

# **Fundamentals of frequency combs: What they are and how they work**

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Boulder, CO*

KISS Worshop: “Optical Frequency Combs for Space Applications”

# **Outline**

## **1. Optical frequency combs in timekeeping**

- How we got to where we are....

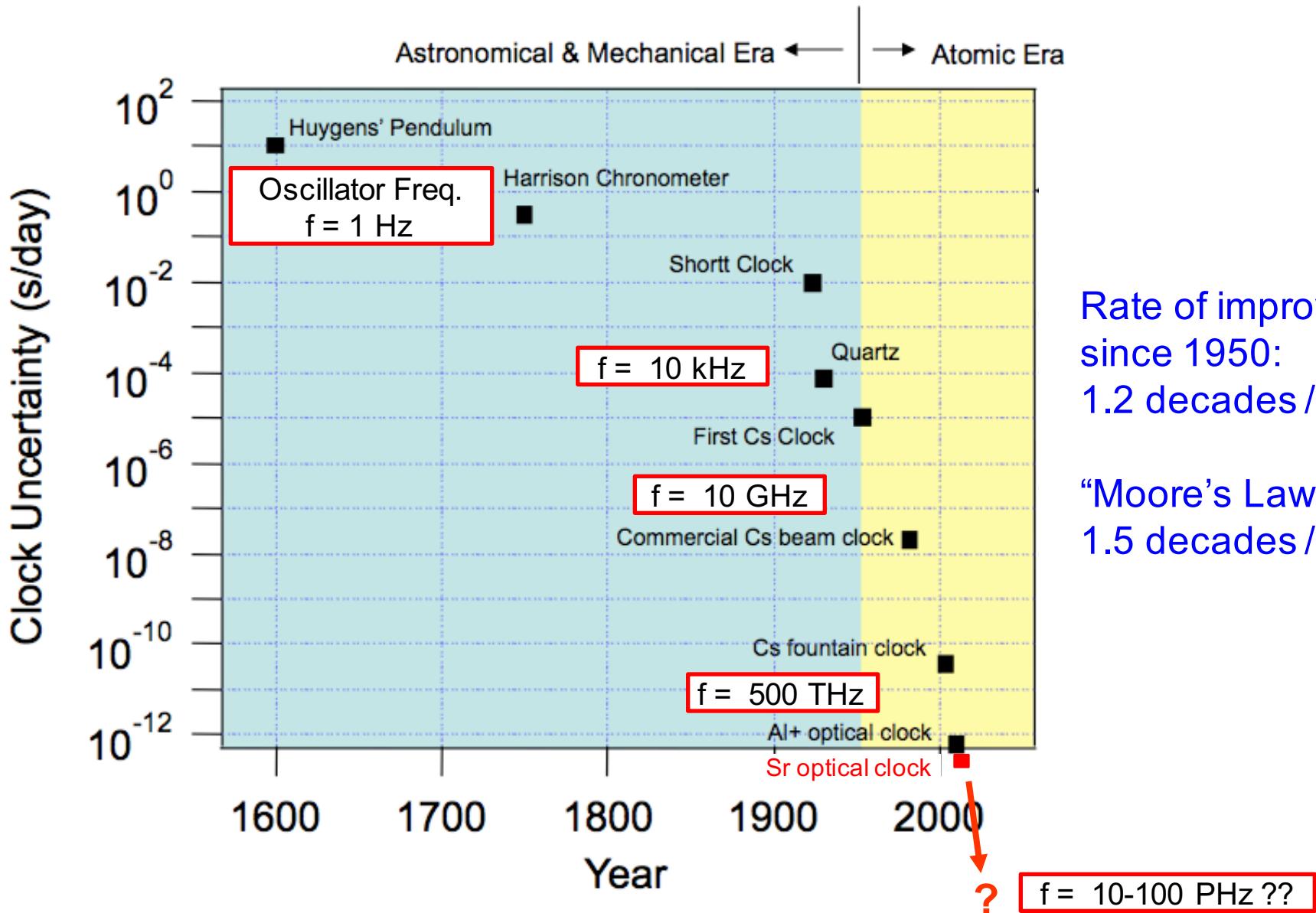
## **2. The multiple faces of an optical frequency comb**

## **3. Classes of frequency combs and their basic operation principles**

- Mode-locked lasers
- Microcombs
- Electro-optic frequency combs

## **4. Challenges and opportunities for frequency combs**

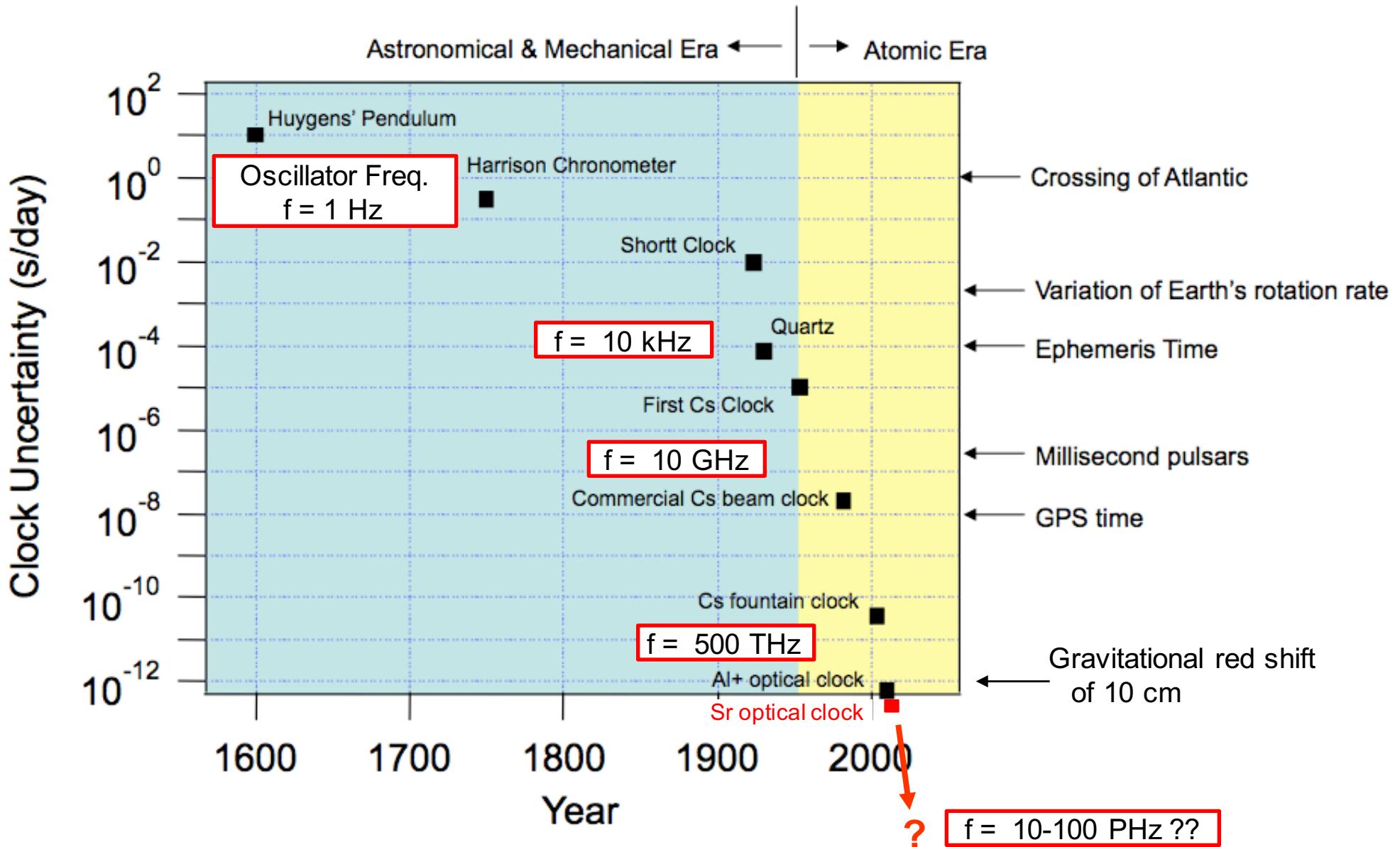
# Timekeeping: The long view



Rate of improvement  
since 1950:  
1.2 decades / 10 years

“Moore’s Law”:  
1.5 decades / 10 years

# Timekeeping: The long view



# Use higher frequencies !

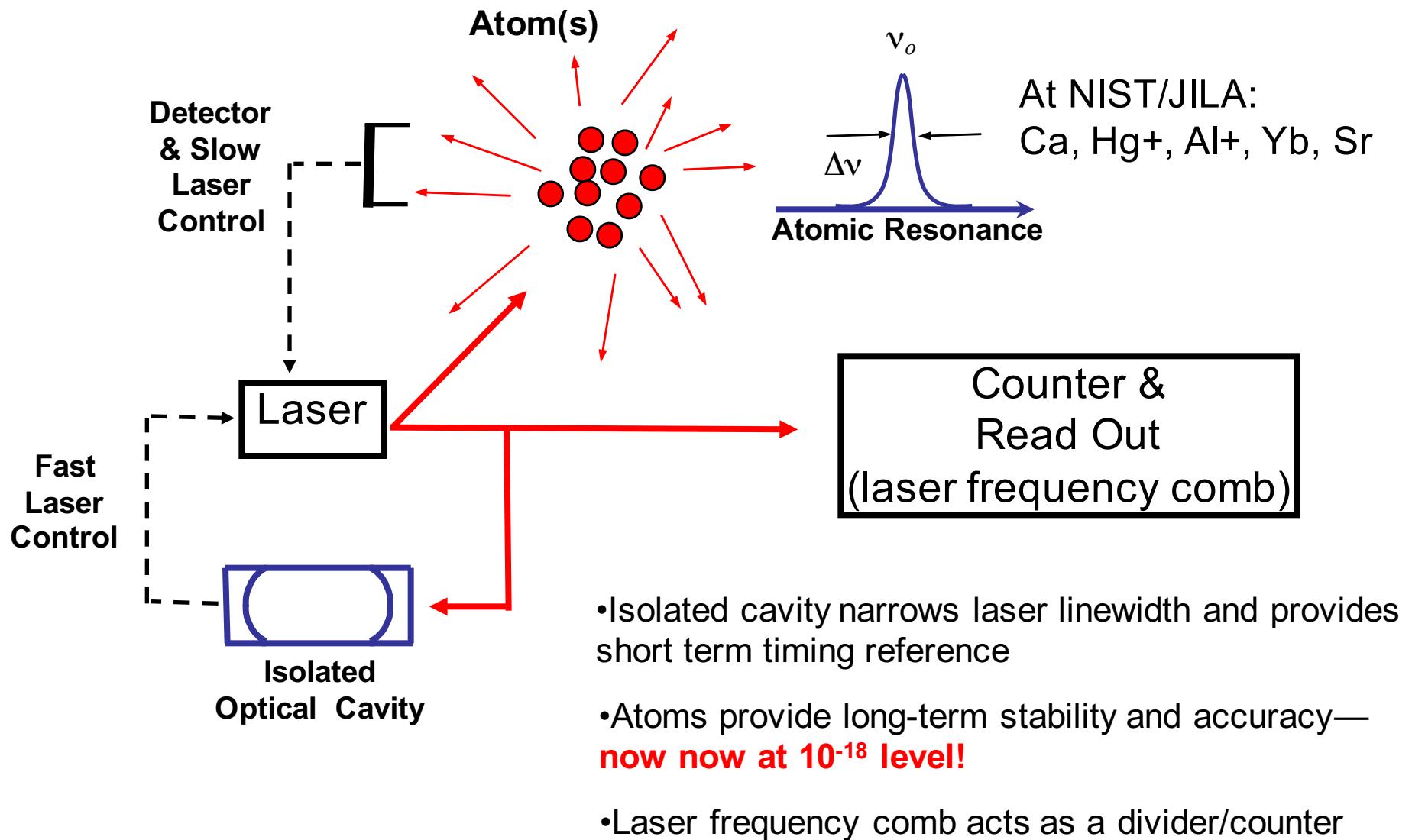
Dividing the second into smaller pieces yields superior frequency standards and metrology tools:

$$\frac{v_{\text{optical}}}{v_{\text{microwave}}} \approx \frac{10^{15}}{10^{10}} \approx 10^5$$

In principle (!), optical standards could surpass their microwave counterparts by up to five orders of magnitude

... but how can one count, control and measure optical frequencies?

# Optical Atomic Clocks



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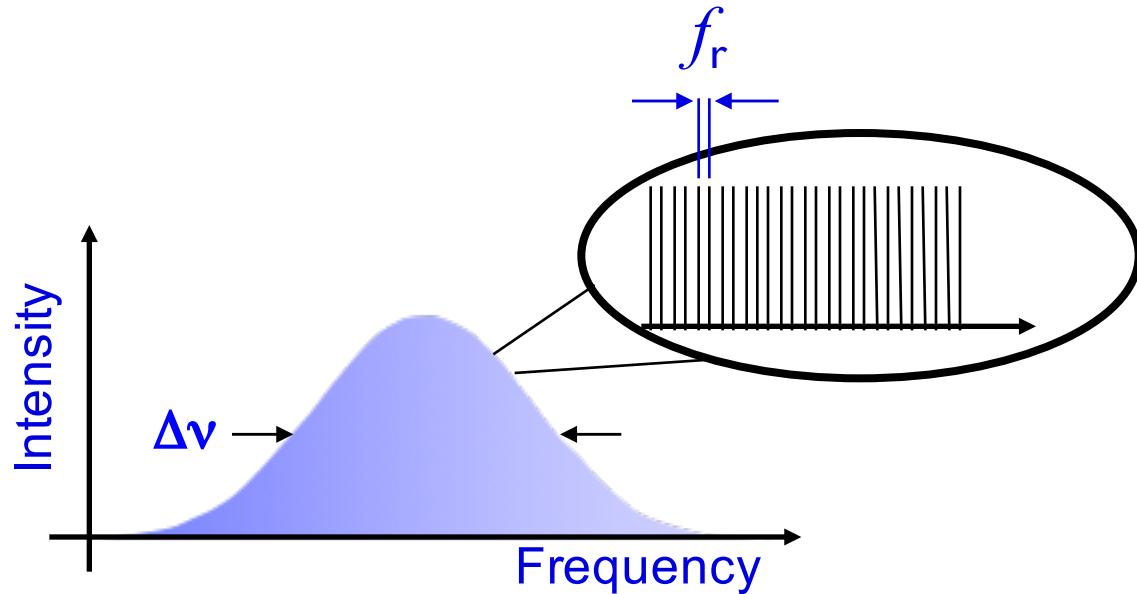
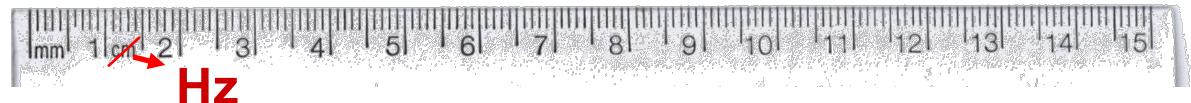
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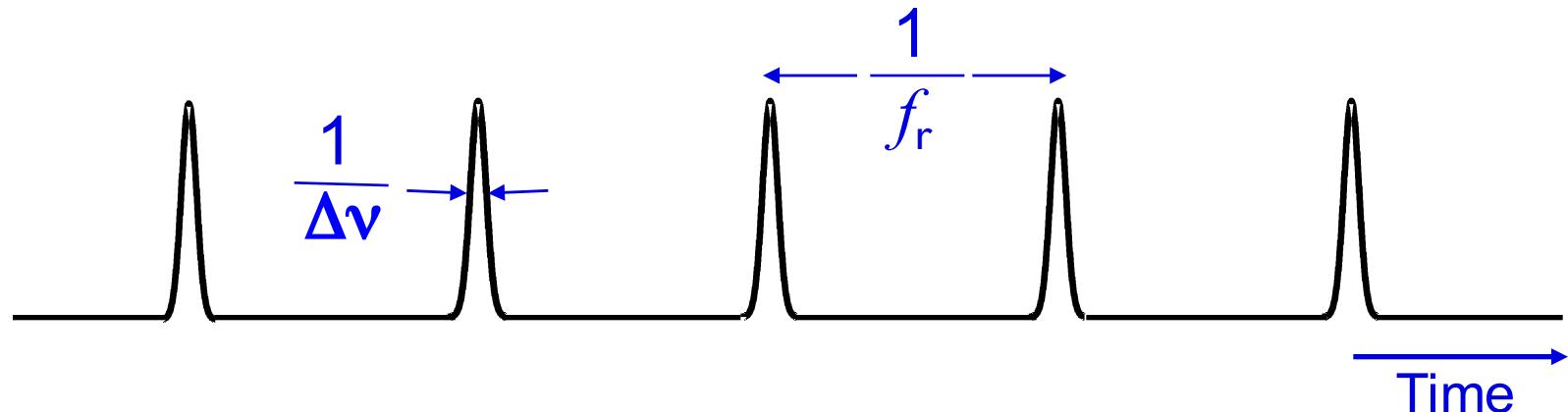
## 4. Challenges and opportunities for frequency combs

# Multiple faces of a frequency comb

1. A ruler for light frequencies

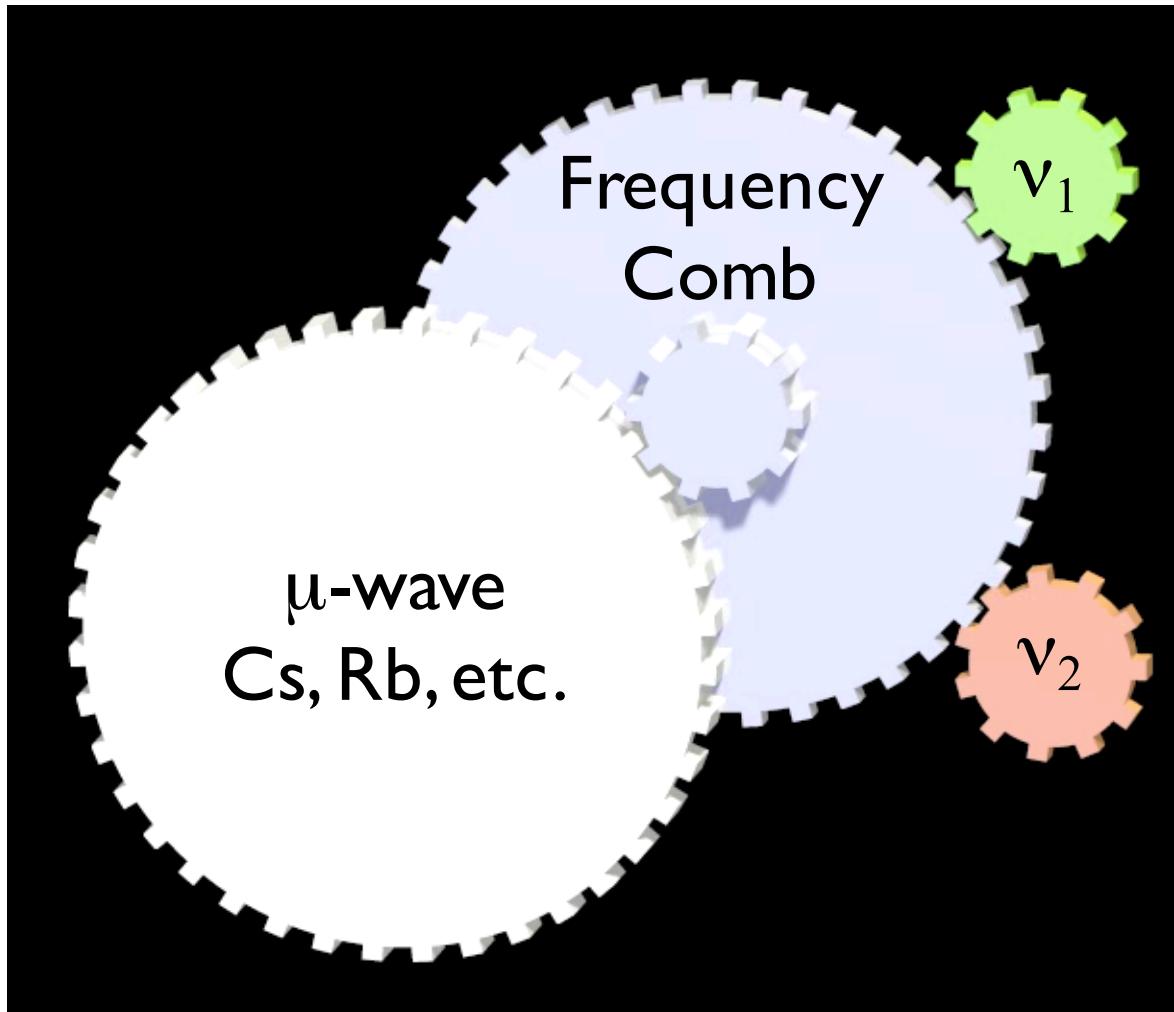


2. A perfectly-spaced train of optical pulses



# Multiple faces of a frequency comb

## 3. An optical clockwork



- Comb uncertainty at the 20<sup>th</sup> decimal place
- Measurement of optical ratios (e.g.  $\nu_1 : \nu_2$ )
- Direct connection from optical to microwave domains

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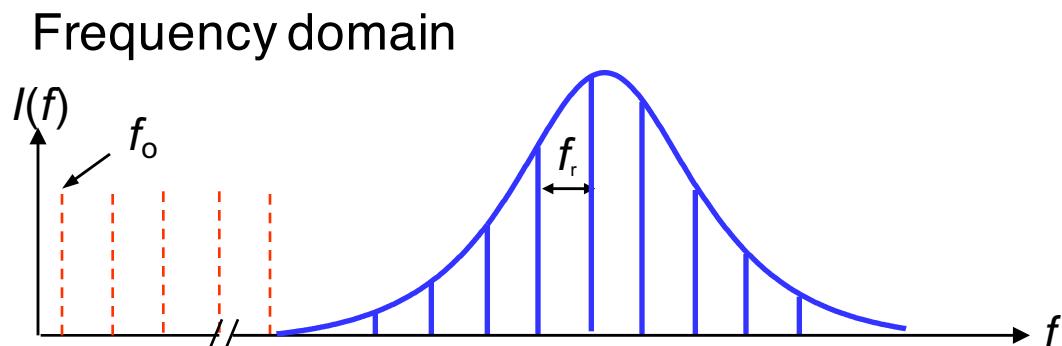
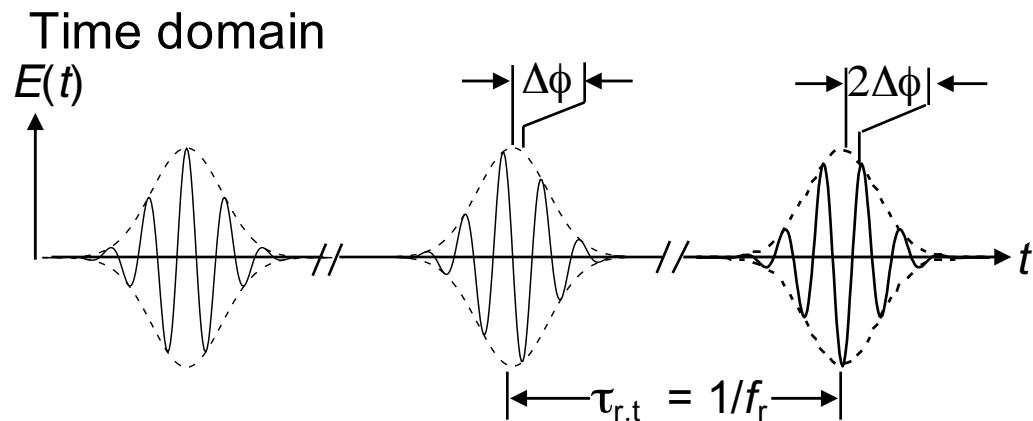
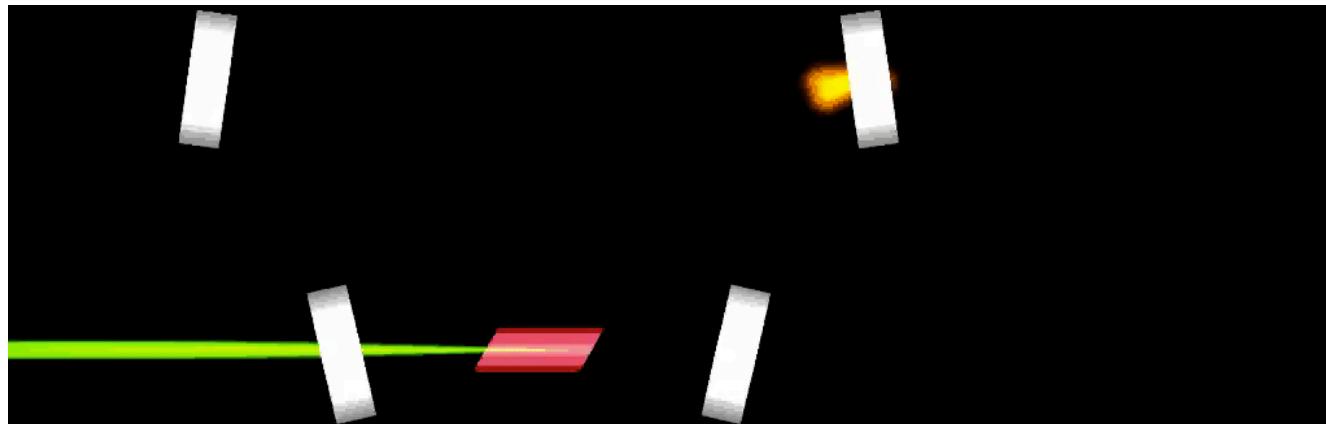
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## 4. Challenges and opportunities for frequency combs

# Mode-Locked Laser: Basis of the Frequency Comb

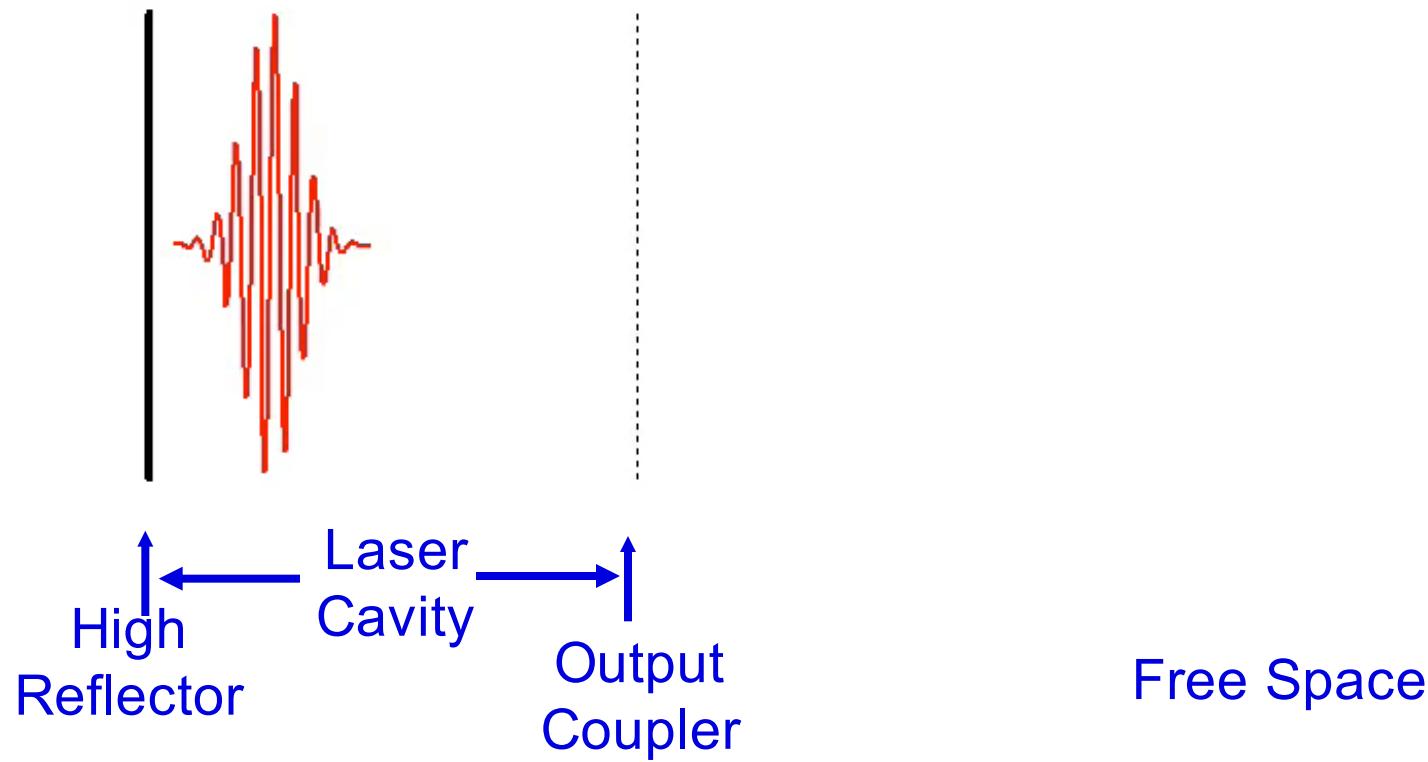


**Key Concept:**

Direct link between  
optical and microwave  
frequencies

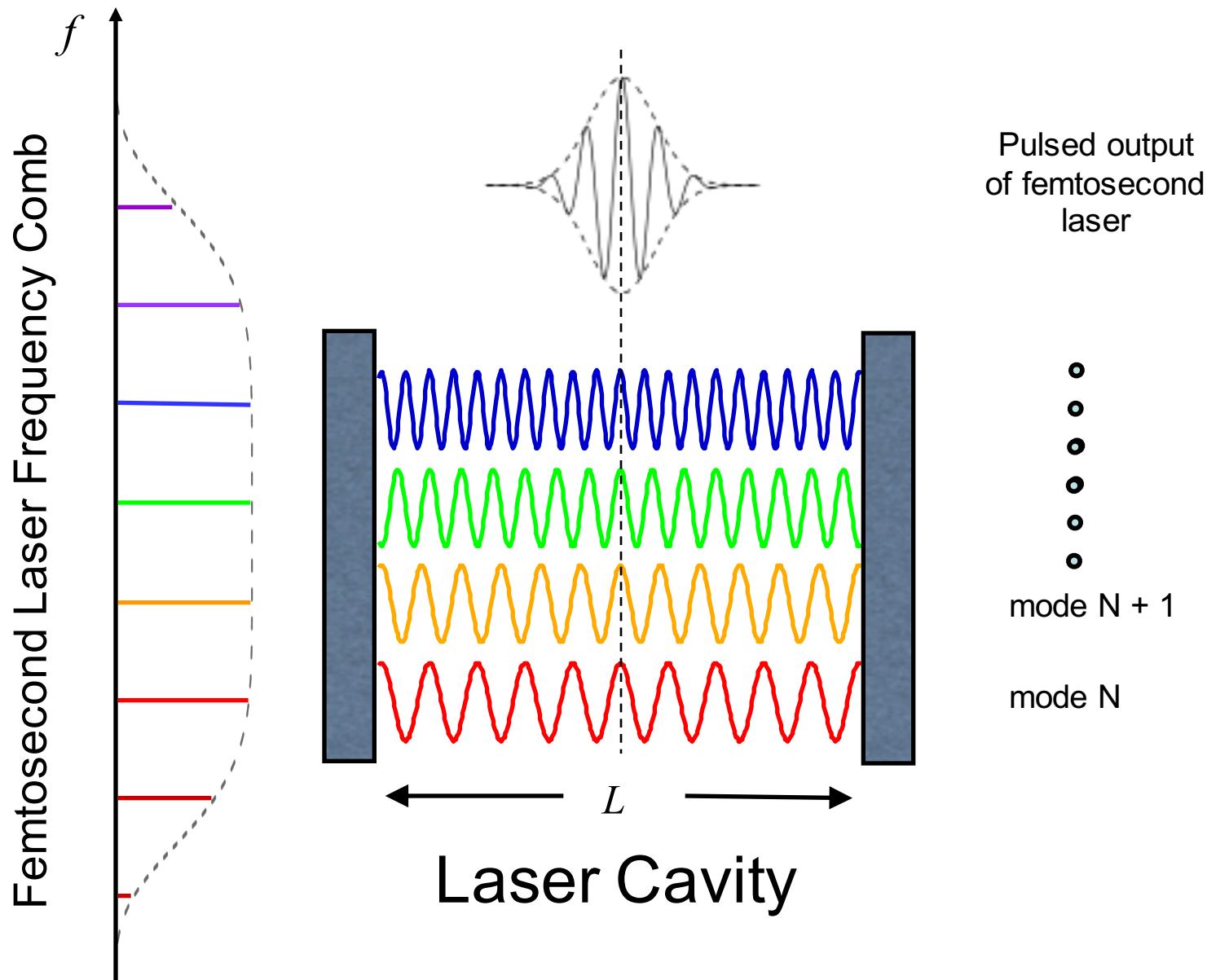
$$\nu_n = n f_r + f_o$$
$$n \sim 10^5$$

# Group and phase velocity in modelocked lasers



animation from Steve Cundiff

# The femtosecond mode-locked laser comb



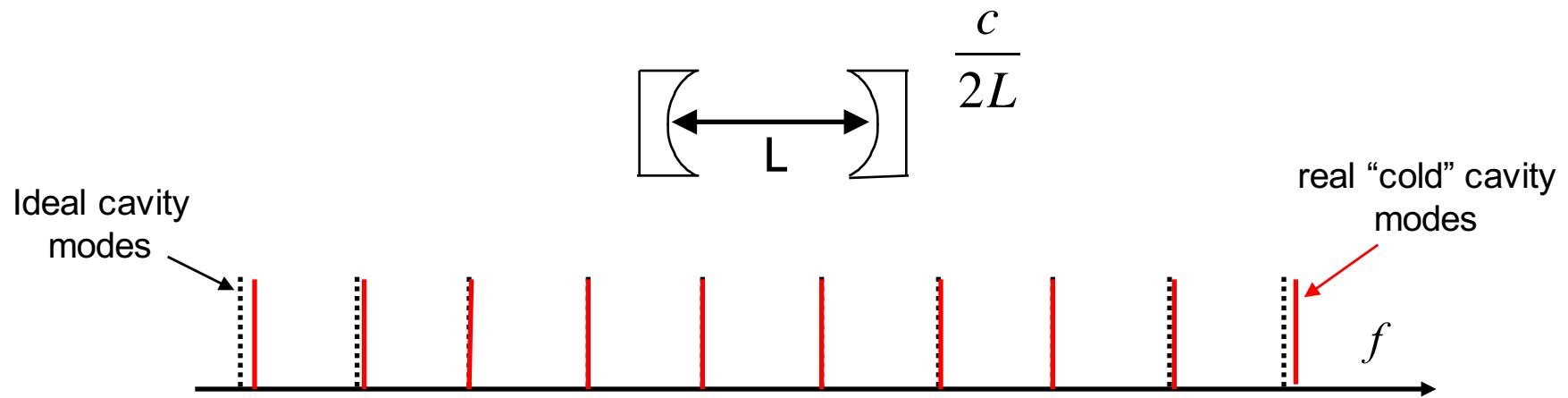
→ Cavity modes are locked in phase to generate a short pulse once every roundtrip time  $2L/v_g$

# How does it work?

→ All Femtosecond lasers require:

- Laser cavity + broadband gain source and optical components
- **Dispersion control**
- **Power-dependent gain or loss**
- **Phase modulation**

ideal mode spacing:

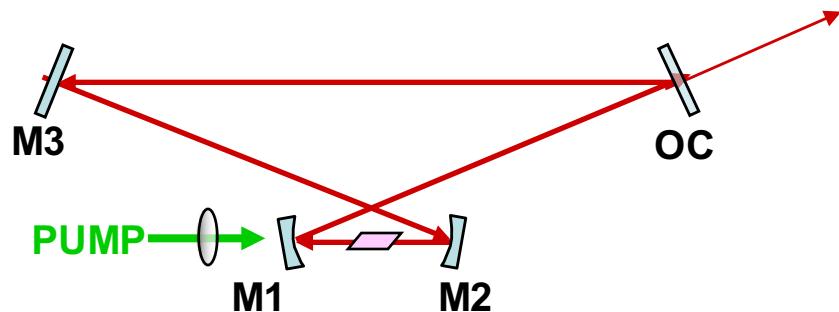


→ Due to dispersion, the cavity modes are not evenly spaced

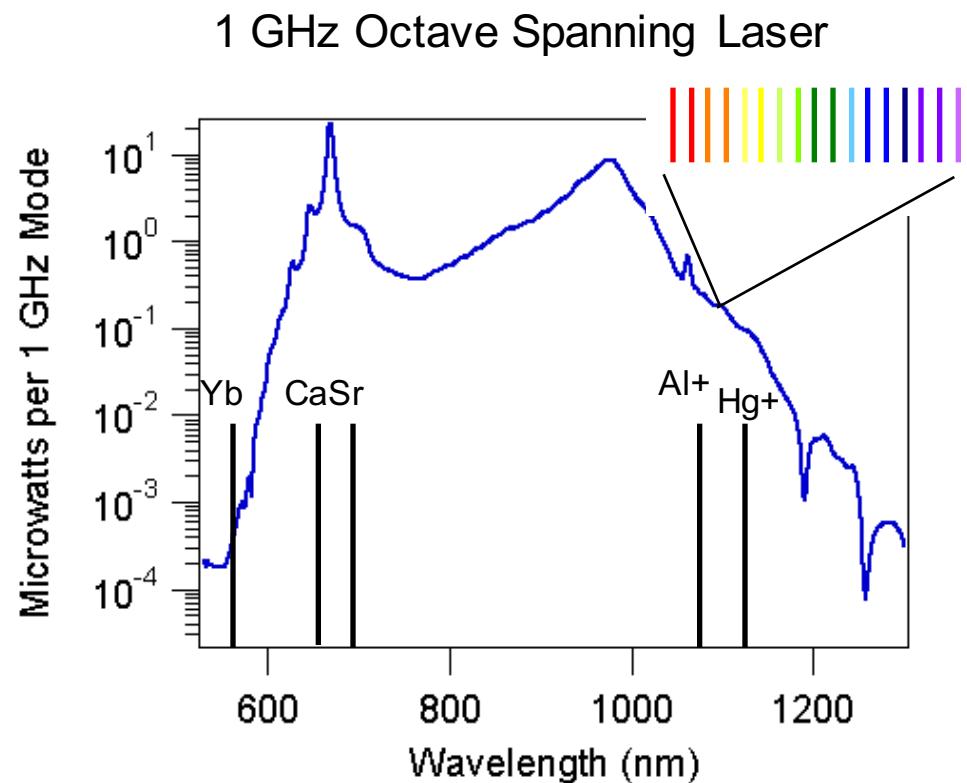
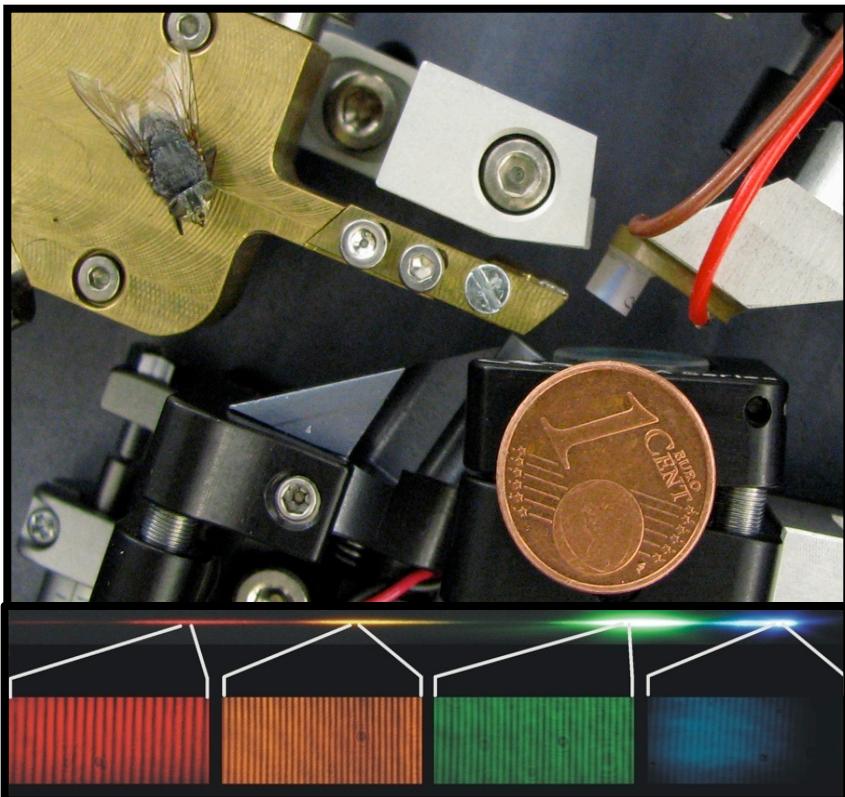
→ However, the **nonlinear phase-modulation** in a mode-locked laser provides the required synchronization of the modes, yielding a strictly uniform mode comb.

# GHz Rep Rate Ti:Sapphire Combs

T. Fortier, A. Bartels, D. Heinecke, M. Kirchner



10 GHz Self-referenced Ti:sapphire Laser

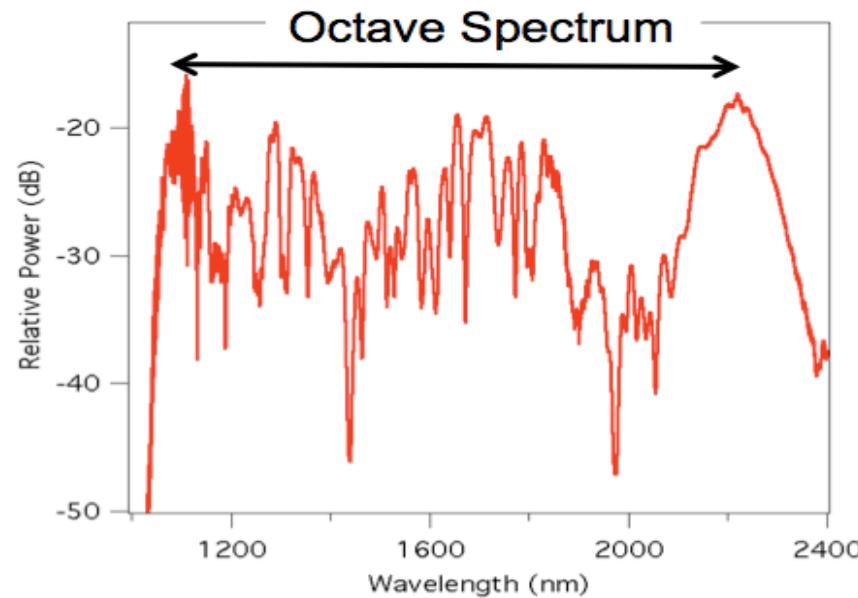
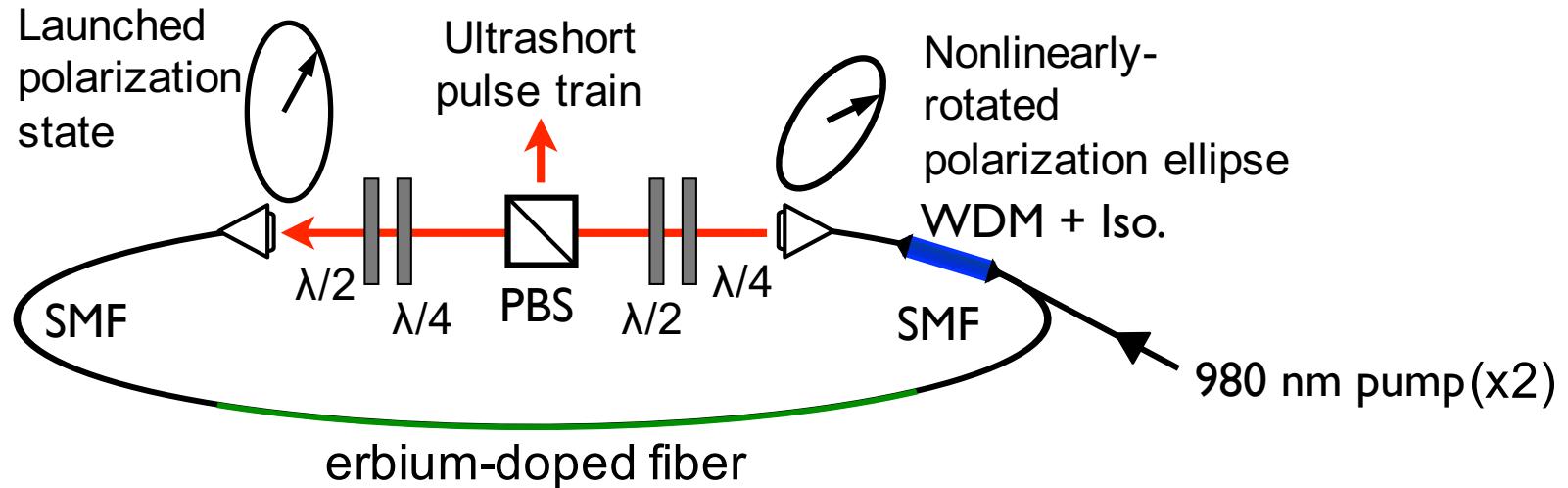


- A. Bartels, H Kurz, *Opt. Lett.* **27**, 1839 (2002)  
T. Fortier, A. Bartels, S. Diddams, *CLEO* (2005)  
T. Fortier, A. Bartels, S. Diddams, *Opt. Lett.* **31**, 1011 (2006)

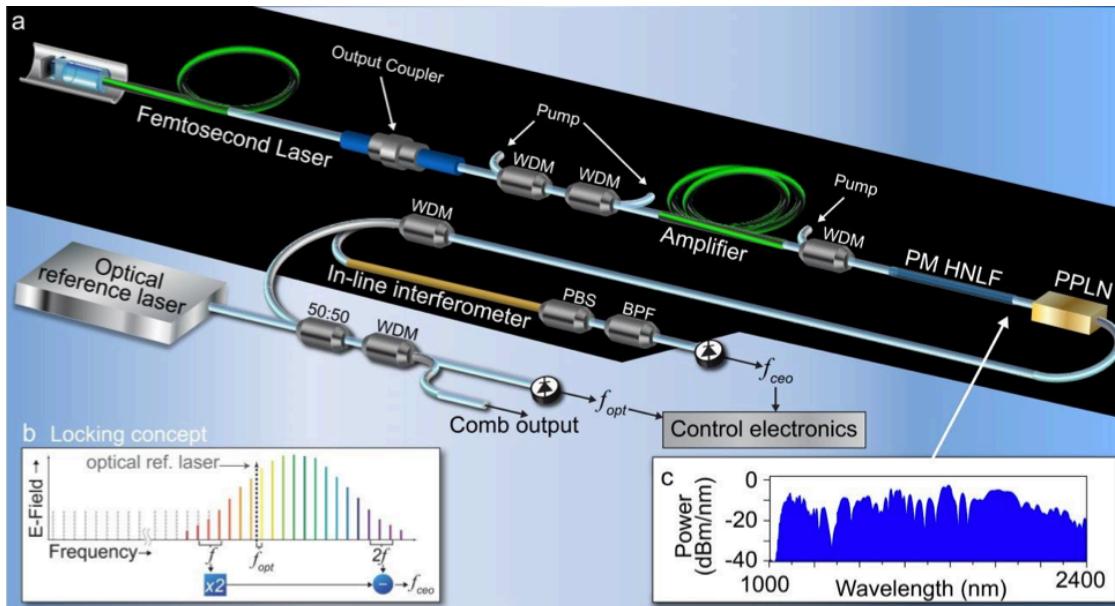
- Stabilized Comb =  $10^6$  Modes
- Hz-level linewidths
- Residual frequency noise at  $1 \times 10^{-19}$  level

# Er:fiber based frequency combs

→ mode-locking based on nonlinear polarization rotation



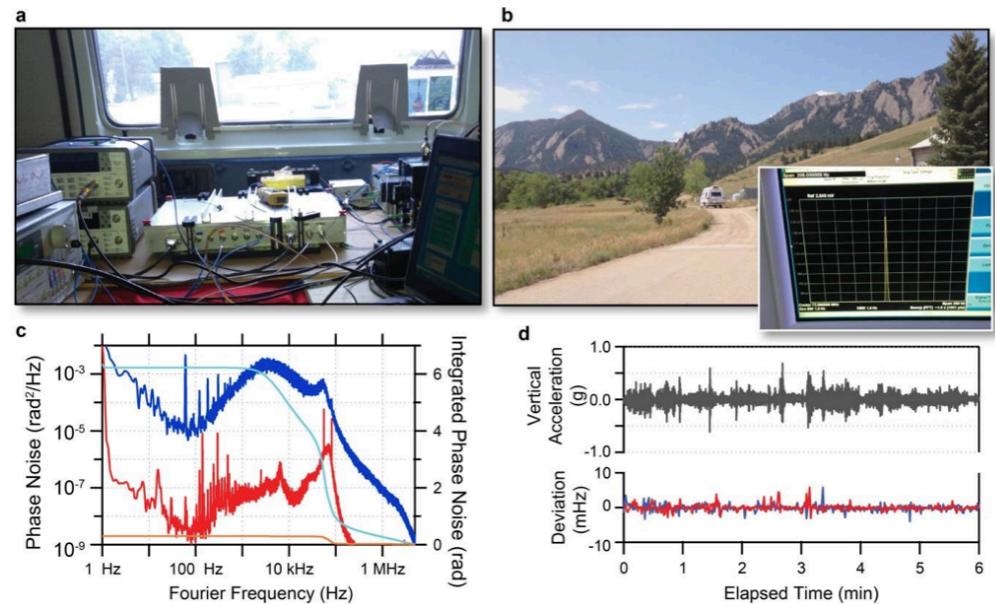
# Polarization-maintaining Er:fiber laser comb



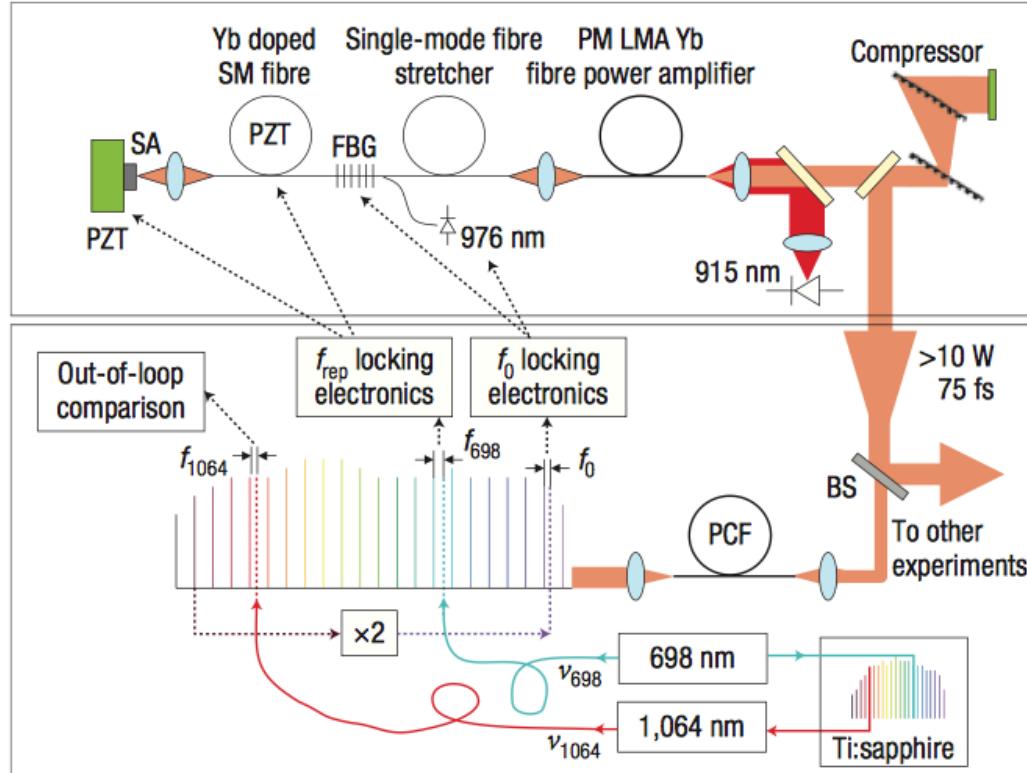
- Laser + amplifier + self-referencing are all constructed “in-line” with polarization-maintaining (PM) fiber optics.
- Laser is mode-locked with saturable absorber mirror
- Robust against environmental perturbations.

(Newbury group at NIST)

Frequency comb operates phase-locked in a moving vehicle.



# High-power Yb:fiber laser frequency comb

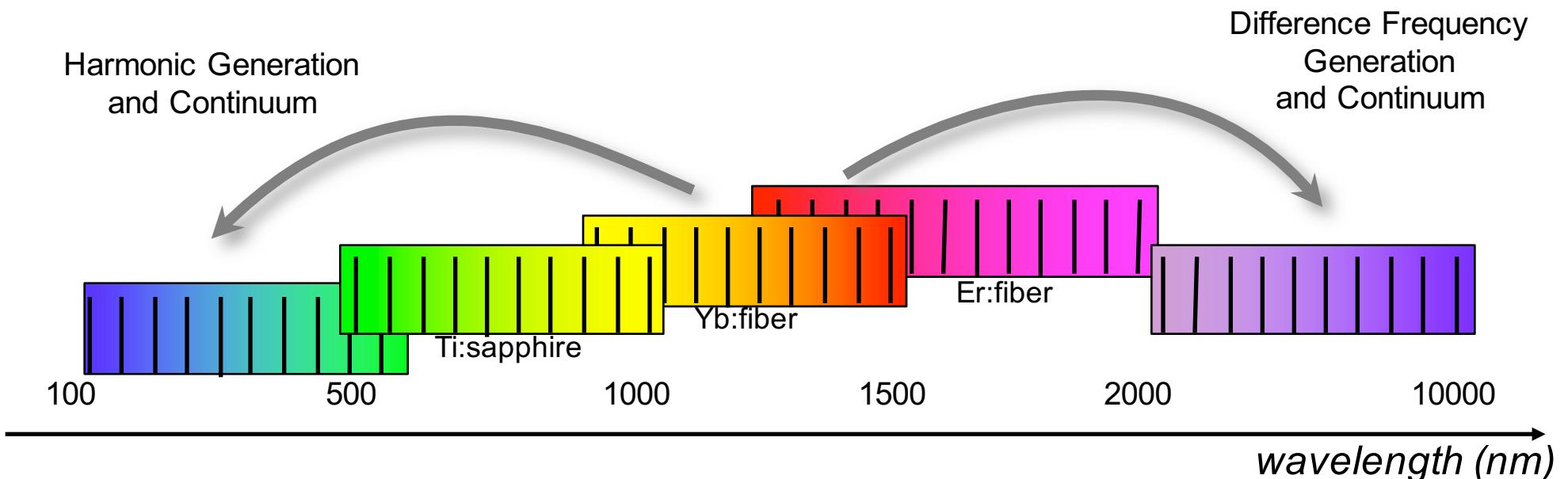


- Linear cavity design
- Saturable absorber end mirror for mode-locking
- Fiber Bragg grating provides output coupling and dispersion control
- **External amplification to ~80 W** followed by compression to ~100 femtosecond pulses

Schibli, et al. *Nature Photonics* **2**, 355 - 359 (2008)

# Frequency Comb Extension via Nonlinear Optics

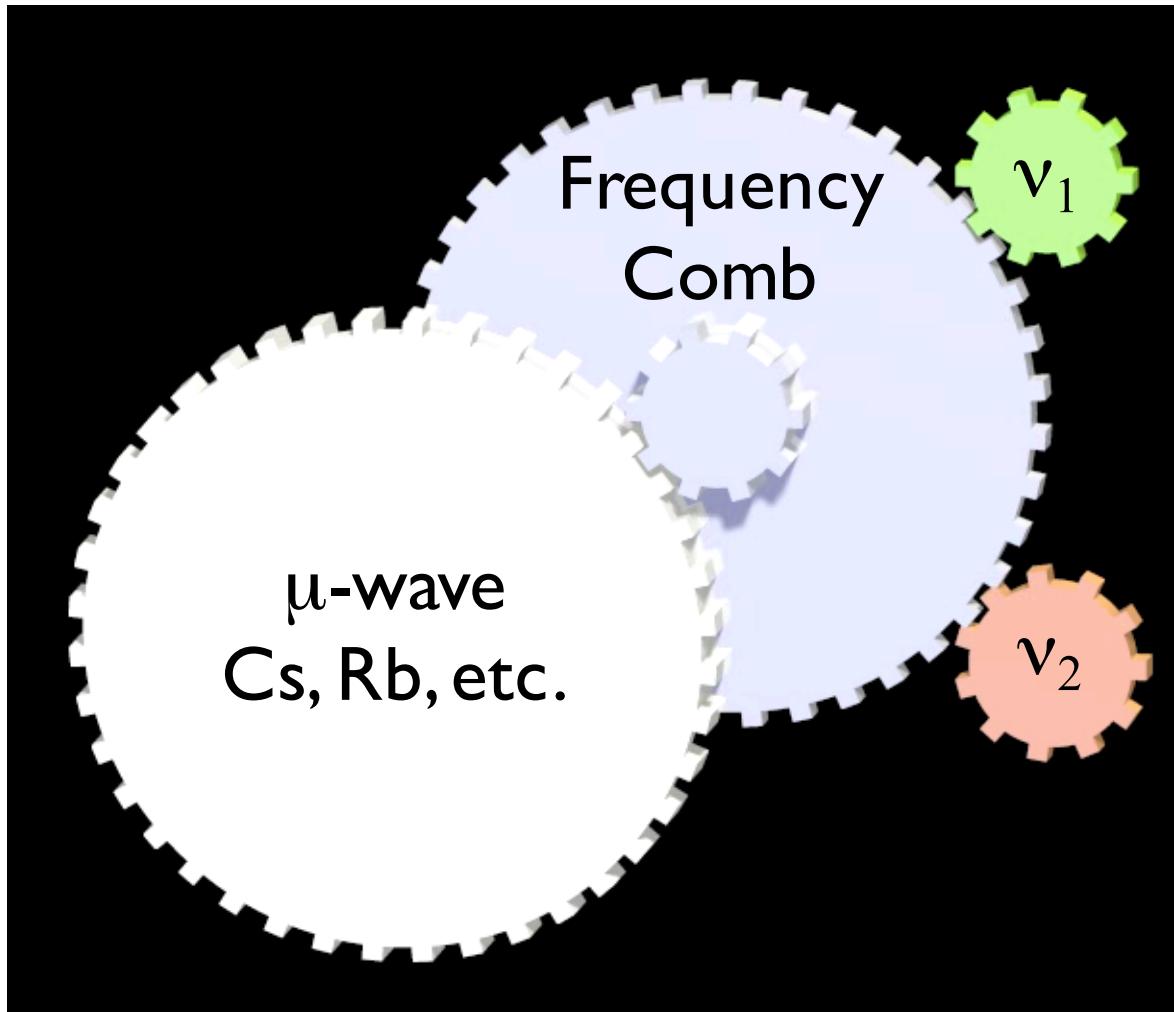
- Using a combination of harmonic generation, difference frequency generation and super-continuum, frequency combs have been extended from the UV to the infrared



- Some examples:
  - Extreme ultraviolet via harmonic generation: *Phys. Rev. Lett.* **94**, 193201 (2005); *Nature* **436**, 234-237 (2005); *Science* **307**, 400 (2005);
  - Mid-infrared comb generation via OPO, DFG and supercontinuum: *Opt. Lett.* **34**, 1330 (2009); *Opt. Lett.* **37**, 1400 (2012); *Lett.* **39**, 2056 (2014); *Opt. Lett.* **36**, 2275-2277 (2011).

# Multiple faces of a frequency comb

## 3. An optical clockwork



- Comb uncertainty at the 20<sup>th</sup> decimal place
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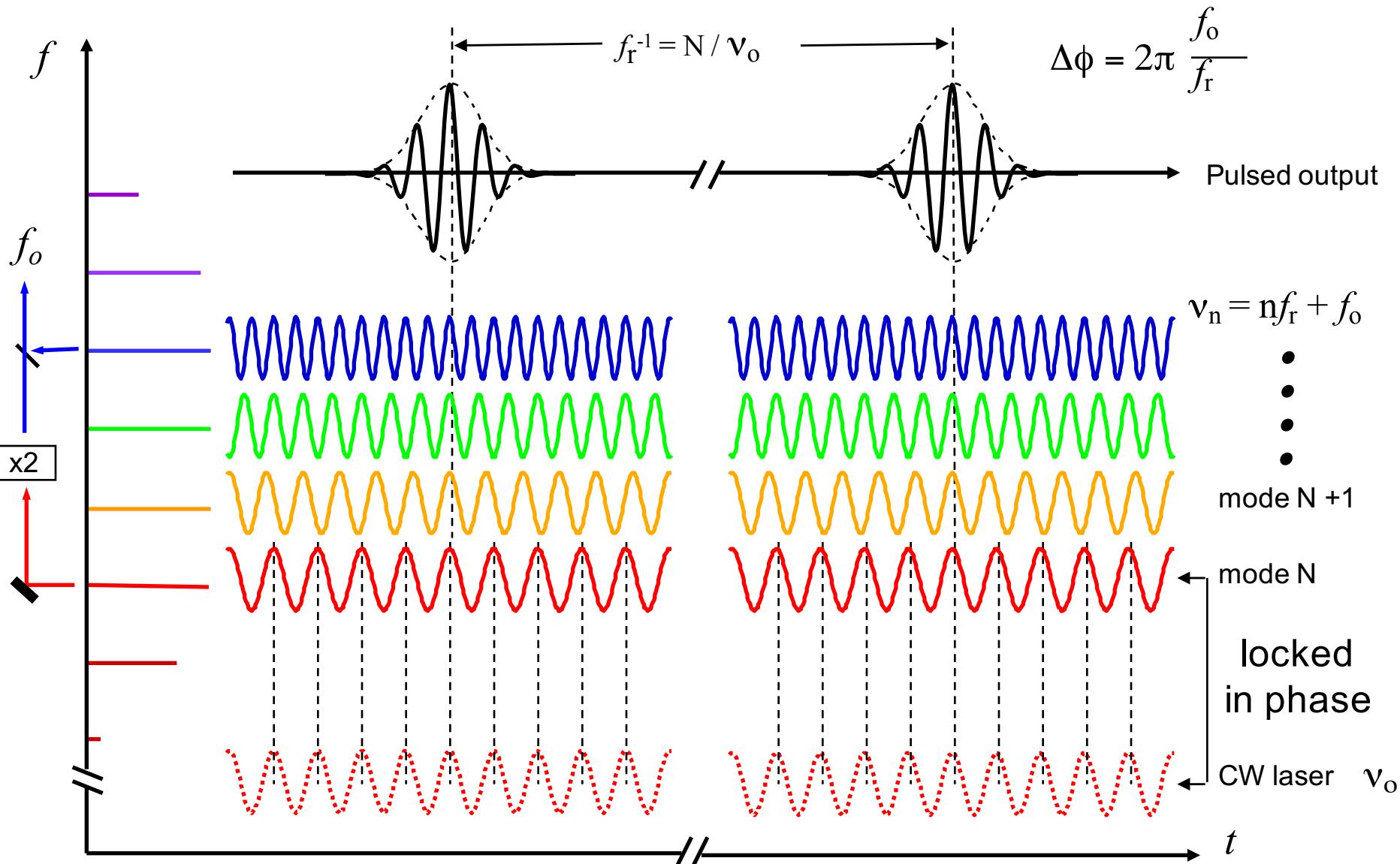
# Controlling the femtosecond laser comb

For most applications with the femtosecond laser frequency comb, we need to measure and control the two degrees of freedom of the frequency comb:  $f_o$  (offset frequency) and  $f_r$  (repetition rate)

$$\nu_n = n f_r + f_o$$

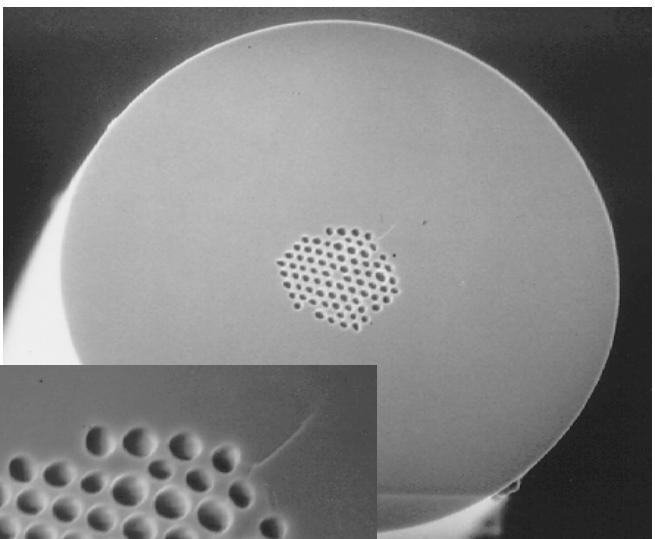
- $f_o$  measured by “self-referencing”
  - Need an octave-span spectrum
- $f_r$  controlled with a microwave source or a CW laser

# The laser comb and its control



Operation is fully reversible: Can lock at microwave and synthesize optical

# Microstructure optical fiber continuum generation

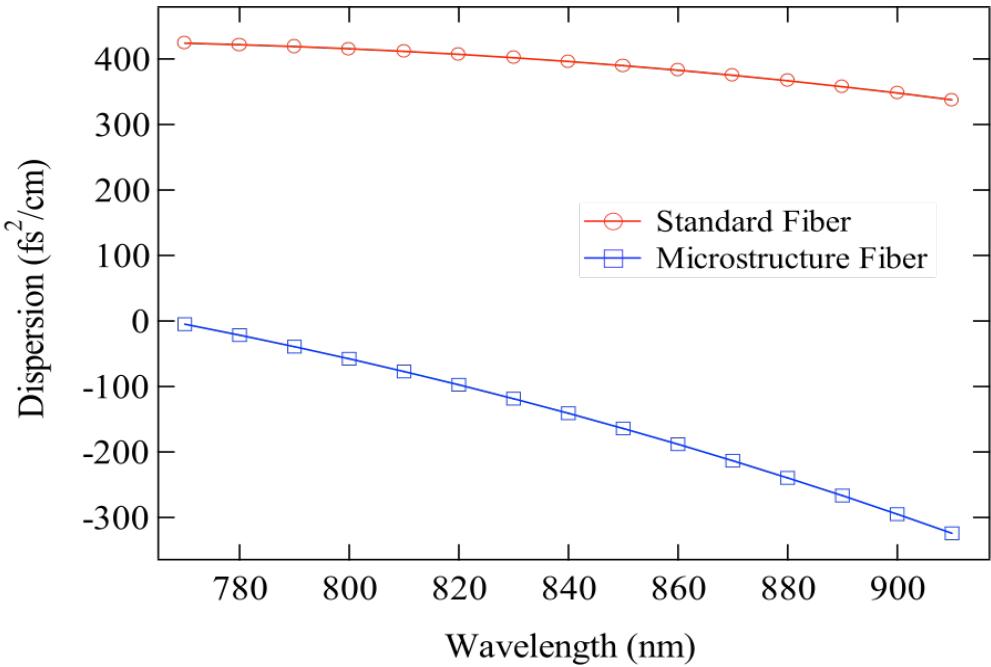
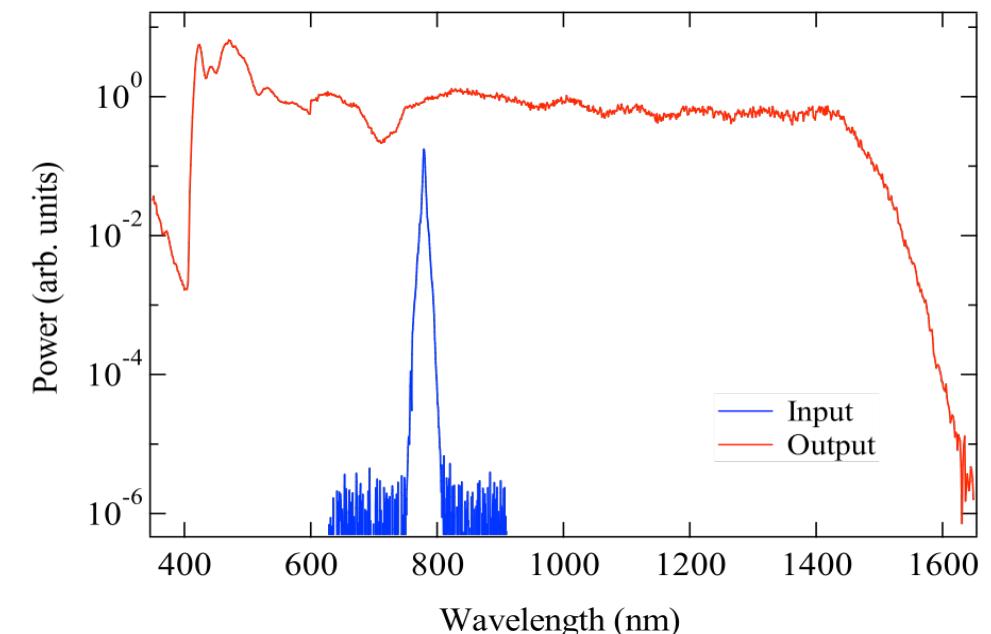


photos courtesy of  
Jinendra Ranka  
Lucent Technologies

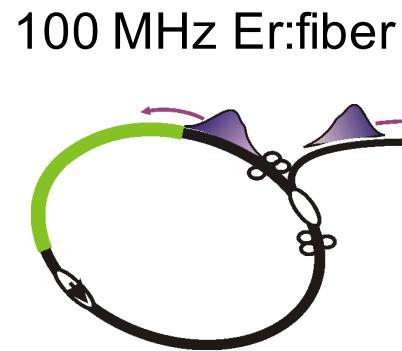
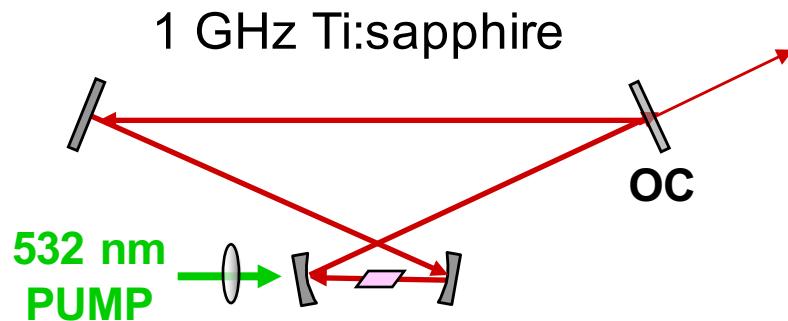
CLEO Postdeadline (CPD8) Baltimore (1999).

J. Ranka, R. Windeler, A. Stenzl, Opt. Lett. **25**, 25 (2000).

- Tight confinement of light leads to high nonlinearity and anomalous dispersion in the wavelength regime of femtosecond Ti:sapphire lasers
- Such fibers are available from commercial sources (ThorLabs, Crystal Fibre) and are developed in research labs (OFS, Univ. of Bath)

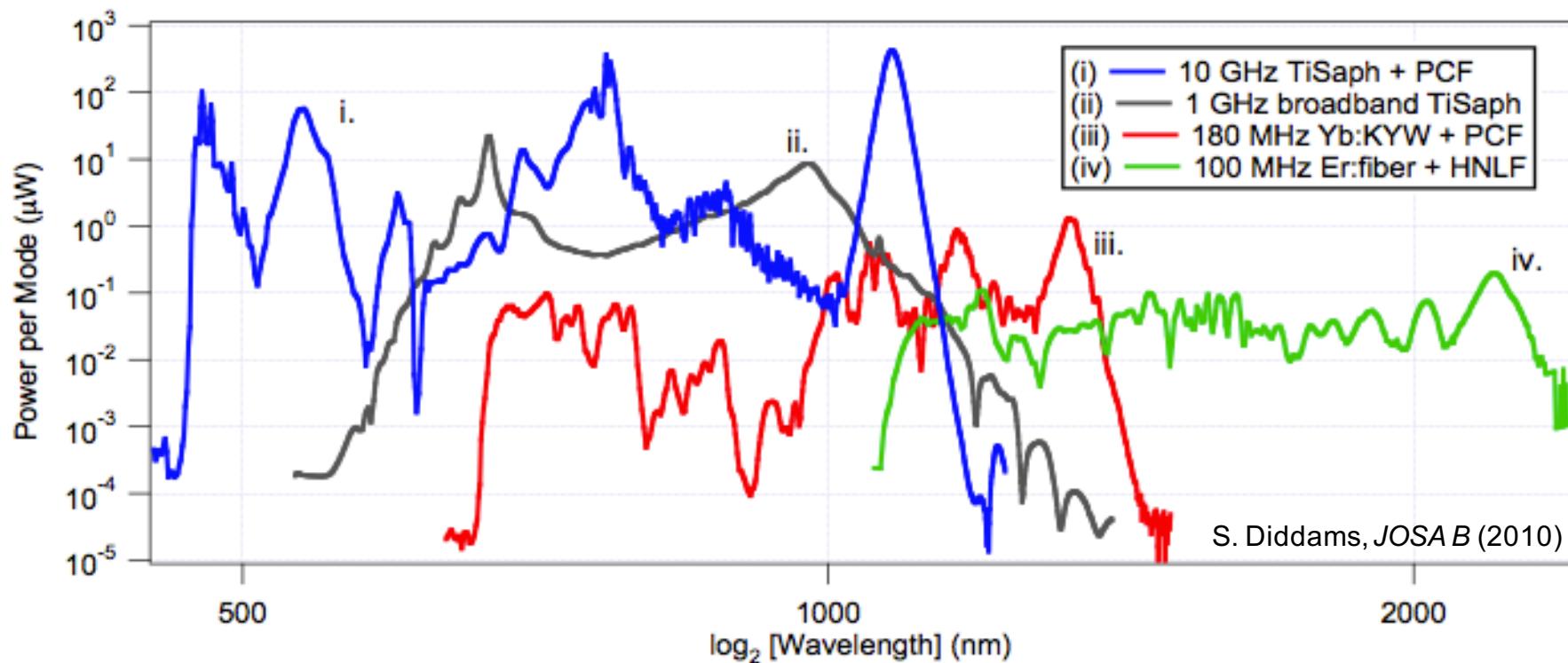


# Octave-Span Supercontinuum

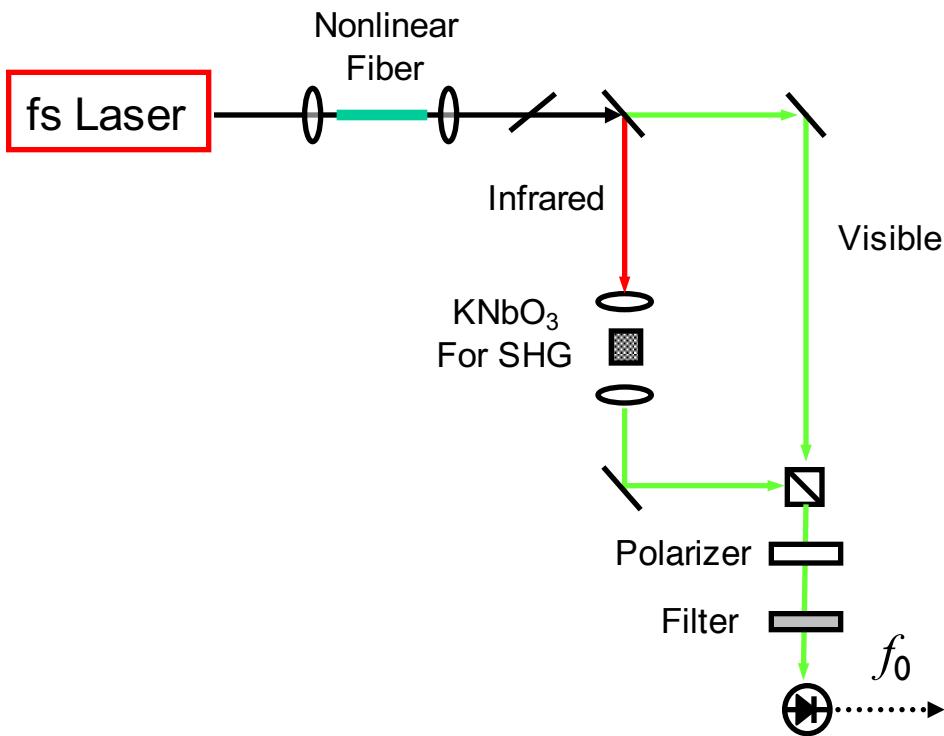


also....

Yb:fiber  
Yb:crystalline  
Tm:fiber  
.....

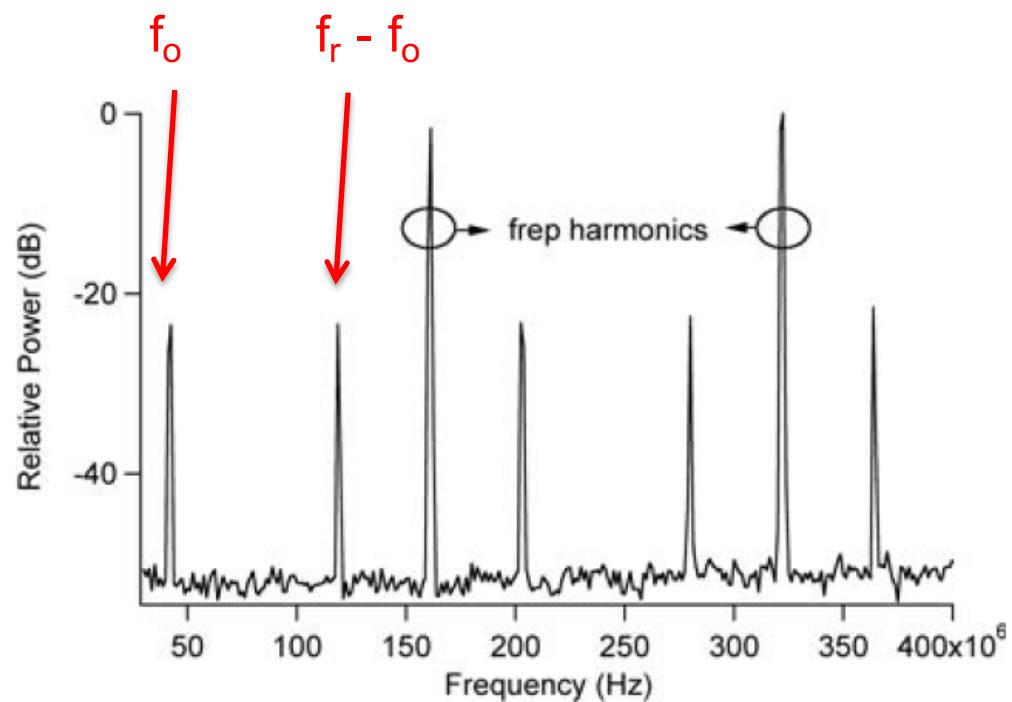


# Nonlinear interferometer for measuring $f_0$



Other interferometer designs exist:

- inline with waveguide PPLN
- Michelson



# First Self-Referenced Mode-locked Lasers

	<b>Ti:Sapphire</b> Jones 2000, Apolonski 2000	<b>Cr:LiSAF</b> Holzwarth 2001	<b>Er:fiber</b> Washburn 2004	<b>Cr:forster-ite</b> Kim 2005, 2006	<b>Yb:fiber</b> Hartl 2007	<b>Yb:KYW</b> Meyer 2008	<b>Er:Yb Glass</b> Stumpf 2009	<b>Tm:fiber</b> Phillips 2011
<b>center <math>\lambda</math></b>	800 nm	894 nm	1560 nm	1275 nm	1040 nm	1030 nm	1560 nm	1950 nm
<b>pulse length</b>	~10-50 fs	~50 fs	80-200 fs	30 fs	70-100fs	290 fs	170 fs	70 fs
<b>Pump source</b>	532 nm, doubled Nd:YVO	650 nm diode	980 or 1480 nm diode	1075 nm fiber laser	976 nm diode	980 nm diode	976 nm diode	793 nm diode
<b>Repetit-ion rate</b>	0.1 - 10 GHz	93 MHz	50-300 MHz	420 MHz	0.1-1 GHz	180 MHz	75 MHz	72 MHz
<b>E-to-O Efficiency</b>	~0.1%	1-2%	~1%	~0.5%	1-2%	~2-3%	~2-3%	??

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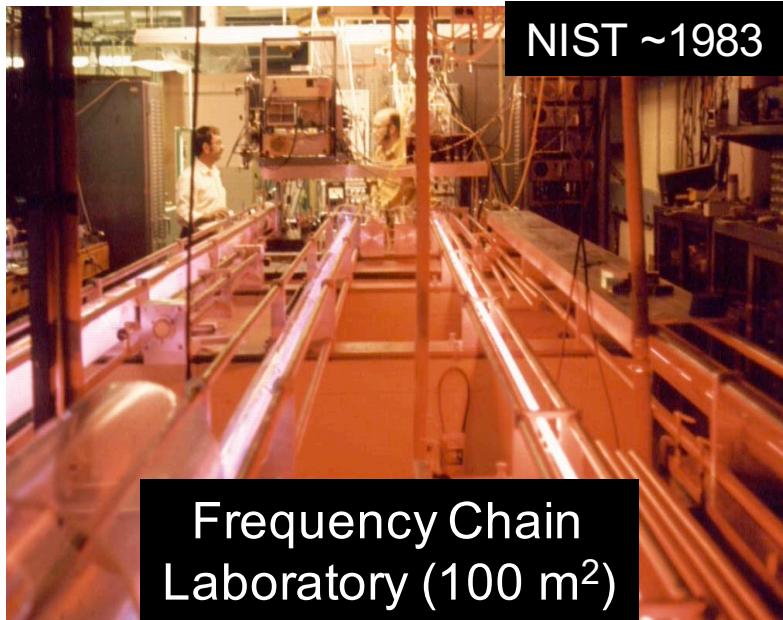
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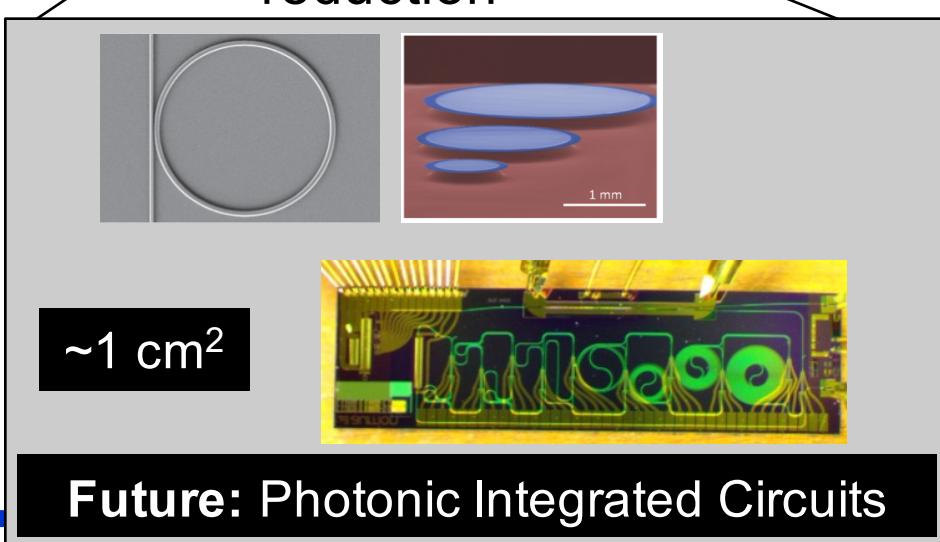
## 4. Challenges and opportunities for frequency combs

# Moving from Lab Scale to Chip Scale

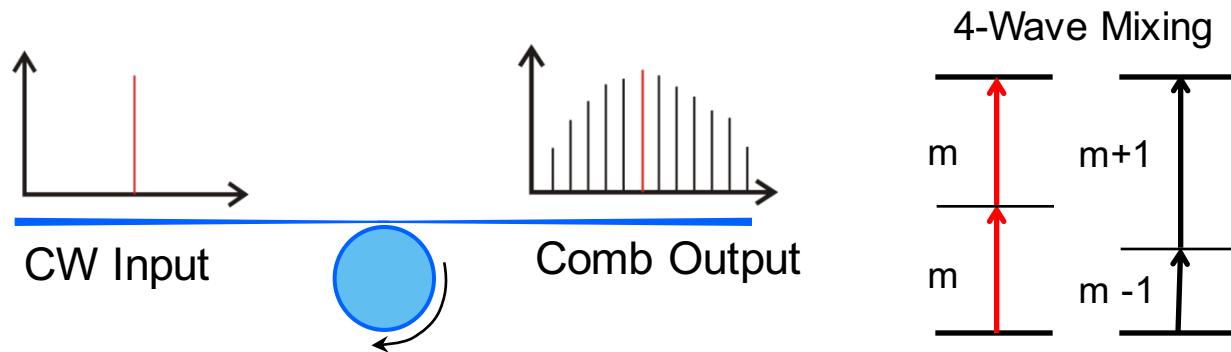


## Potential Impact:

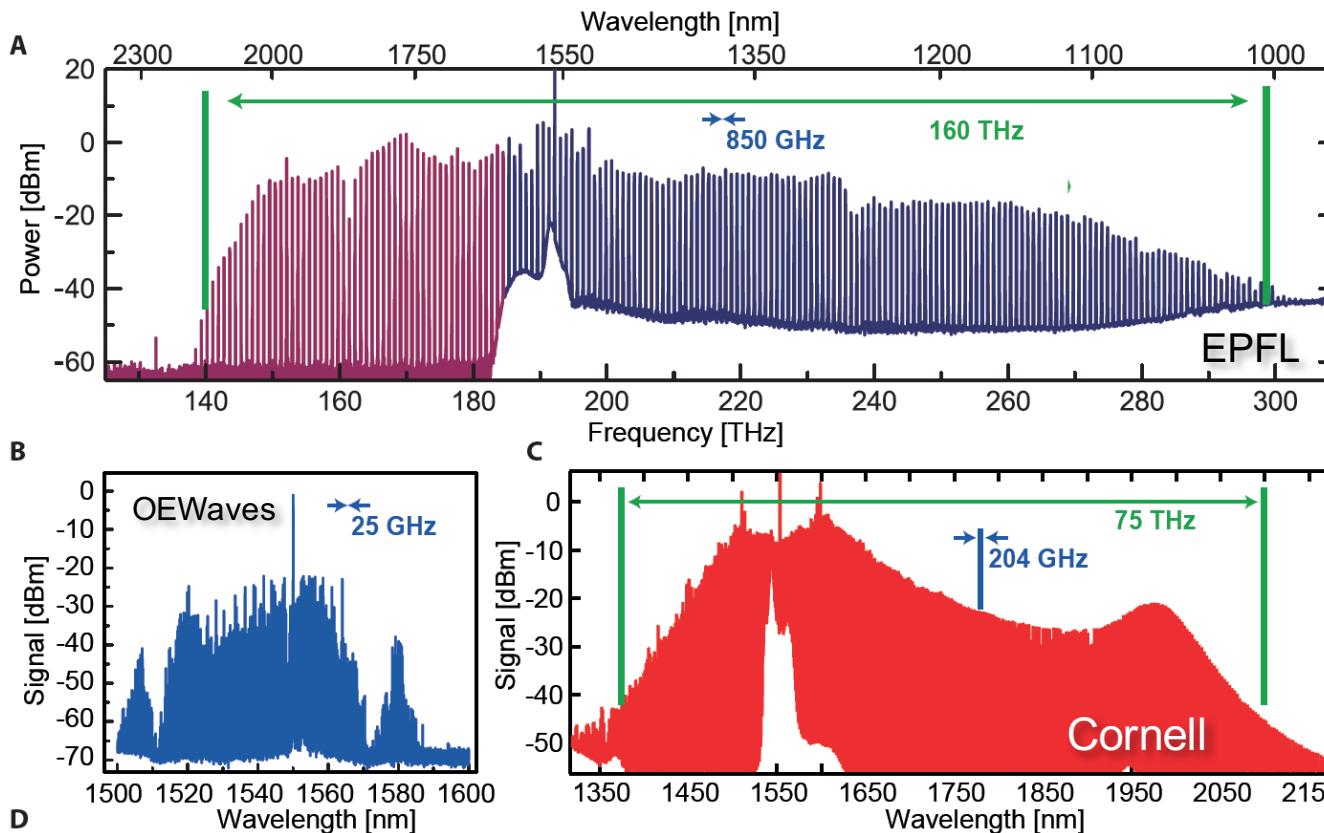
- Operation in any environment
- Chip scale clocks
- Inexpensive and mass produced
- Communication and navigation
- Sensing (environment, medical, manufacturing...)



# A Tiny Revolution in Frequency Combs



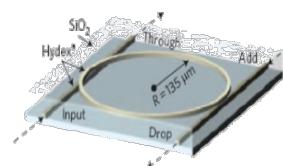
1. Energy conservation:  $2\omega_P = \omega_S + \omega_I$
2. Momentum conservation: linear + nonlinear
3. Line spacing given by resonator size



- Combs that appear regularly-spaced are possible, but not all are useful for metrology
- Understanding (controlling?) noise processes is critical
- What is happening in the time domain?

# Microresonator Gallery

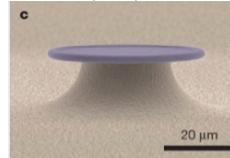
Hydex



Si:Nitride



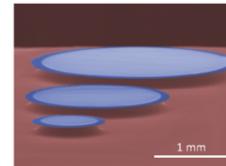
Silica toroid



Crystals



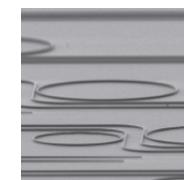
Silica wedge



Quartz



Diamond



Al:Nitride



RMIT

Cornell,  
Purdue, NIST  
G-burg,  
EPFL,  
UCLA

MPQ,  
EPFL,  
Caltech

OEWaves  
JPL  
EPFL

Caltech

NIST

Harvard

Yale

## Key Properties

- High-Q cavity ( $>10^9$ )
- Small mode volume
- Mode-spacing given by perimeter
- Low & controllable dispersion
- Integrated chip-scale package

[1] L. Razzari, D. Duchesne, M. Ferrera, R. Morandotti, S. Chu, B. E. Little & D. J. Moss (Nature Photonics **4**, 41 – 45, 2010)

[2] J.S. Levy, A. Gondarenko, M.A. Foster, A.C. Turner-Foster, A.L. Gaeta & M. Lipson (Nature Photonics **4**, 37 – 40, 2010)

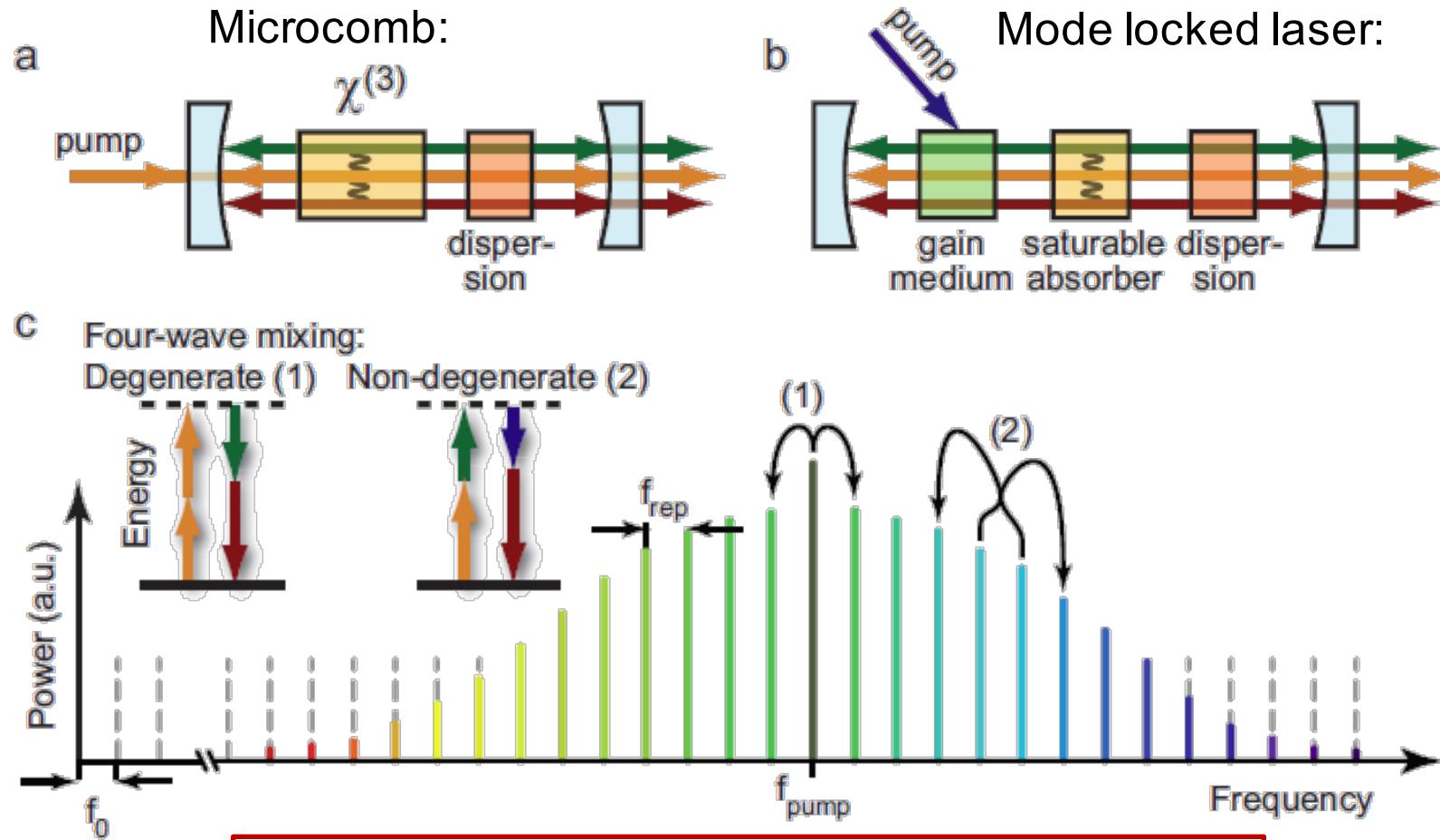
[3] P. Del'Haye, A. Schliesser, O. Arcizet, T. Wilken, R. Holzwarth, T. J. Kippenberg (Nature **450**, 1214-1217, 2007)

[4] A.A. Savchenkov, A.B. Matsko, V.S. Ilchenko, I. Solomatine, D. Seidel, and L. Maleki (Phys Rev Let. **101**, 093902, 2008)

[5] S.B. Papp and S.A. Diddams (PRA **84**, 053833, 2011)

[5] F. Ferdous, H. Miao, D. E. Leaird, K. Srinivasan, J. Wang, L. Chen, L. T. Varghese & A. M. Weiner (Nature Photonics **5**, 770, 2011)

# Comb Generation Principle

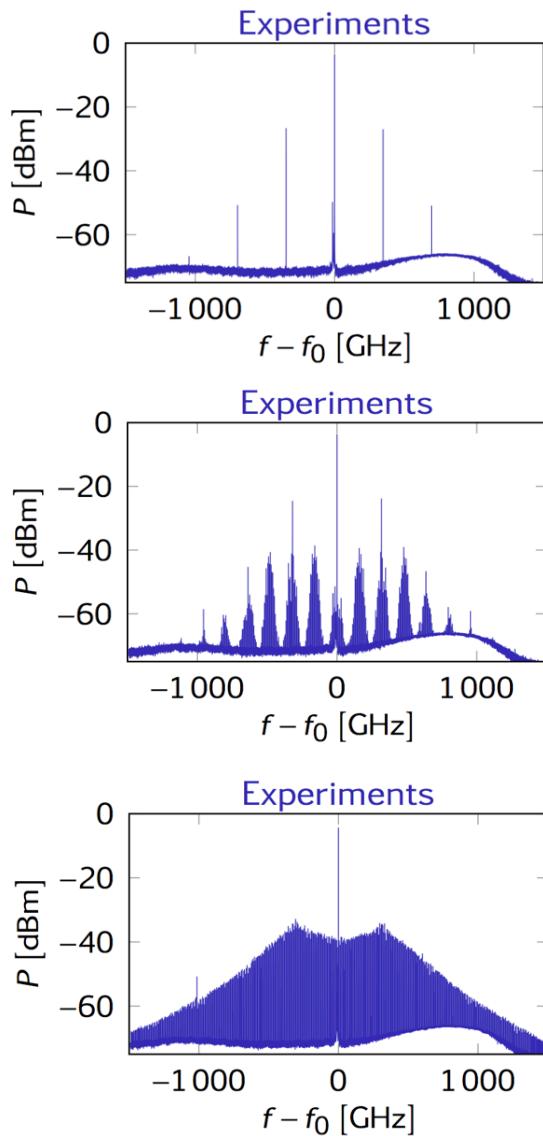


## Microcomb:

- Parametric gain vs. stimulated emission
- Pump laser part of comb (offset tuning)
- No saturable absorber

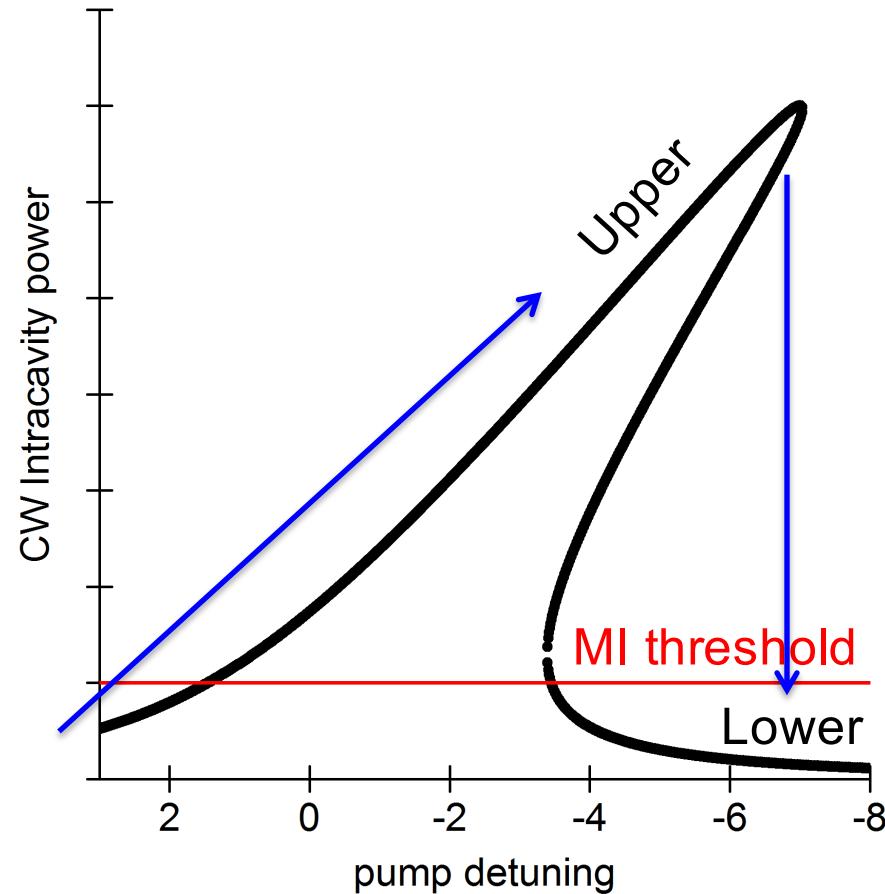
# Kerr Microcomb Formation

Upper branch:  
Modulation instability

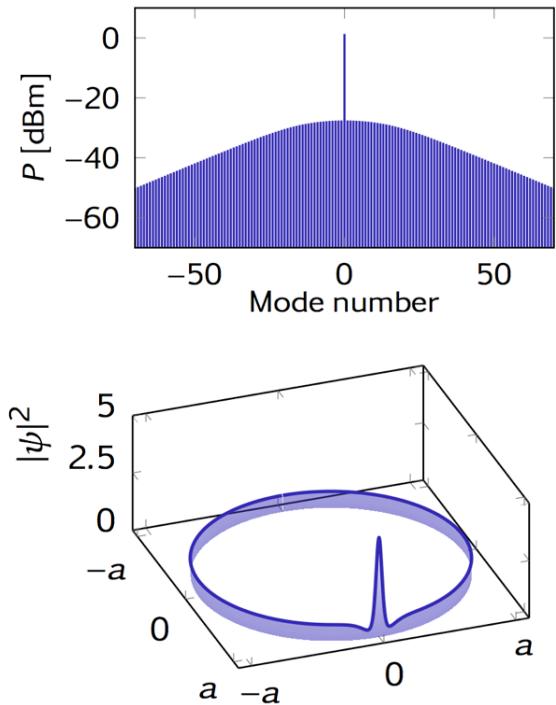


## Kerr-nonlinear microcavity

$$\frac{\partial E}{\partial t} = -(1 + i\Delta)E + i|E|^2 E - i\frac{\beta}{2} \frac{\partial^2 E}{\partial \theta^2} + F$$



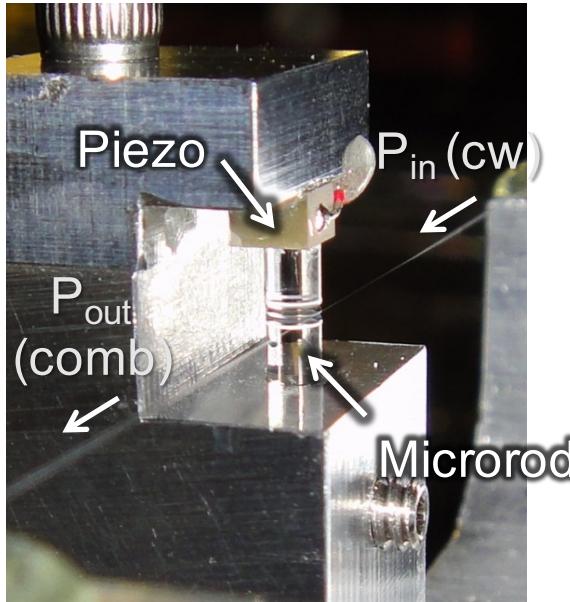
Lower branch:  
Cavity soliton



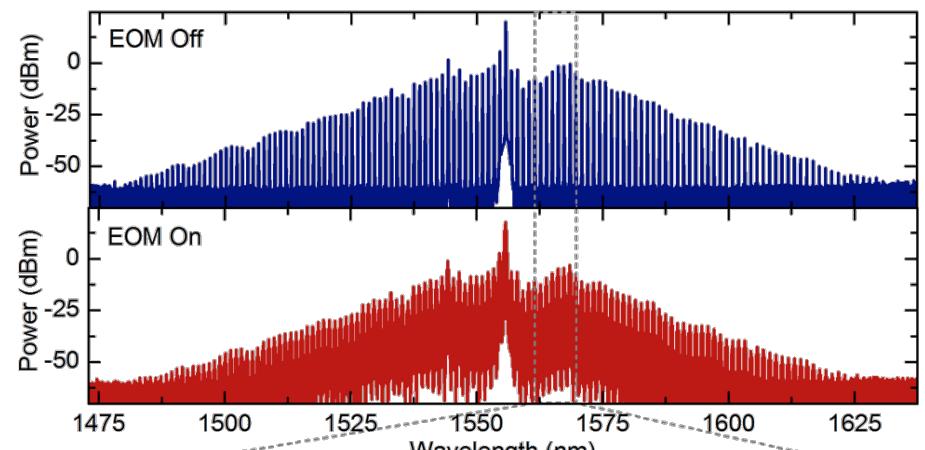
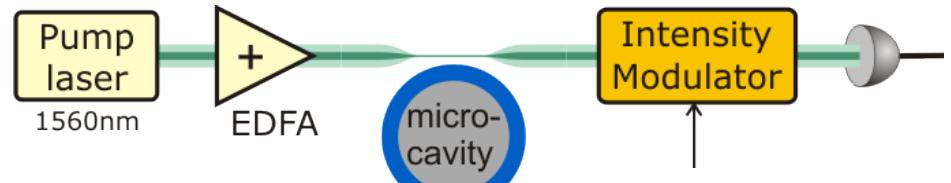
# Frequency control of microcombs

Demonstrated Frequency Control:  $<10^{-15}$  at 1s

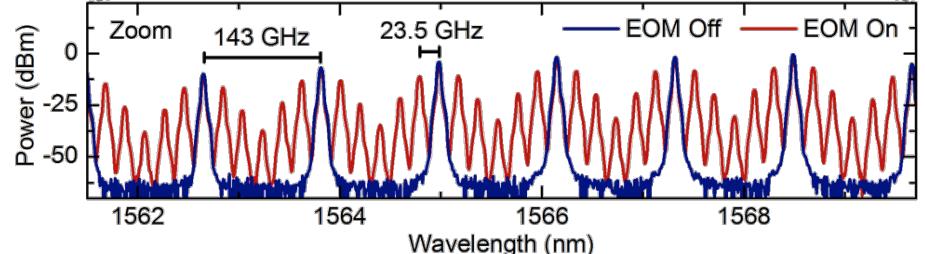
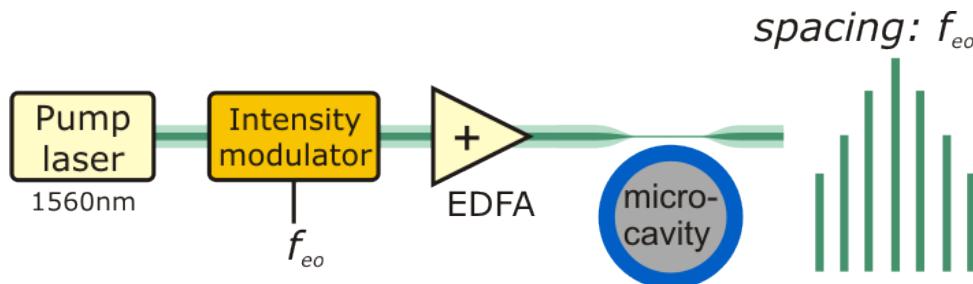
Mechanical control (wide BW)



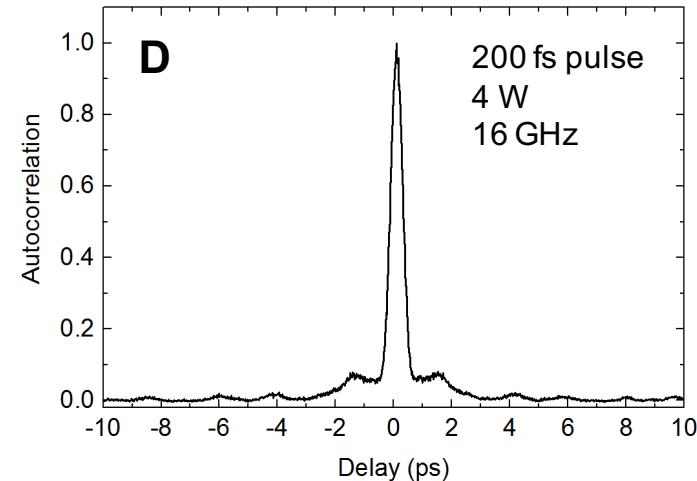
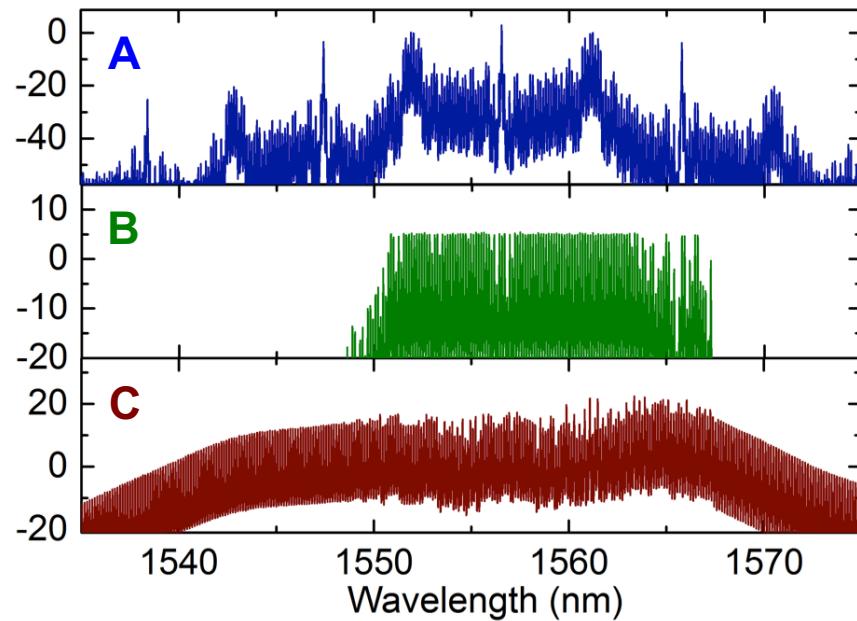
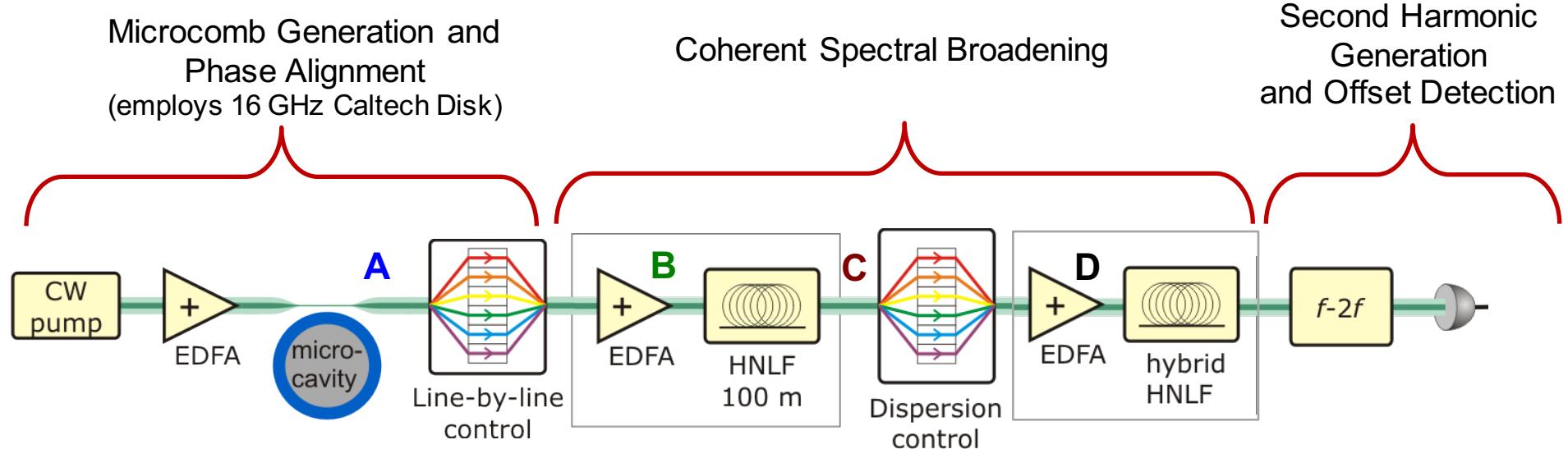
Hybrid EOM + microcomb (high rep. rate)



Parametric seeding (deterministic control)

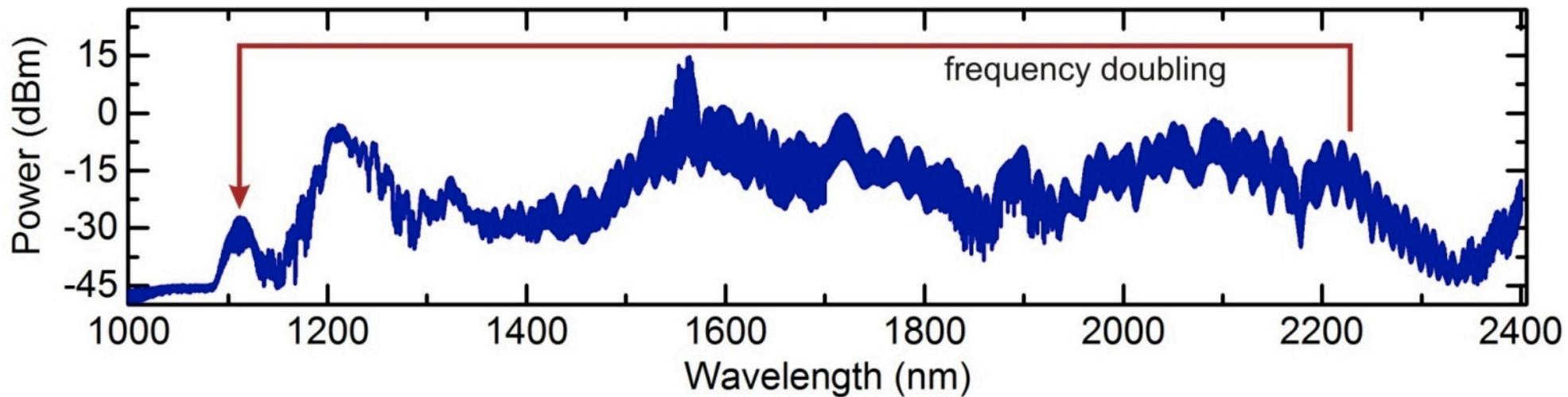


# Self-Referencing a Microcomb



Pascal Del'Haye, Aurélien Coillet  
also: Kippenberg group

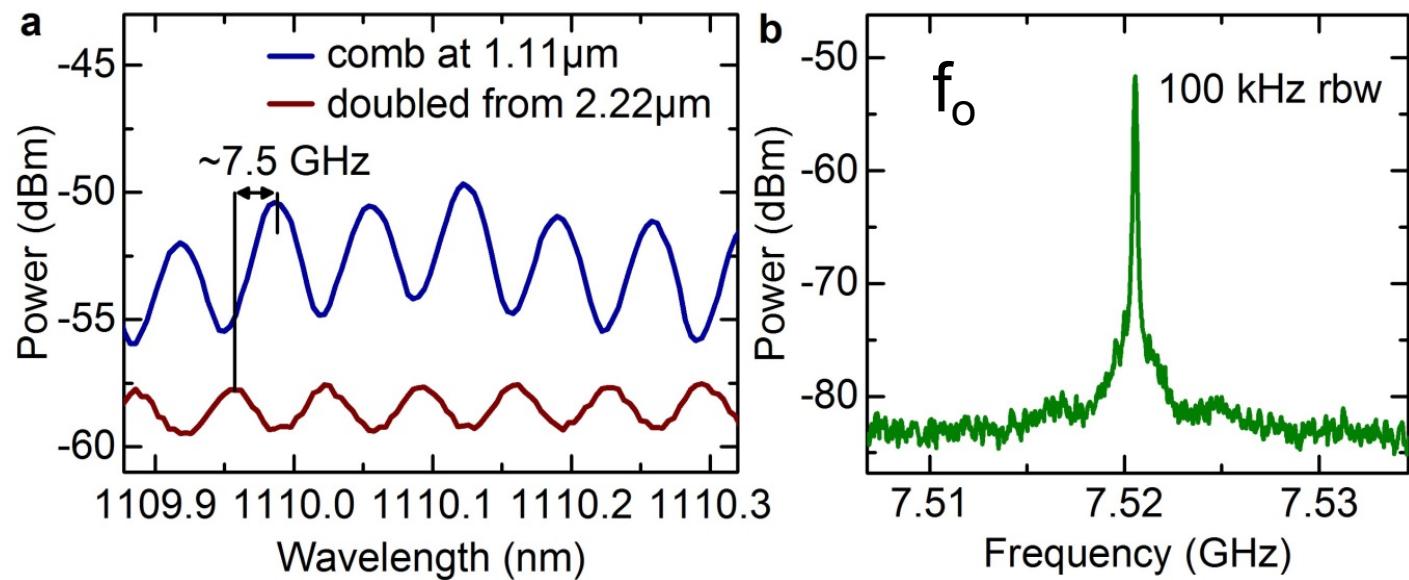
# Self-Referencing a Microcomb



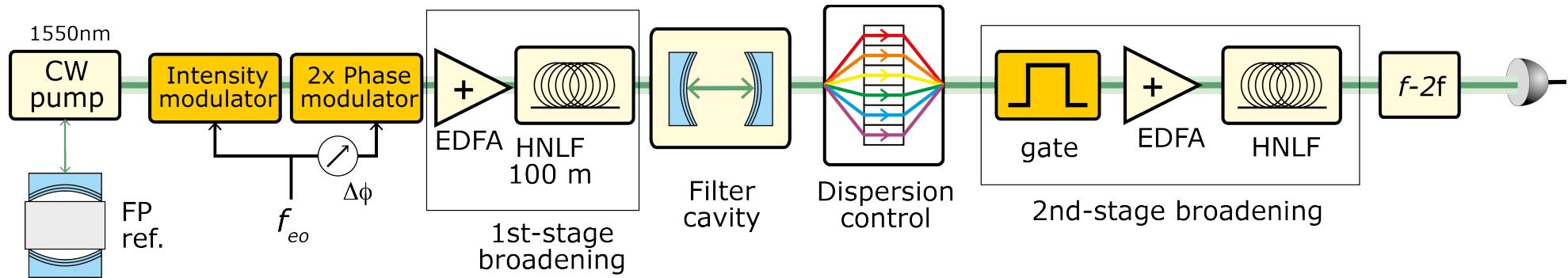
f-2f self-referencing

Highest reprise for self-referencing (16.4 GHz)

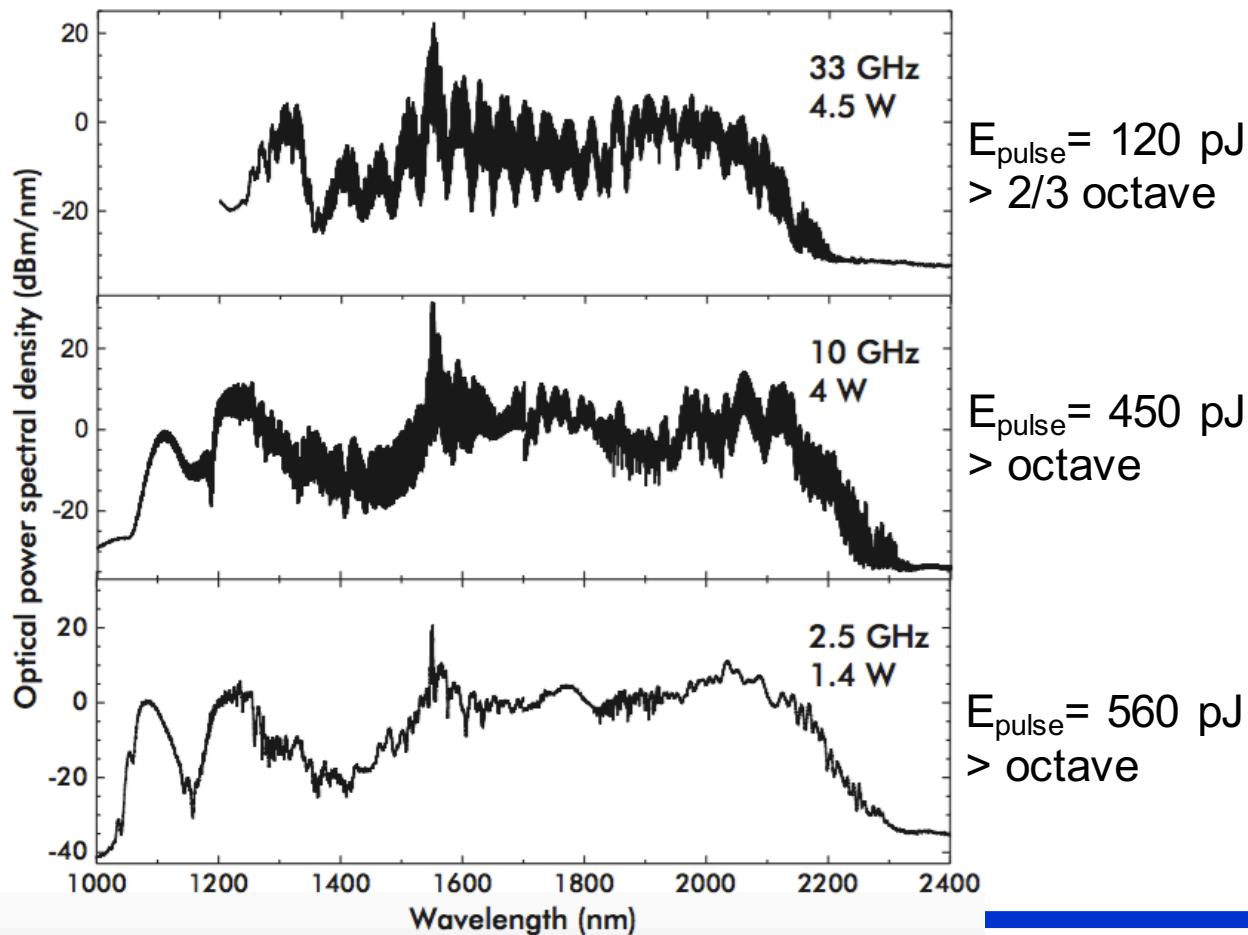
Highest measured  $f_o$  (7.5 GHz)



# EOM Comb: Self-referencing a CW laser



see Scott Papp's talk



External broadening  
Dual-stage pulse compression,  
amplification, and nonlinear  
broadening

+

Frequency noise control

Myslivets et al., Opt. Exp., **20**, 3331 (2012)  
Ishizawa et al., Opt. Exp., **19**, 22402 (2011)  
Cole et al., arXiv:1310.4134 (2013)  
Beha et al., arXiv (2015)

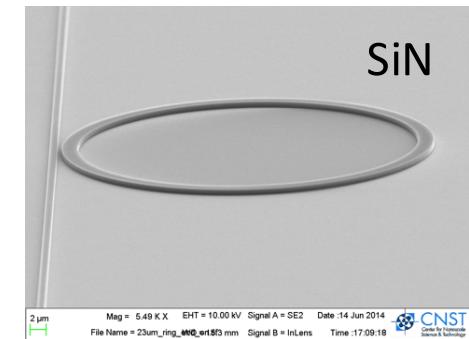
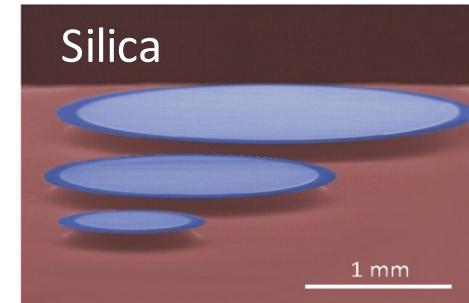
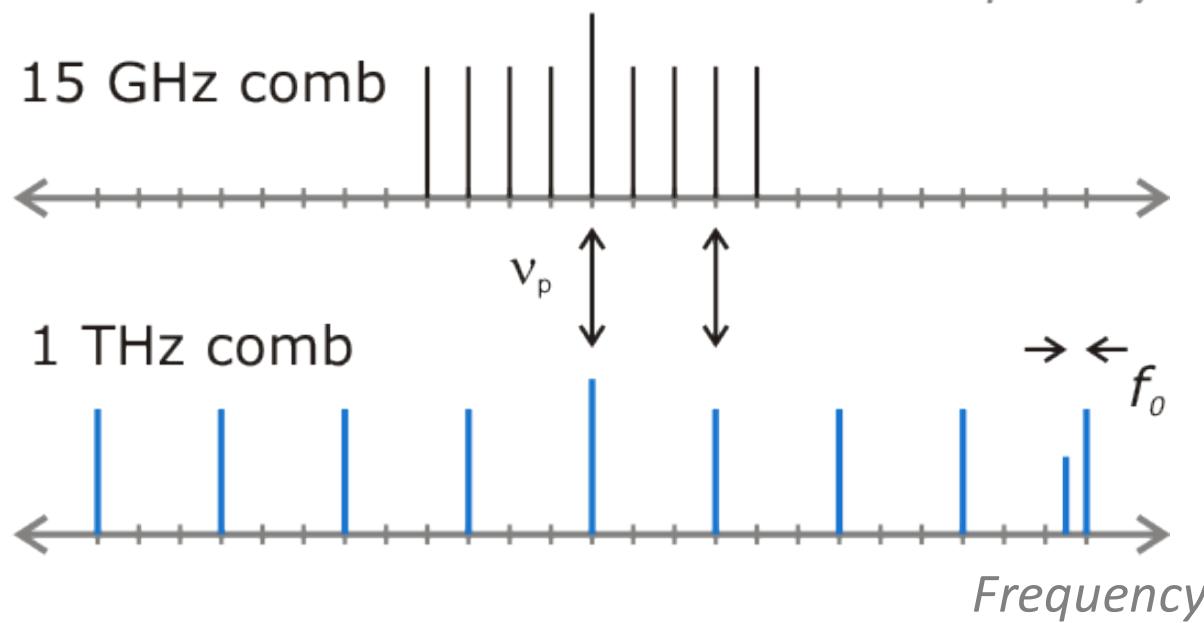
# Self-referencing on a chip?

**Goal:** An octave-span, self-referenced microcomb on a chip

**Challenges:** Power, frequency control & basic nonlinear optics

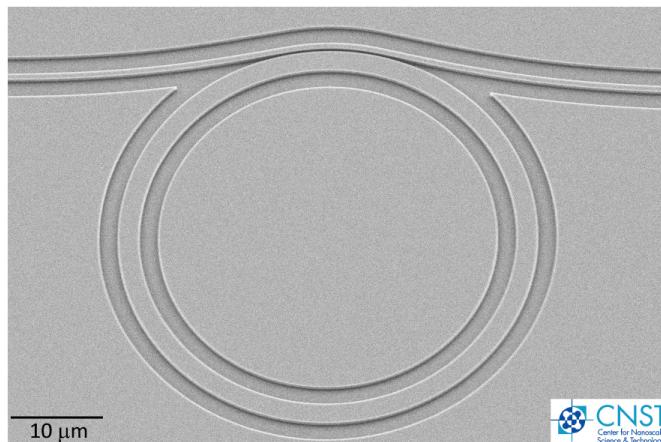
**Approach:** Dual reduction gear  $200 \text{ THz} \rightarrow 1 \text{ THz} \rightarrow 15 \text{ GHz}$

**Leverage:** Photonic integration (pump laser, PPLN, photodiodes)



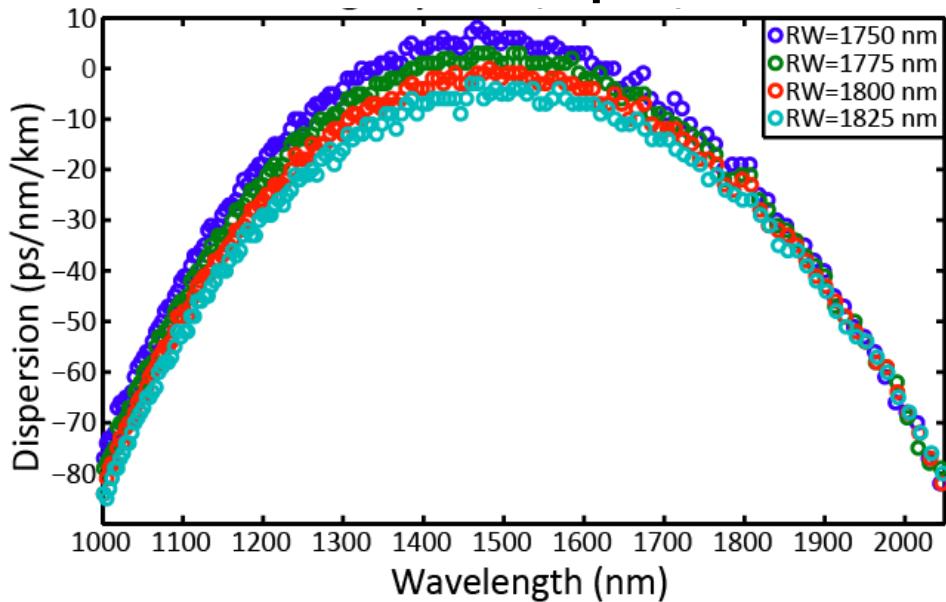
# THz microcomb chip

1 THz SiN resonator

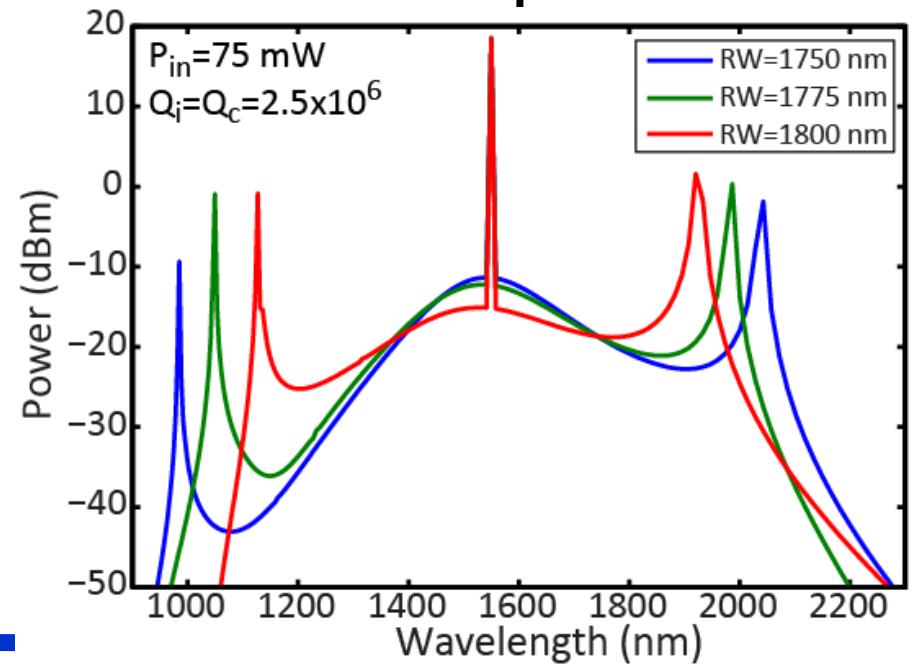


Kartik Srinivasan  
Qing Li  
Daron Westly

Calculated Dispersion

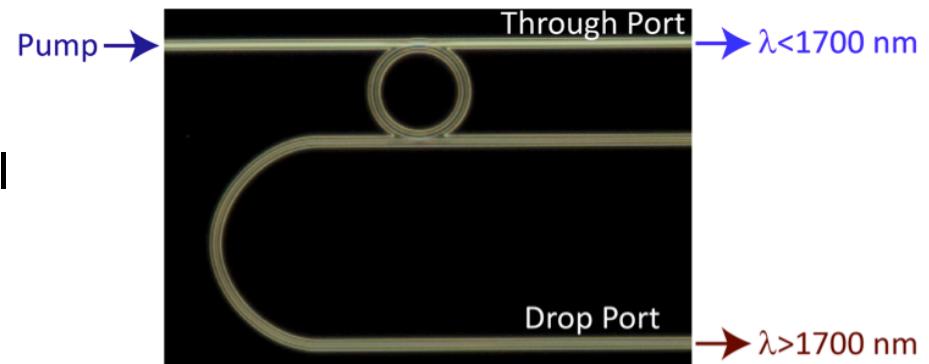


Modeled Spectrum

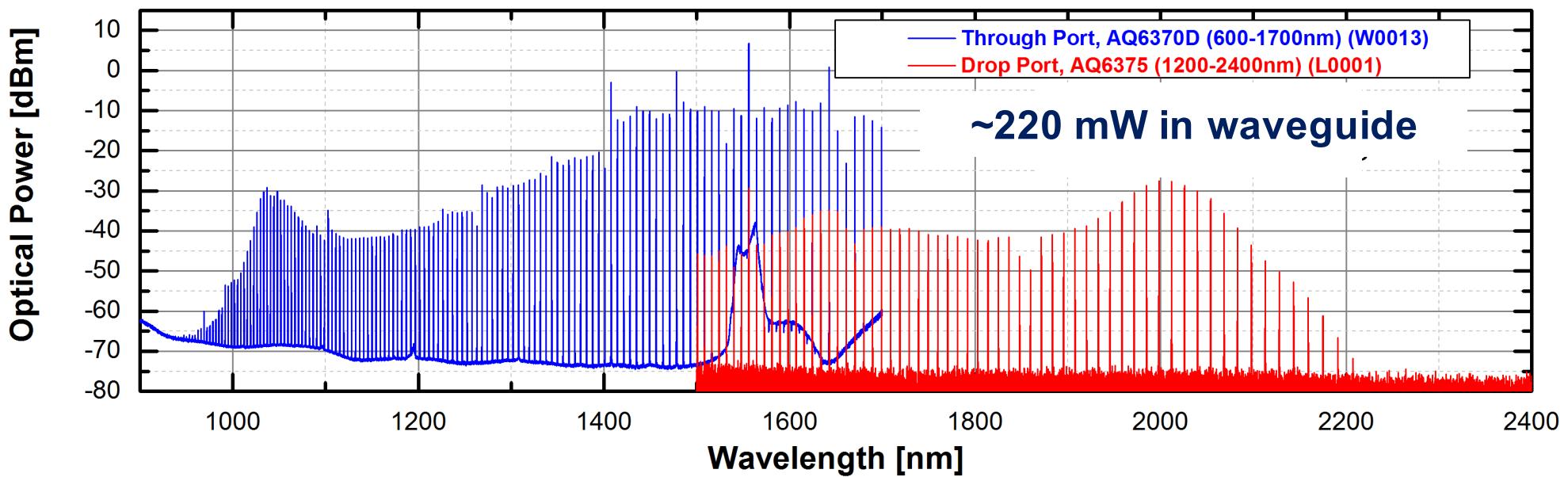


# Octave Span & Dual Dispersive Waves

- dual dispersive waves via dispersion engineering
- “through” and “drop” ports provide optimal out-coupling of 1000 and 2000 nm



Travis Briles

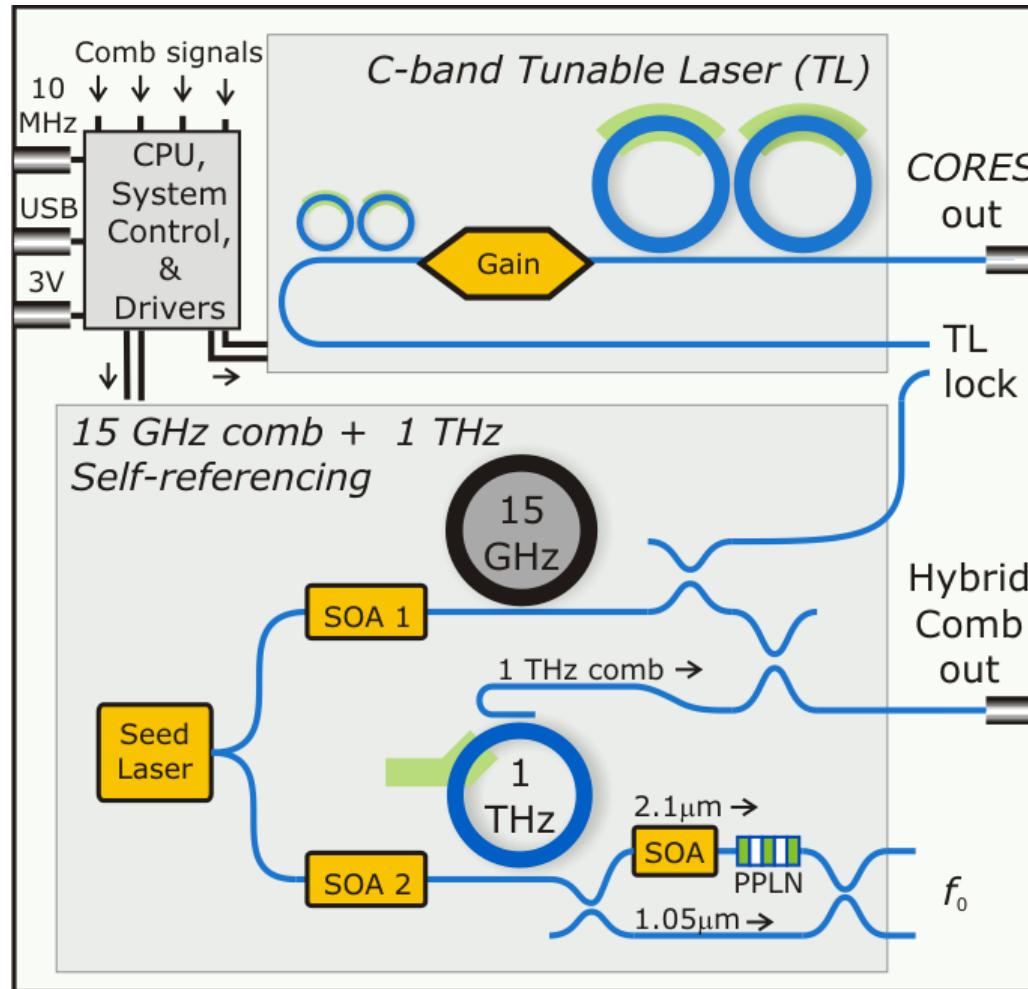


Next Steps:

- Low-noise solitons
- f-2f nonlinear interferometry (fine tune mode frequencies)

# The future: Heterogeneous integration

- Self-referenced comb on a silicon chip
- Included pump and tunable laser output
- Could also include electronic control



# **Outline**

## **1. Optical frequency combs in timekeeping**

- How we got to where we are....

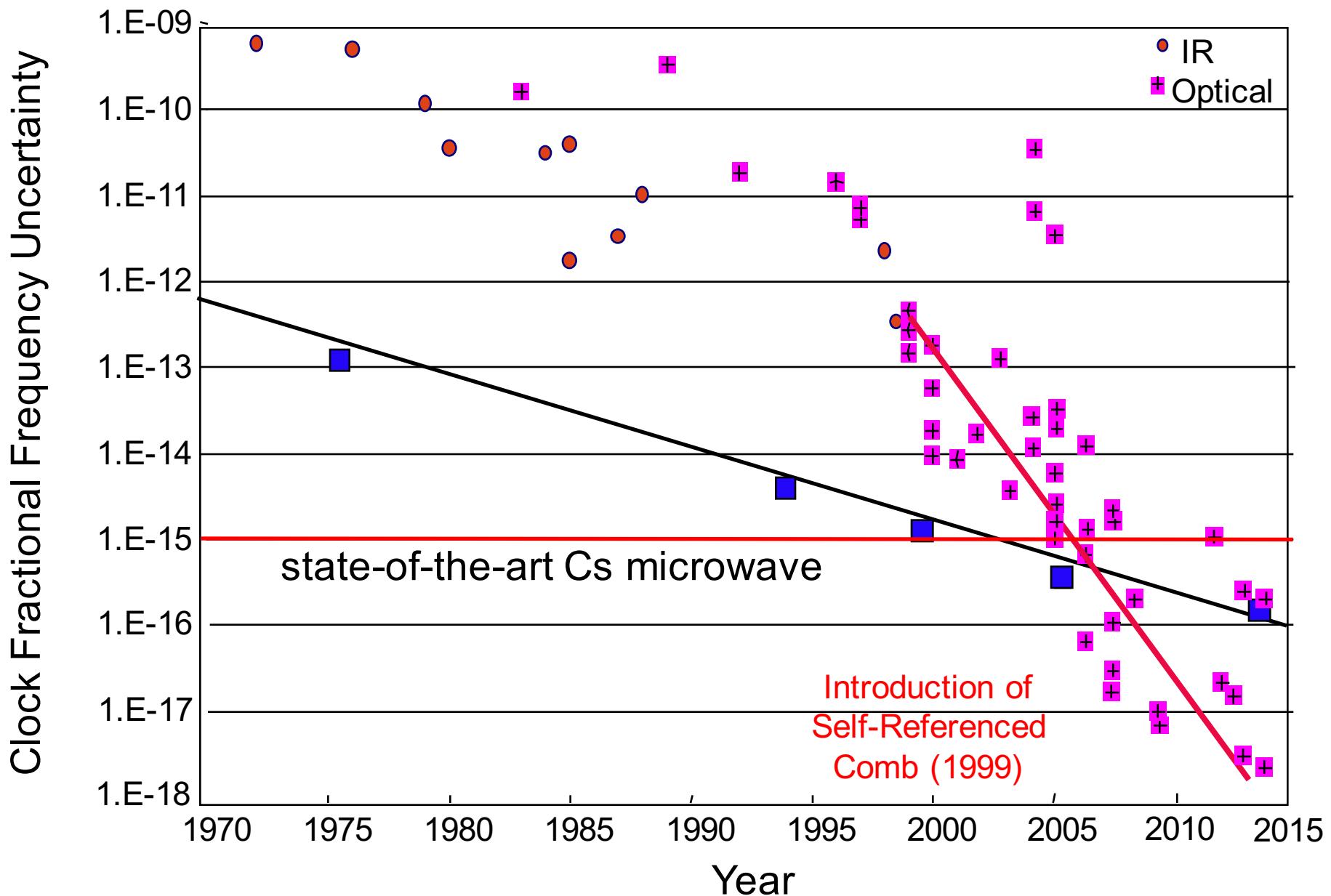
## **2. The multiple faces of an optical frequency comb**

## **3. Classes of frequency combs and their basic operation principles**

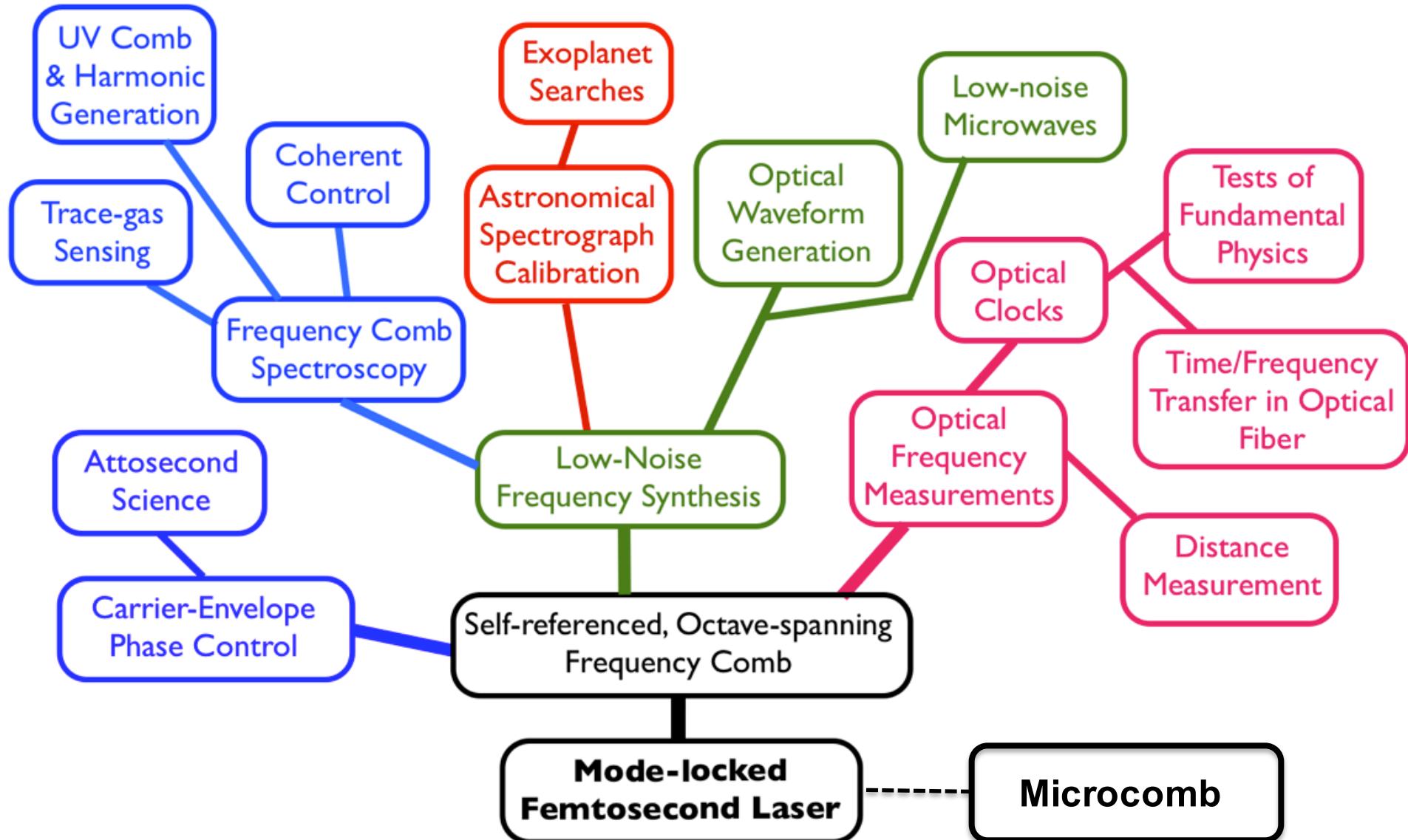
- Mode-locked lasers
- Microcombs
- Electro-optic frequency combs

## **4. Challenges and opportunities for frequency combs**

# Frequency Combs and Clocks



# Broad Range of Applications Beyond Clocks



# Challenges/Opportunities

1. Gaps in our knowledge
  - Microcomb nonlinear optics and operation for full control and optimization of a low-noise, broad bandwidth spectrum
  - Fiber combs employ an “empirical recipe”
2. Technology is complex: Improved robustness, space worthiness....
3. Materials & systems
  - Improved nonlinear optics (integrated fiber and waveguide) more compatible with low power
  - New materials coming online (MIR, QCLs)
  - Best platform/material for different wavelength regions
4. Integration
5. Matching the technology to the application

# Thank you!

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