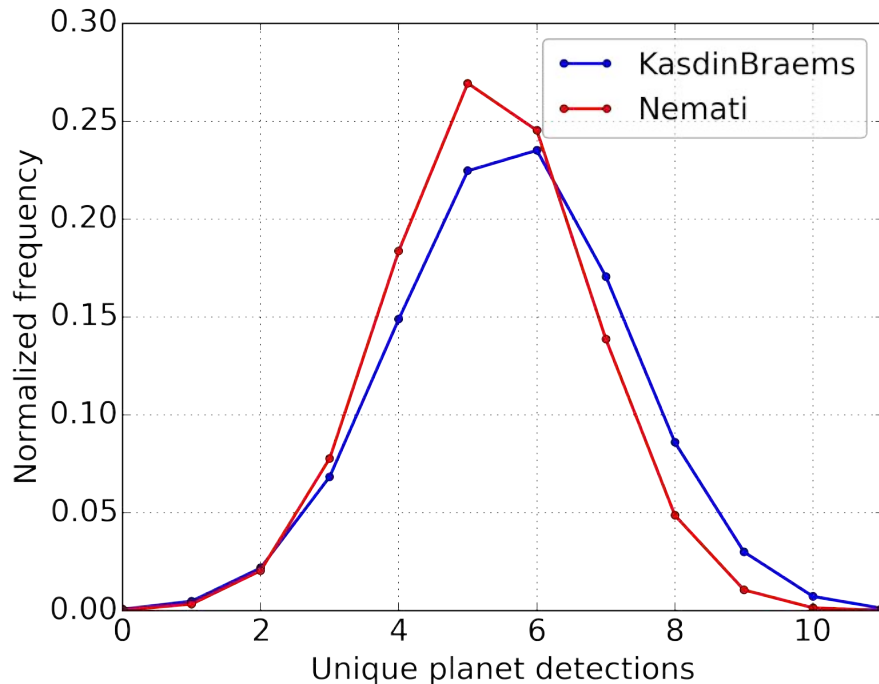
- From Kasdin & Braems 2006

$$t(\lambda) = \frac{c_b}{c_p^2 \overline{\Delta\alpha}} \left(z_{\text{FA}} - z_{\text{MD}} \sqrt{1 + \frac{c_p \sum \overline{\text{PSF}}_{ij}^3}{c_b \sum \overline{\text{PSF}}_{ij}^2}} \right)^2$$

where $\overline{\Delta\alpha}$ is the dimensionless pixel size, and $\overline{\text{PSF}}$ is the normalized PSF

Comparison using EXOSIMS

- method 1, Nemati 2014: setting a **SNR = 5**
- method 2, Kasdin 2006: **$P_{FA} = 3E-5$** and **$P_{MD} = 1E-3$**



Null hypothesis H_0 : there is no planet.

Alternative hypothesis H_1 : there is a planet.

- Fail to reject H_0 while true (True Negative):

$$P(\text{no detection}) = P(Z < z_{\text{FA}}) = F_Z(z_{\text{FA}}) = 1 - p_{\text{FA}}$$

- Reject H_0 while true (type I error, False Positive):

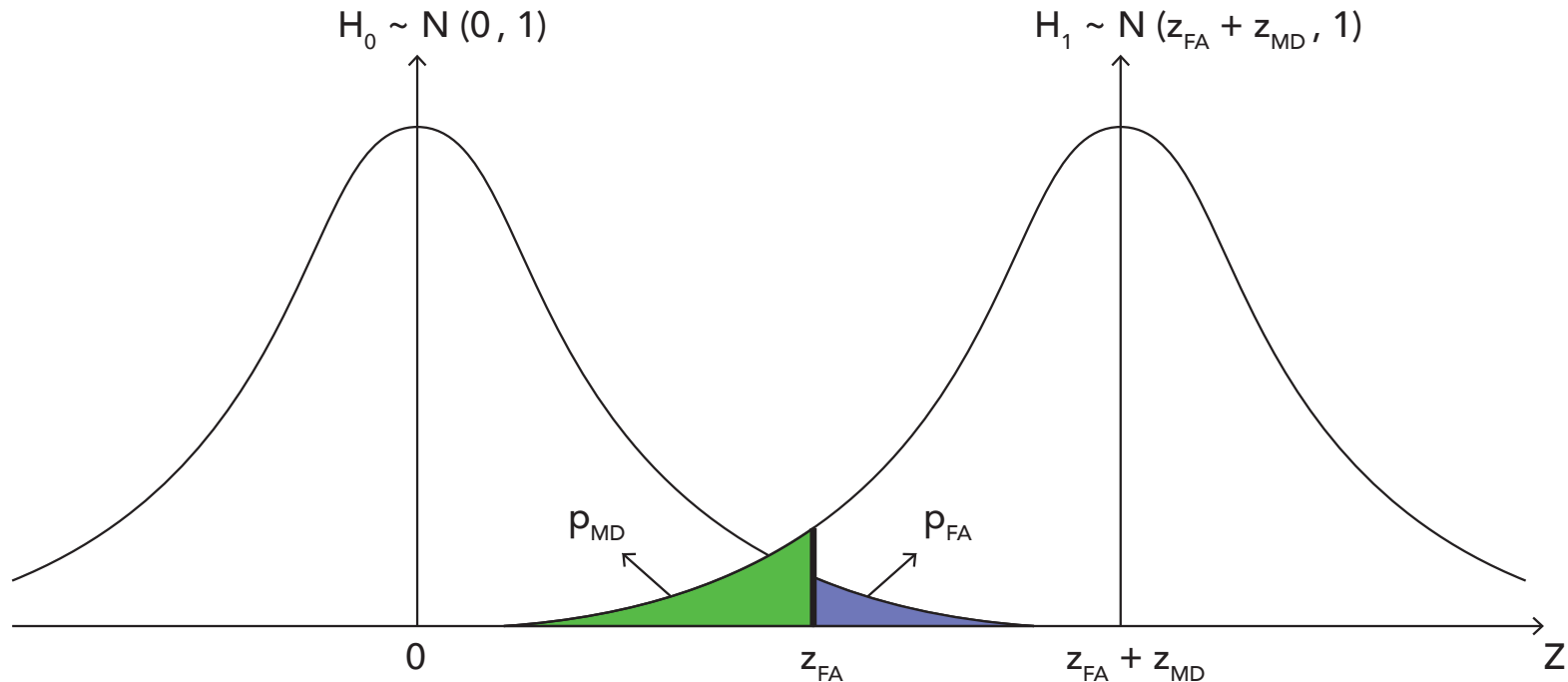
$$P(\text{false alarm}) = p_{\text{FA}}$$

- Reject H_0 while false (True Positive):

$$P(\text{detection}) = P(Z < z_{\text{MD}}) = F_Z(z_{\text{MD}}) = 1 - p_{\text{MD}}$$

- Fail to reject H_0 while false (type II error, False Negative):

$$P(\text{missed detection}) = p_{\text{MD}}$$

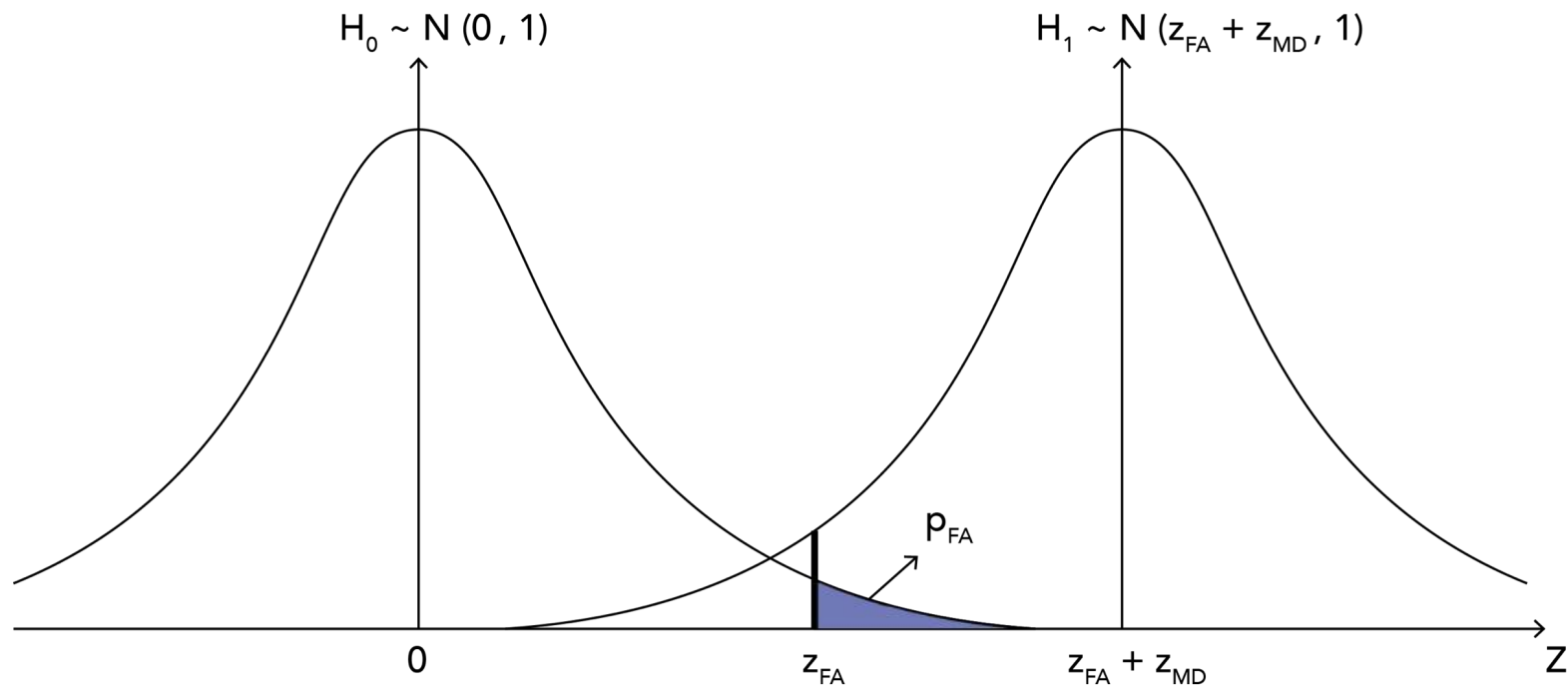


Probabilistic case

Case 1, no calculated SNR.

For the whole system:

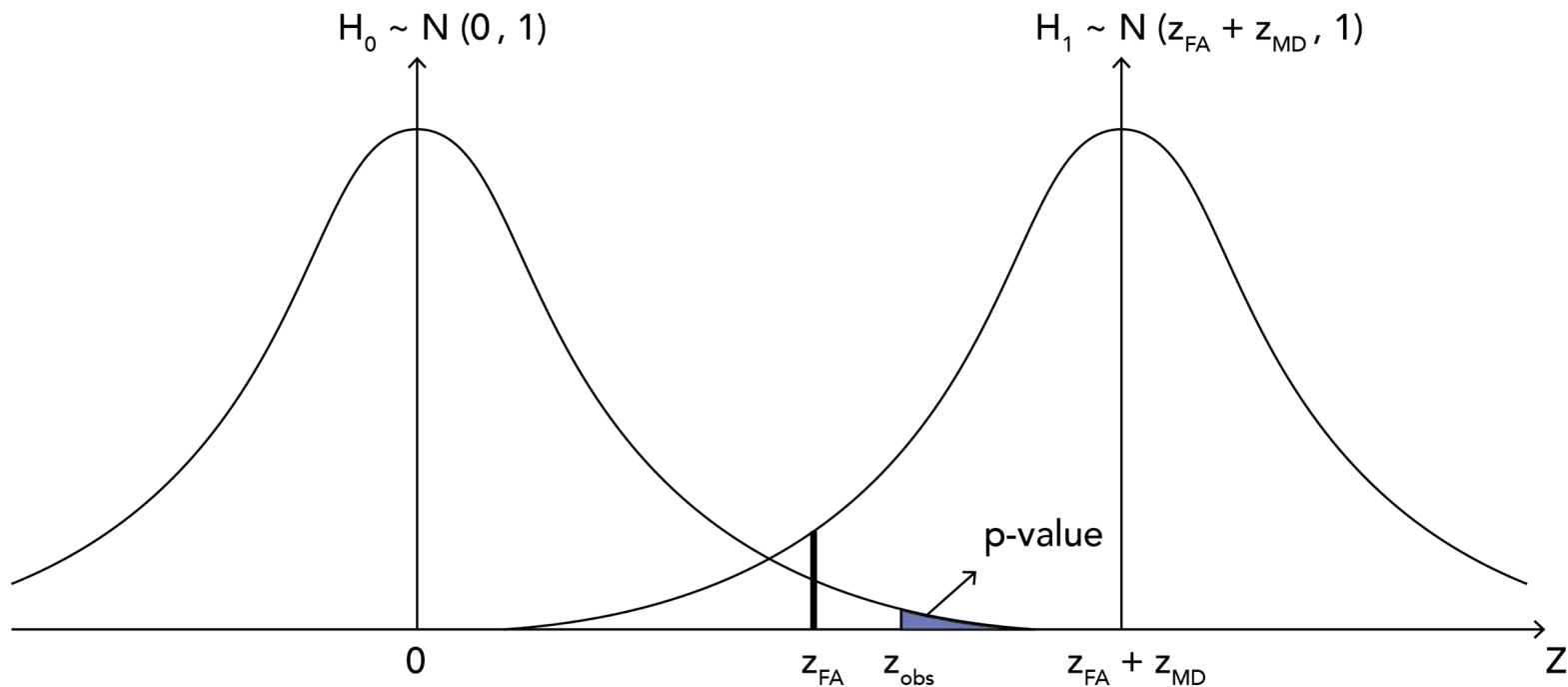
- True Negative: $P(\text{no detection}) = F_z(z_{\text{FA}}) = 1 - p_{\text{FA}}$
- False Positive: $P(\text{false alarm}) = p_{\text{FA}}$



Probabilistic case (cont'd)

Case 2.1, calculated $\text{SNR} = z_{\text{obs}} > z_{\text{FA}} \rightarrow \text{reject } H_0$.

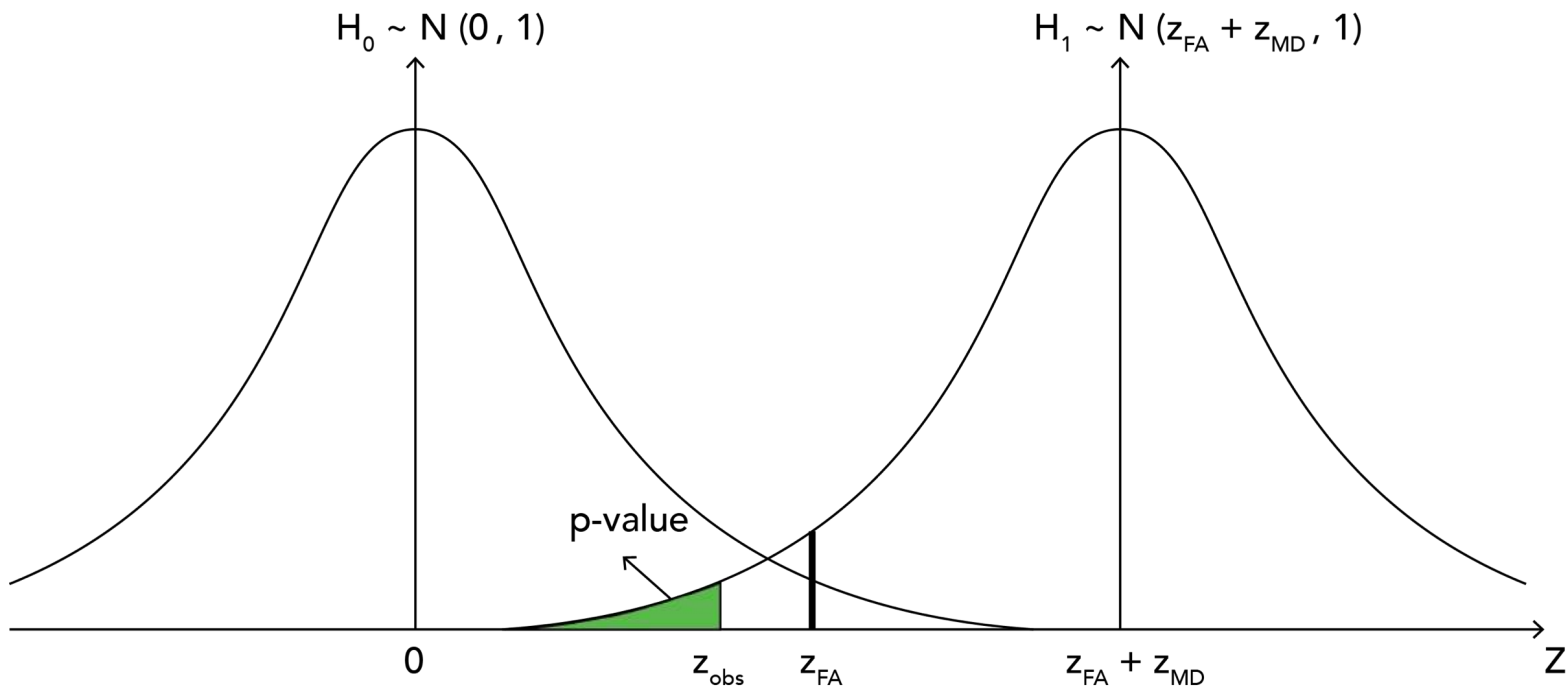
- True Positive: $P(\text{detection}) = P(Z < z_{\text{obs}}) = F_Z(z_{\text{obs}})$
- False Positive: $P(\text{false alarm}) = 1 - F_Z(z_{\text{obs}}) = \text{p-value}$



Probabilistic case (cont'd)

Case 2.2, calculated SNR = $z_{\text{obs}} < z_{\text{FA}}$ --> fail to reject H_0 .

- True Negative: $P(\text{no detection}) = P(Z < z_{\text{FA}} + z_{\text{MD}} - z_{\text{obs}}) = F_Z(z_{\text{FA}} + z_{\text{MD}} - z_{\text{obs}})$
- False Negative: $P(\text{missed detection}) = 1 - F_Z(z_{\text{FA}} + z_{\text{MD}} - z_{\text{obs}}) = \text{p-value}$



Backup slides

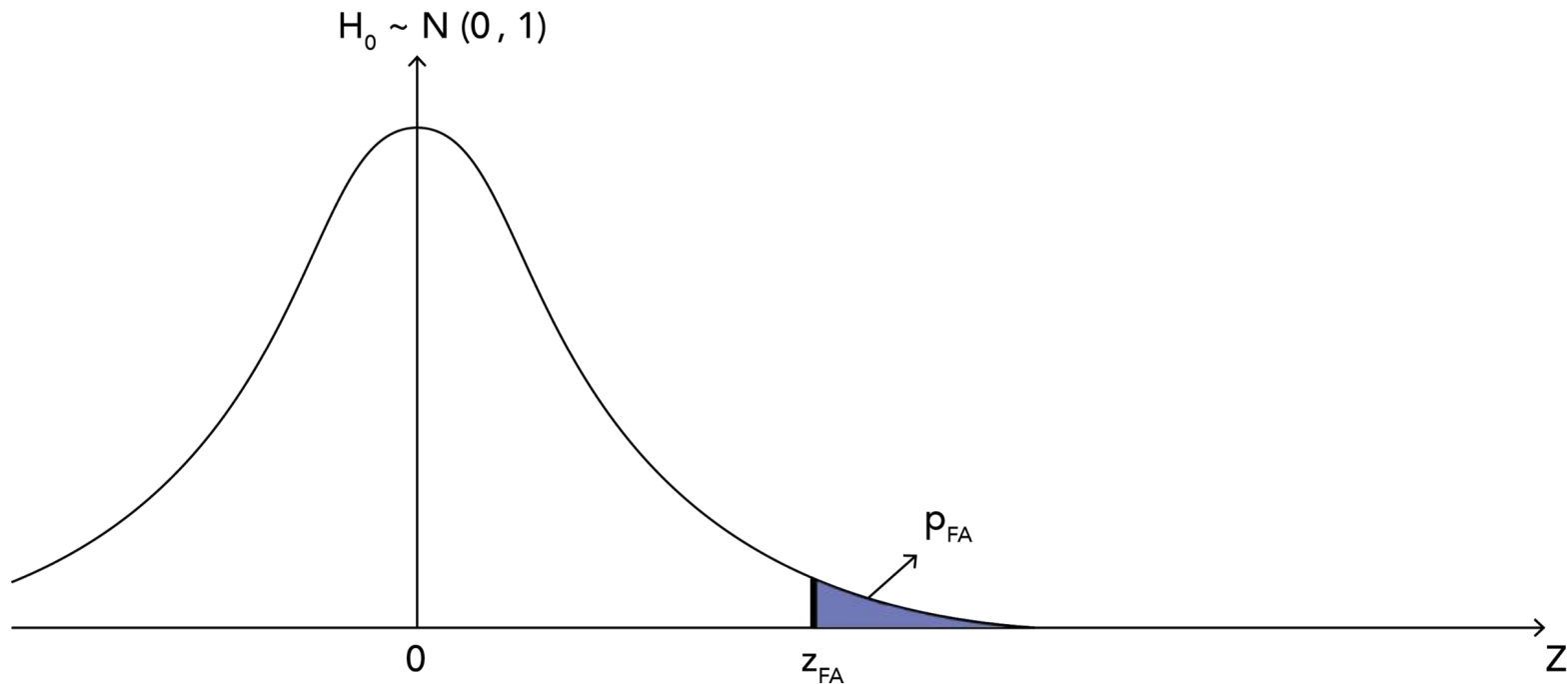
Deterministic case

We 'know' if there is a planet or not

Case 1, there is no planet, H_0 is true.

For the whole system:

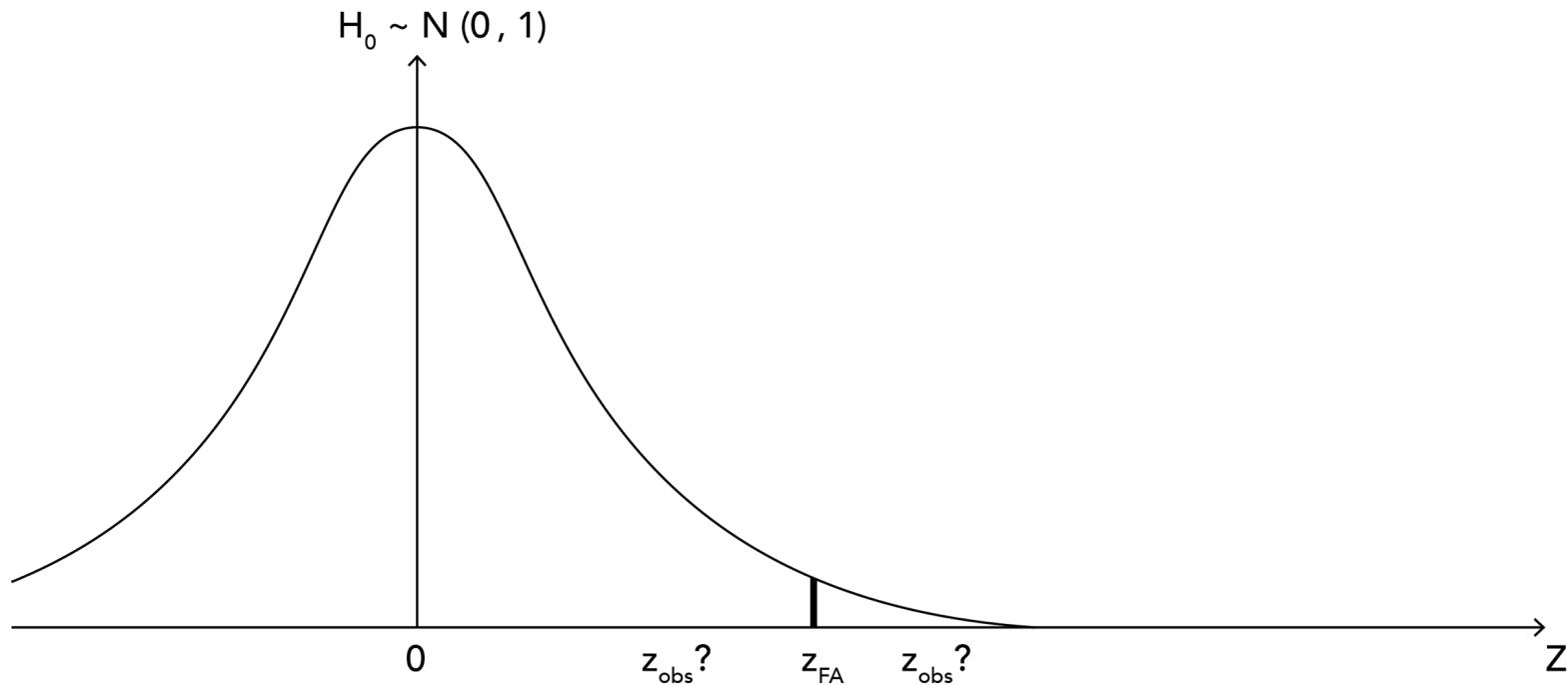
- True Negative: $P(\text{no detection}) = F_Z(z_{\text{FA}}) = 1 - p_{\text{FA}}$
- False Positive: $P(\text{false alarm}) = p_{\text{FA}}$



Deterministic case (cont'd)

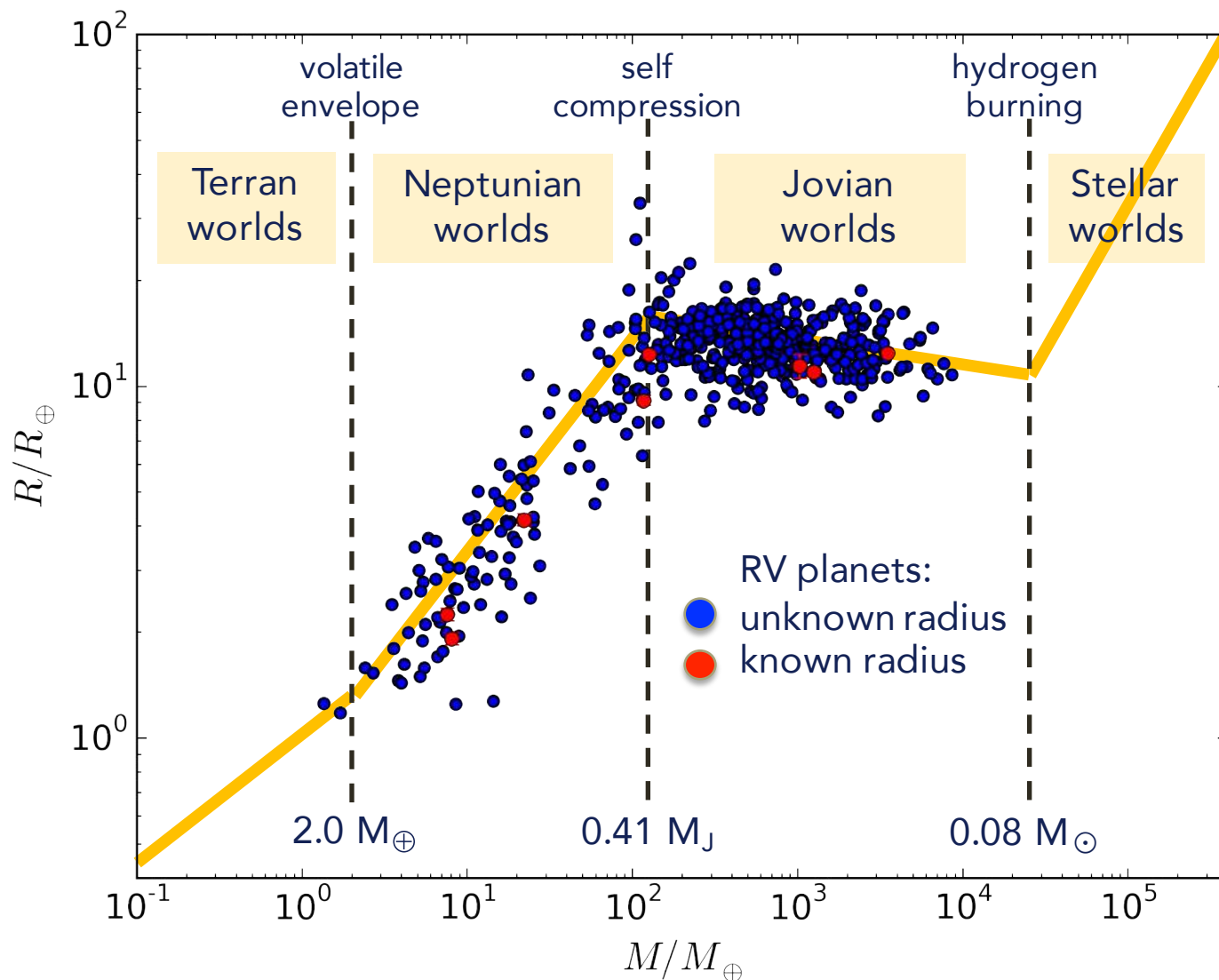
Case 2, there is a planet, H_0 is false.

- if $\text{SNR} = z_{\text{obs}} > z_{\text{FA}}$ --> reject H_0 : True Positive (detection)
- if $\text{SNR} = z_{\text{obs}} < z_{\text{FA}}$ --> fail to reject H_0 : False Negative (missed detection)



Populate Universe: e.g. known RV planets

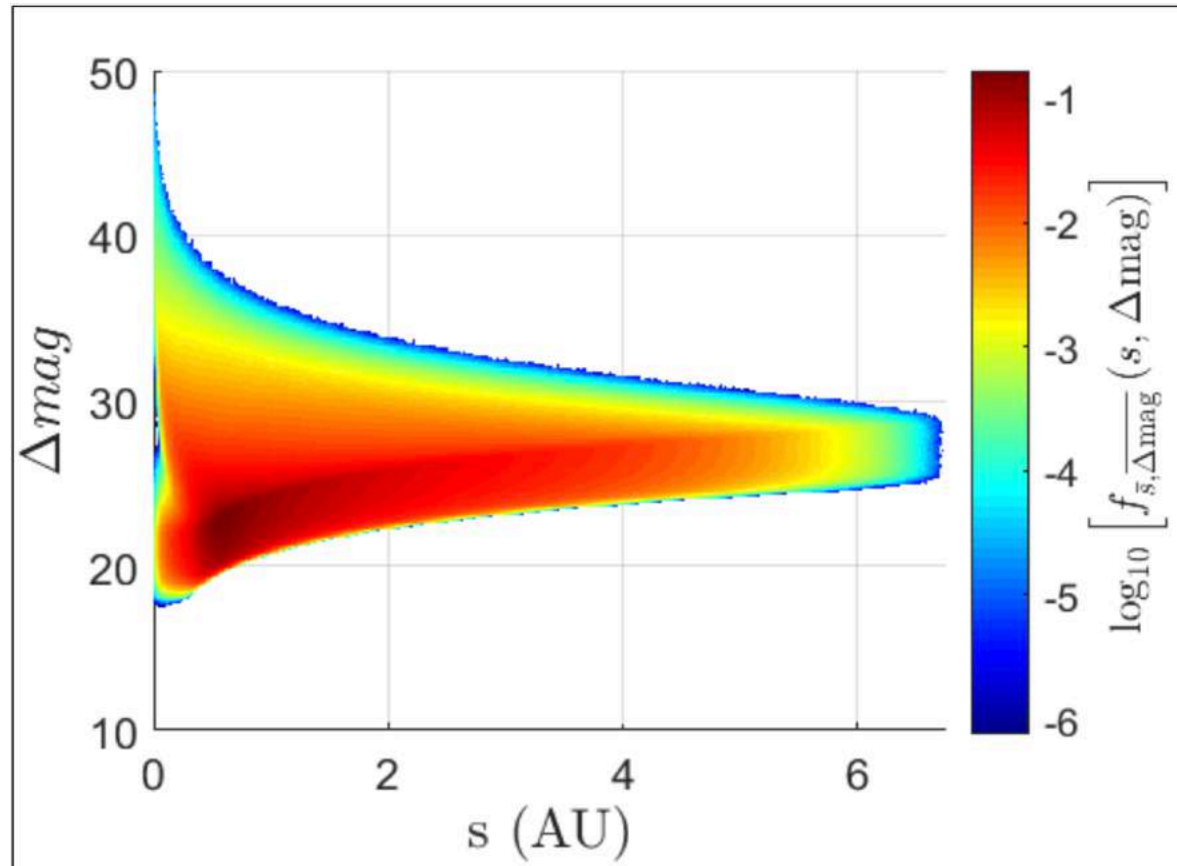
M-R relation from FORECASTER (Chen and Kipping 2016)
available at github.com/chenjj2/forecaster



Example of joint probability density function

Garrett et al. 2016

- PDF of planet orbital and physical properties
- Completeness = CDF (cf. Brown 2005)
- Probability to detect a planet
- Updates completeness values for systems previously observed

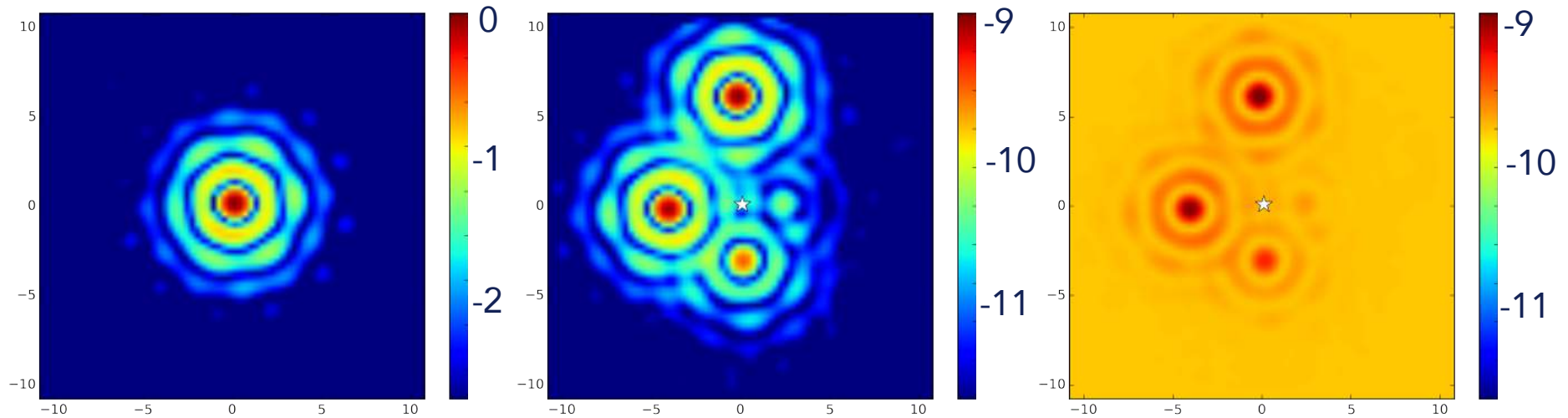


Planet integration time – noise budget (cont'd)

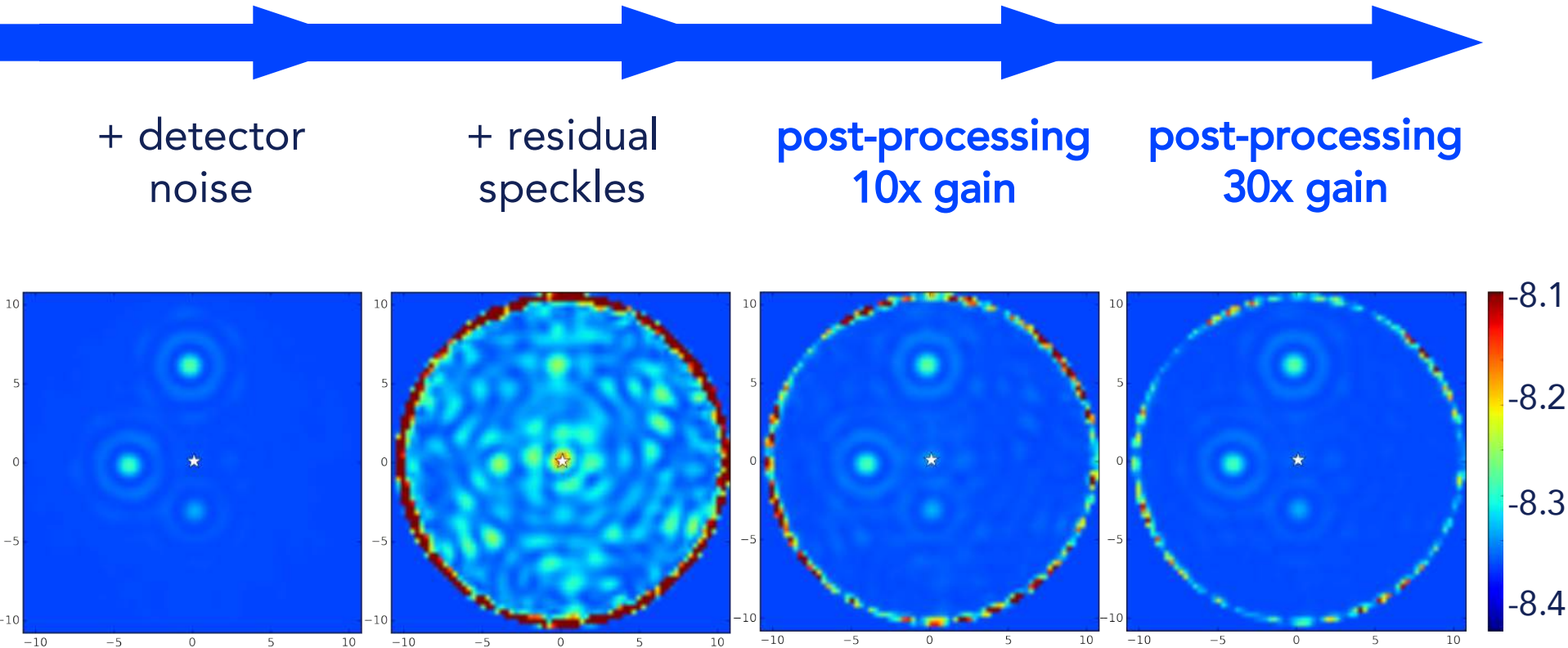
normalized
star PSF

planets
(star cancelled)

+ local zodi
+ exozodi



Planet integration time – noise budget (cont'd)



e.g. WFIRST contrast/throughput curve

