

Chip-Based Optical Frequency Combs

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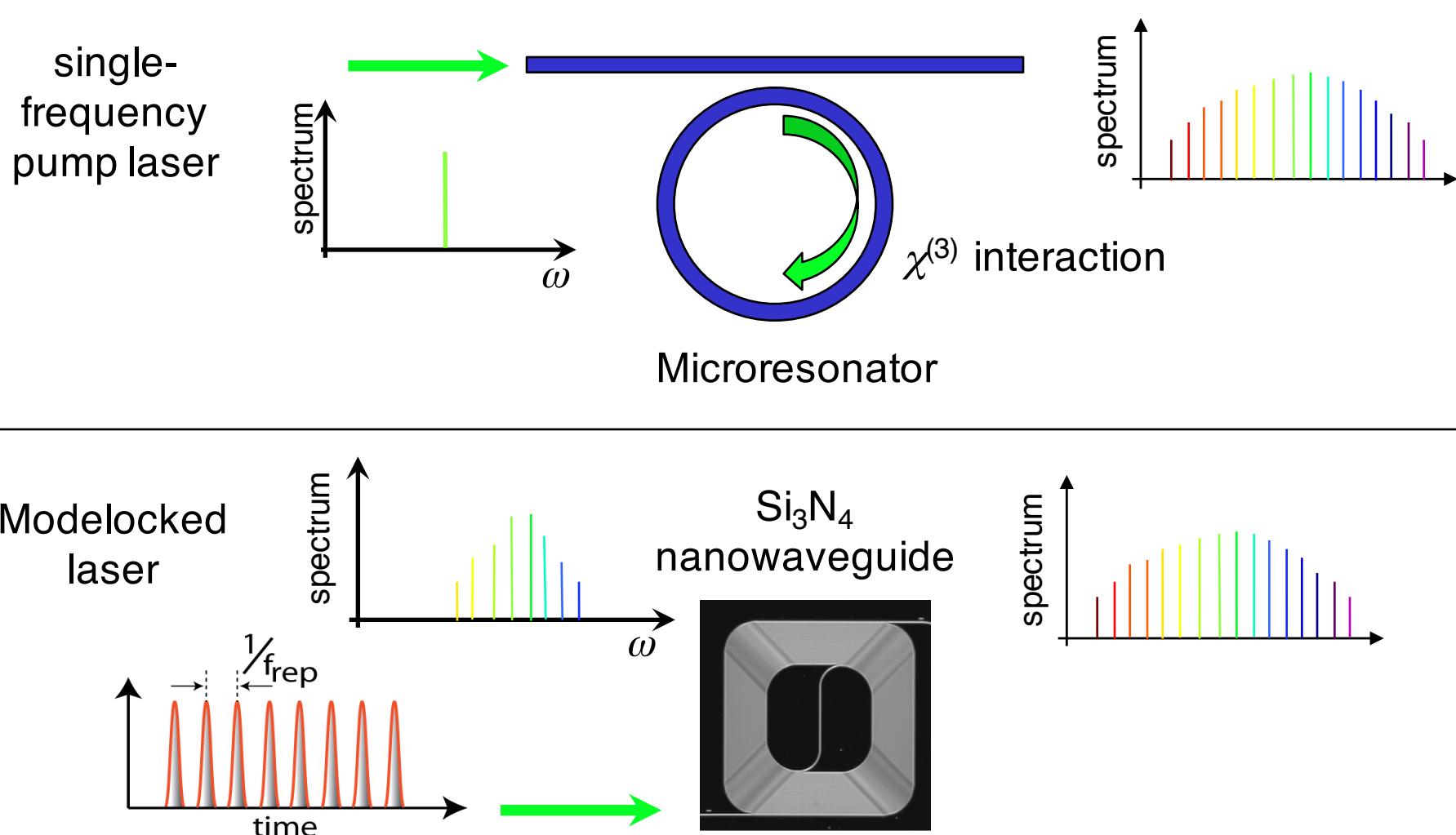
Department of Electrical Engineering



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The Fu Foundation School of Engineering and Applied Science

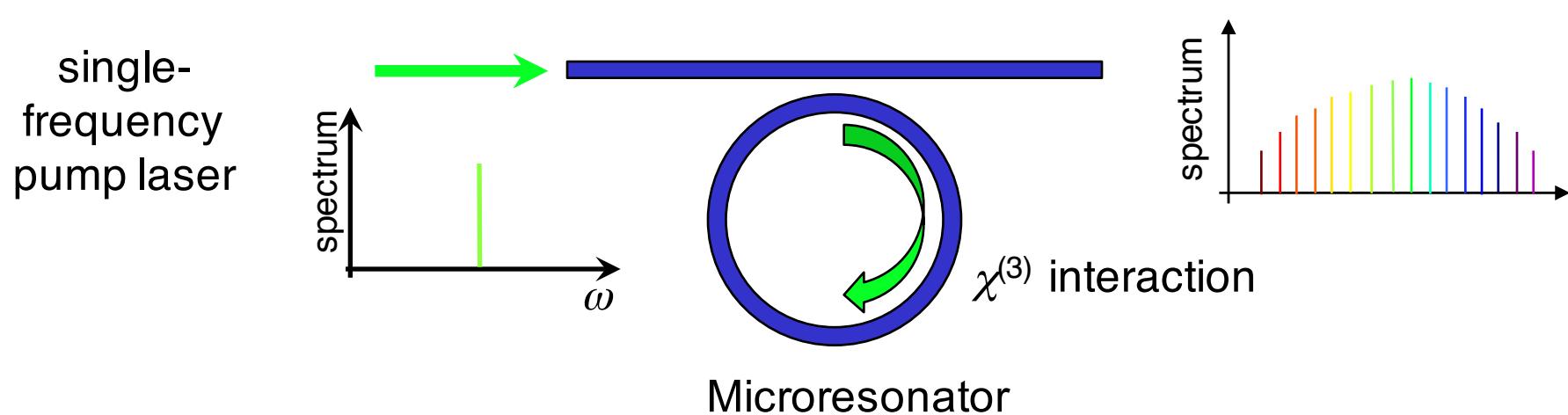
KISS Frequency Comb Workshop
Cal Tech, Nov. 2-5, 2015

Chip-Based Comb Generation



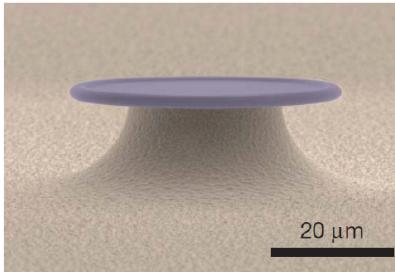
- Origin of combs can be traced to **four-wave mixing (FWM)**
- Requires small anomalous group-velocity dispersion

Chip-Based Comb Generation



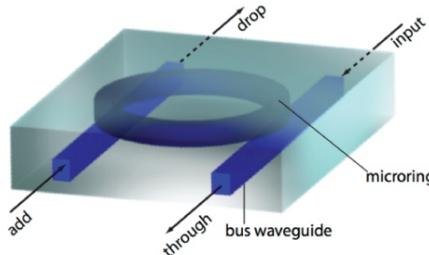
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Microresonator-Based Parametric Combs



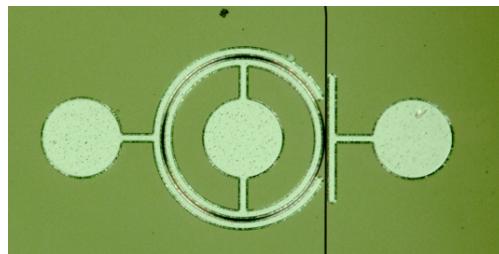
silica μ -toroids

Del' Haye *et al.*, Nature (2007).
Del' Haye *et al.*, PRL (2008).



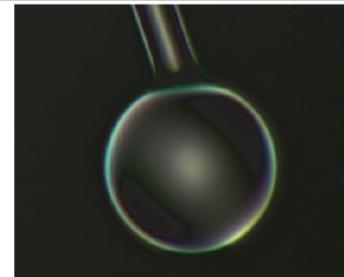
high-index glass μrings

Razzari *et al.*, Nature Photon. (2010).
Pasquazi *et al.*, Opt. Express (2013).



silicon

Griffith *et al.*, (2014).



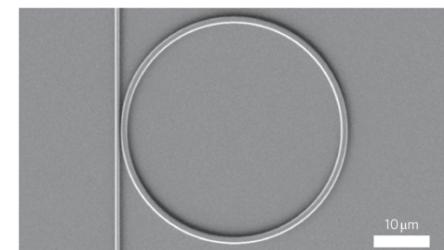
silica μ -spheres

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silica disks & rods

Li *et al.*, PRL (2012)
Papp, *et al.*, PRX (2013)



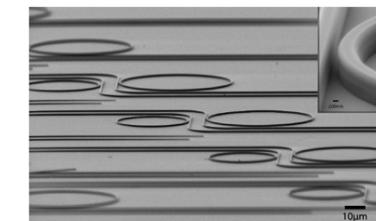
Si nitride

Levy *et al.*, Nat. Photon. (2010).
Ferdous *et al.*, Nat Photon. (2012).
Herr *et al.*, Nat. Photon. (2012).



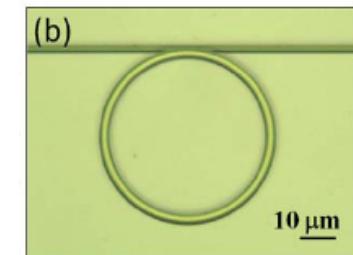
CaF₂, MgF₂, & quartz

Savchenkov *et al.*, PRL (2008).
Liang *et al.*, Opt. Lett. (2011).
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diamond

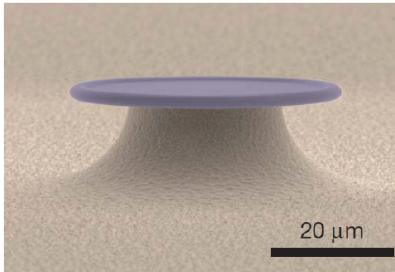
Hausmann *et al.*, Nat. Photon. (2013).



Al nitride

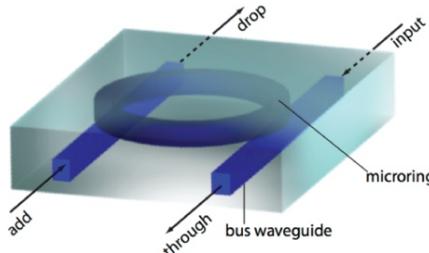
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Microresonator-Based Parametric Combs



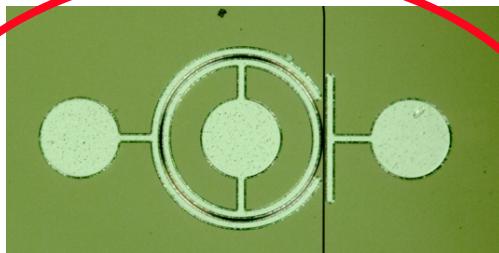
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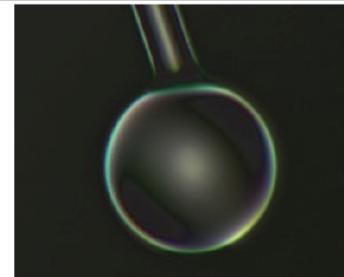
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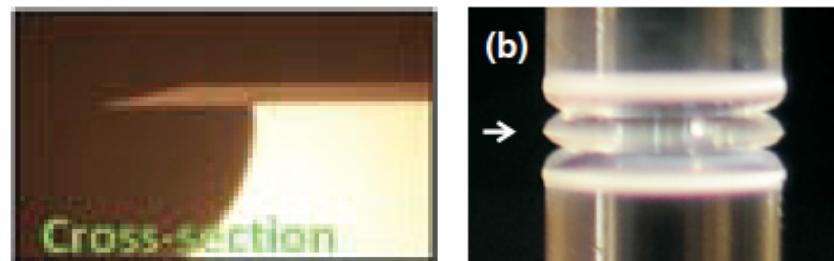
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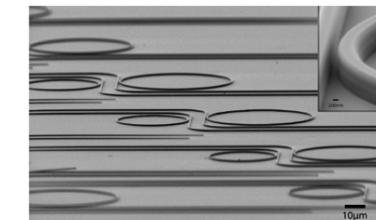
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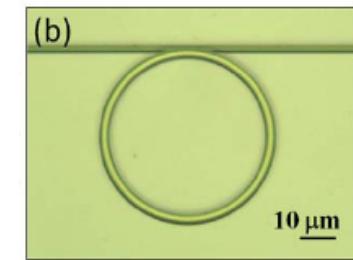
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diamond

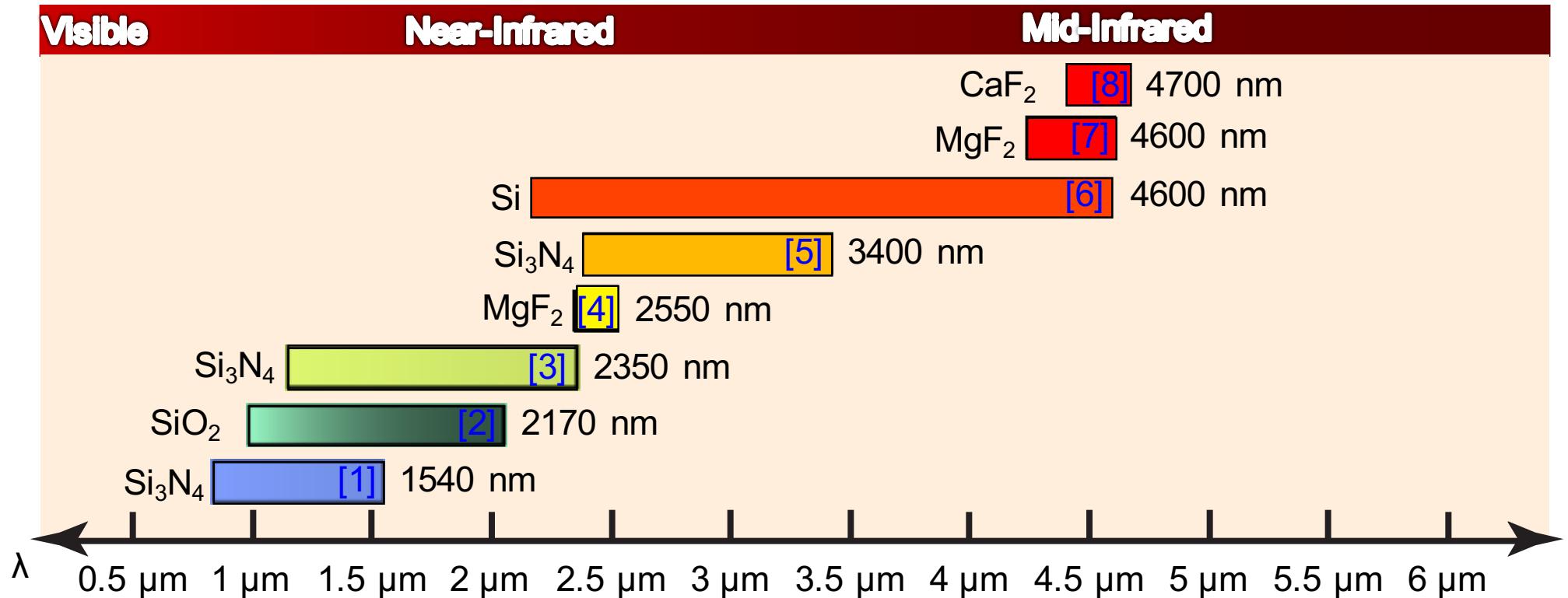
Hausmann *et al.*, Nat. Photon. (2013).



Al nitride

Jung *et al.*, Opt. Lett. (2013).

Microresonator Comb Spectral Coverage



[1] Saha, et al., Lipson & Gaeta (2013); Luke, et al., Gaeta & Lipson, in preparation (2015).

[2] Del'Haye, et al., and Kippenberg, Phys. Rev. Lett. (2011).

[3] Okawachi, et al., Lipson & Gaeta, Opt. Lett. (2011); Okawachi, et al., Lipson & Gaeta, Opt. Lett. (2013).

[4] Wang, et al., and Kippenberg, Nature Comm (2012).

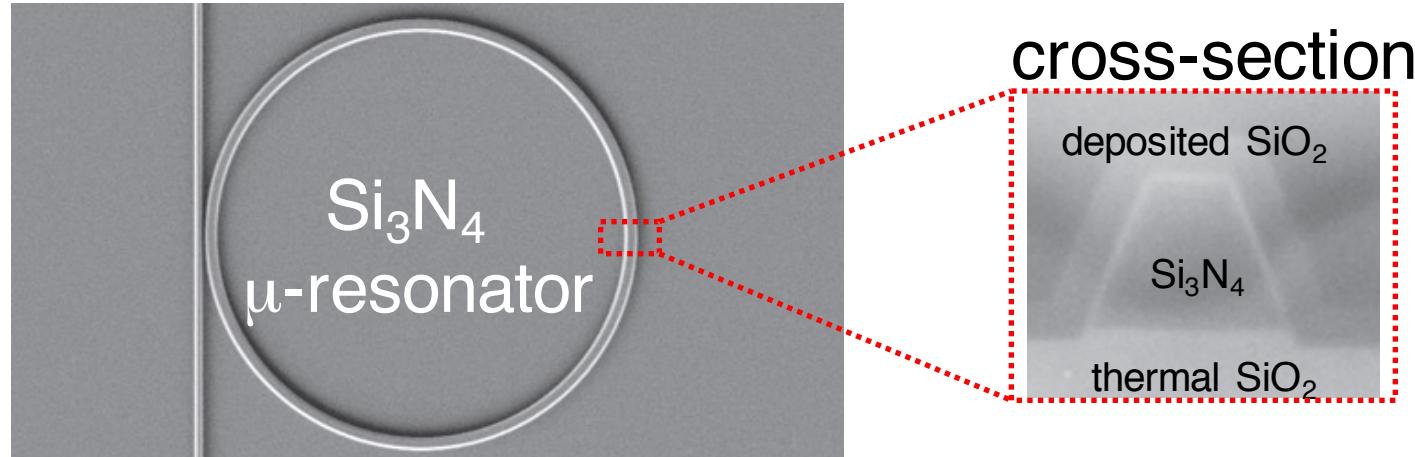
[5] Griffiths, et al., Gaeta & Lipson, Nat. Comm. (2015).

[6] Luke, et al., Gaeta and Lipson, in preparation (2015).

[7] Lecaplain, et al., Kippenberg, arXiv (2015).

[8] Savchenko, et al., Maleki, arXiv (2015).

Silicon-Based Microresonators for Parametric Comb Generation



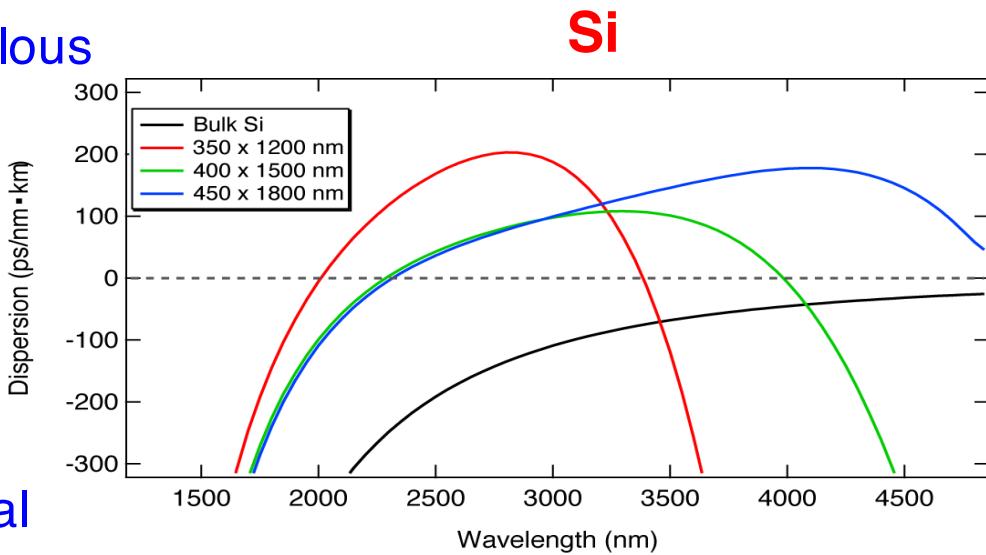
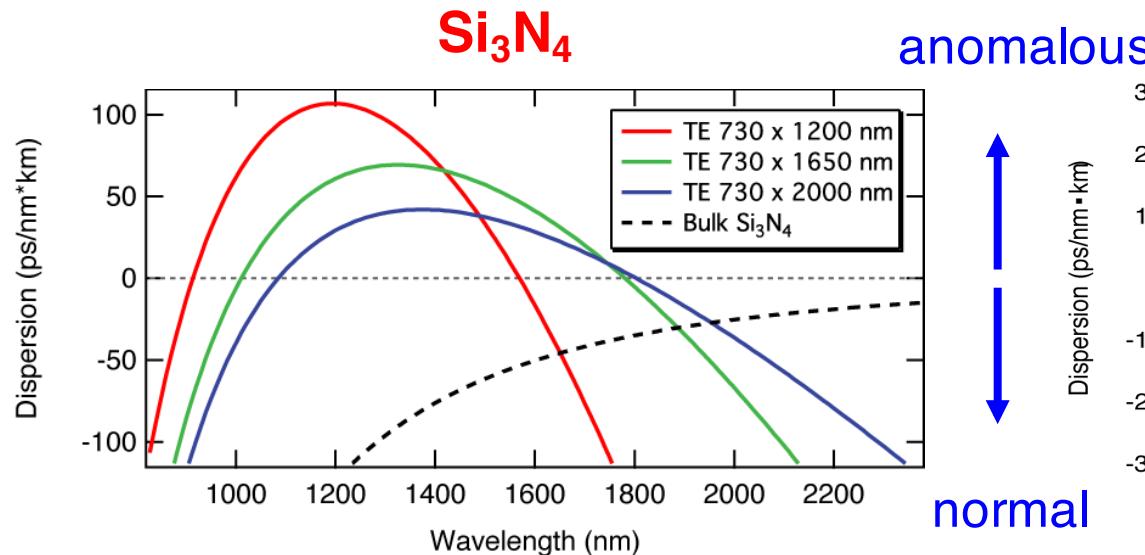
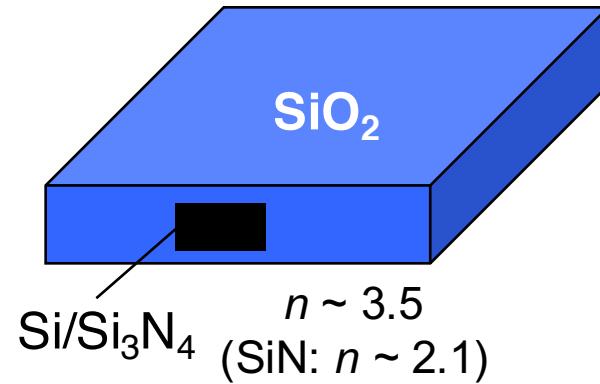
- CMOS-compatible material
- Fully monolithic and sealed structures and couplers
- High- Q resonators → Si_3N_4 $Q = 7 \times 10^6$ [Luke, et al., *Opt. Express* (2013).]

$$\text{Si} \quad Q \sim 10^6 \text{ [Lee, et al., (2013).]}$$

- High nonlinearity → $n_2 \sim 10\text{-}100 \times$ silica
- Waveguide dispersion can be engineered
 [Foster, et al., Lipson, Gaeta, *Nature* **441**, 960 (2006).
 Turner-Foster, et al., Gaeta, Lipson, *Opt. Express* **18**, 1904 (2010).]]

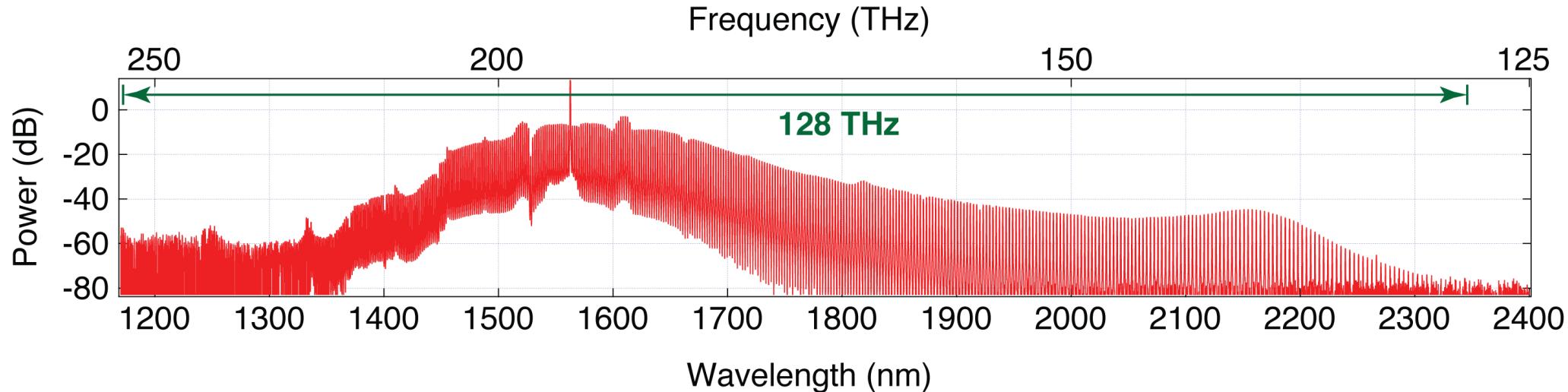
Tailoring of GVD in Si-Based Waveguides

- GVD can be tuned by varying waveguide shape and size.
- Same chip can operate w/ different pump wavelengths.



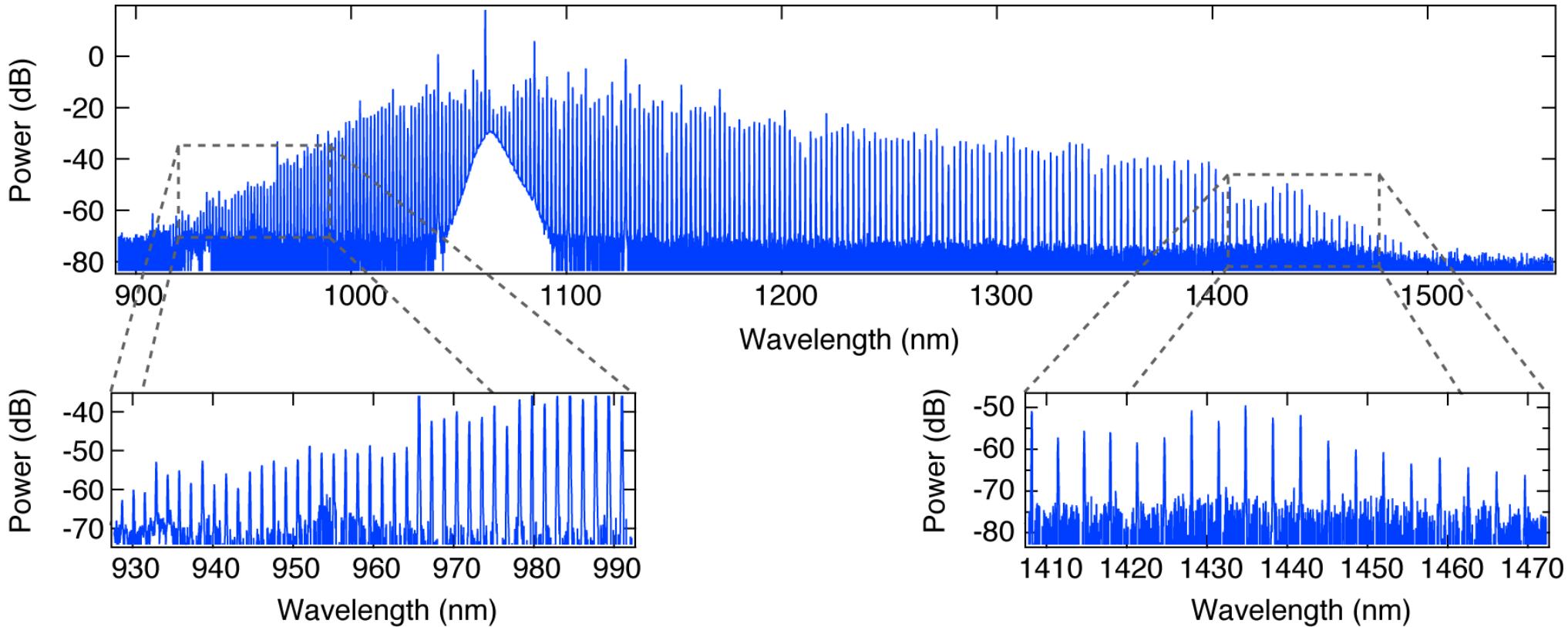
- Oxide cladding limits generation $< 5 \mu\text{m}$ (?)

Octave-Spanning Comb in Si_3N_4



- > 150 THz bandwidth
- Stable, robust, highly compact comb source for clock applications
- Modest power requirements (100's of mW)

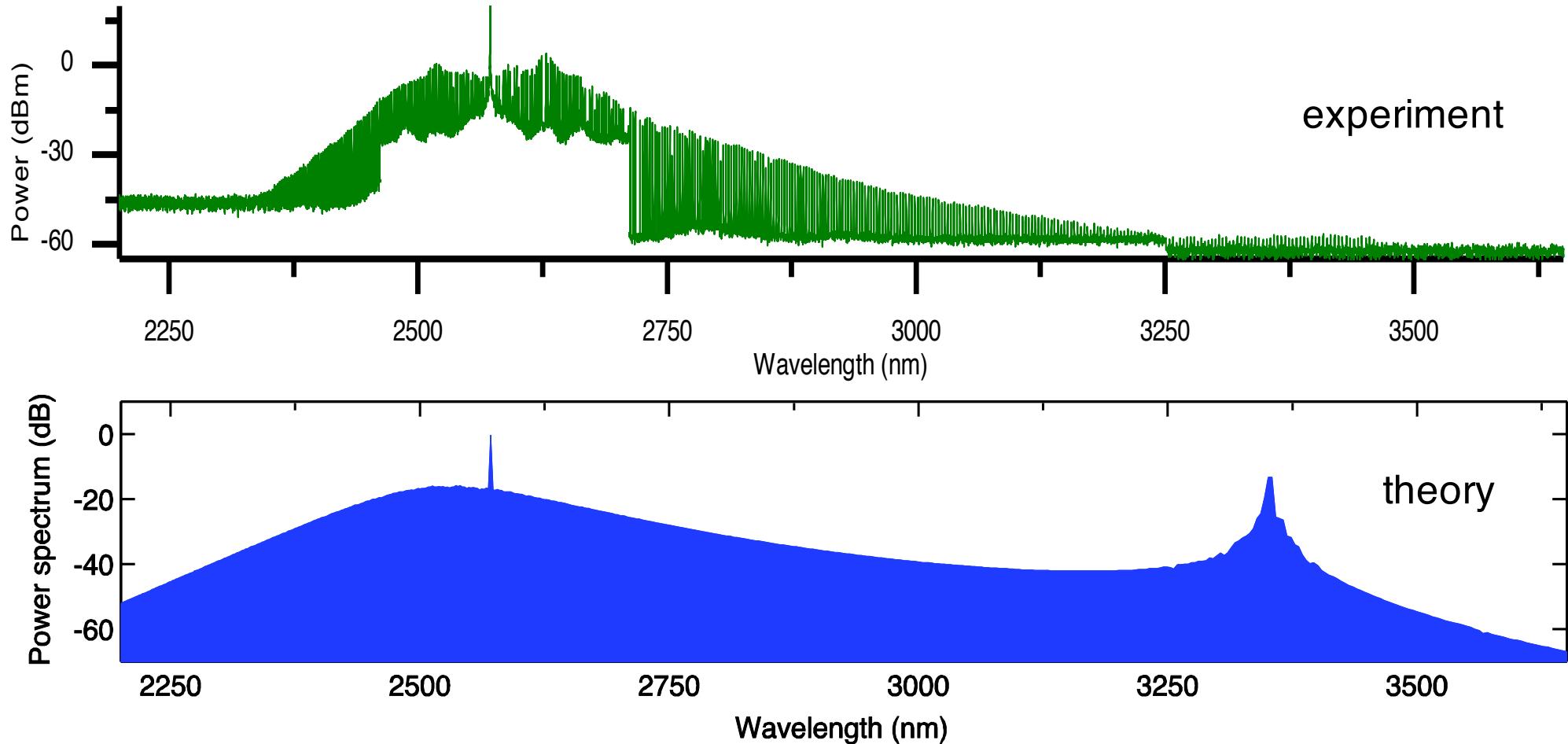
Dispersion Engineering: Broadband Combs with 1- μm Pump in Si_3N_4



- 690 x 1400 nm cross section, 46- μm resonator radius (500 GHz FSR)
- >2/3 octave of continuous comb bandwidth

Saha, et al., Lipson, and Gaeta, Opt. Express (2012)
 Luke et al. Lipson, Gaeta, to be published (2014).

Mid-IR Comb in Si_3N_4



- 950 x 2700 nm waveguide
- Fully filled in comb spanning 2.3 - 3.4 μm
- $P_{th} \sim 80$ mW, FSR = 99 GHz

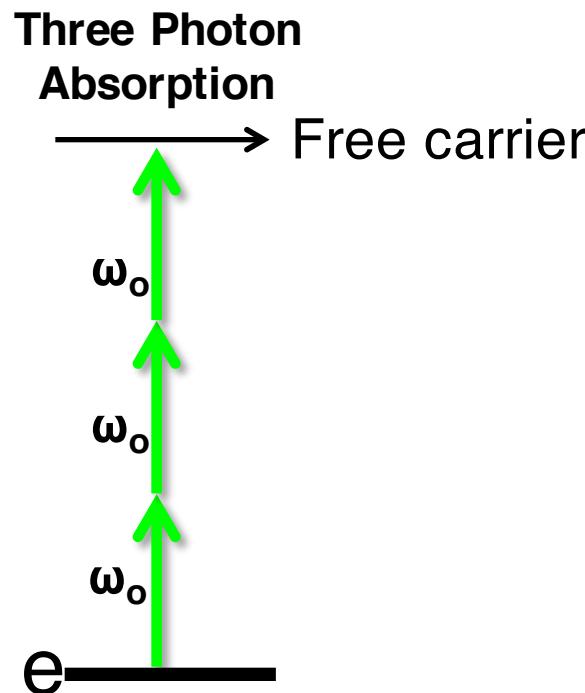
Silicon as a Mid-IR Material

Advantages:

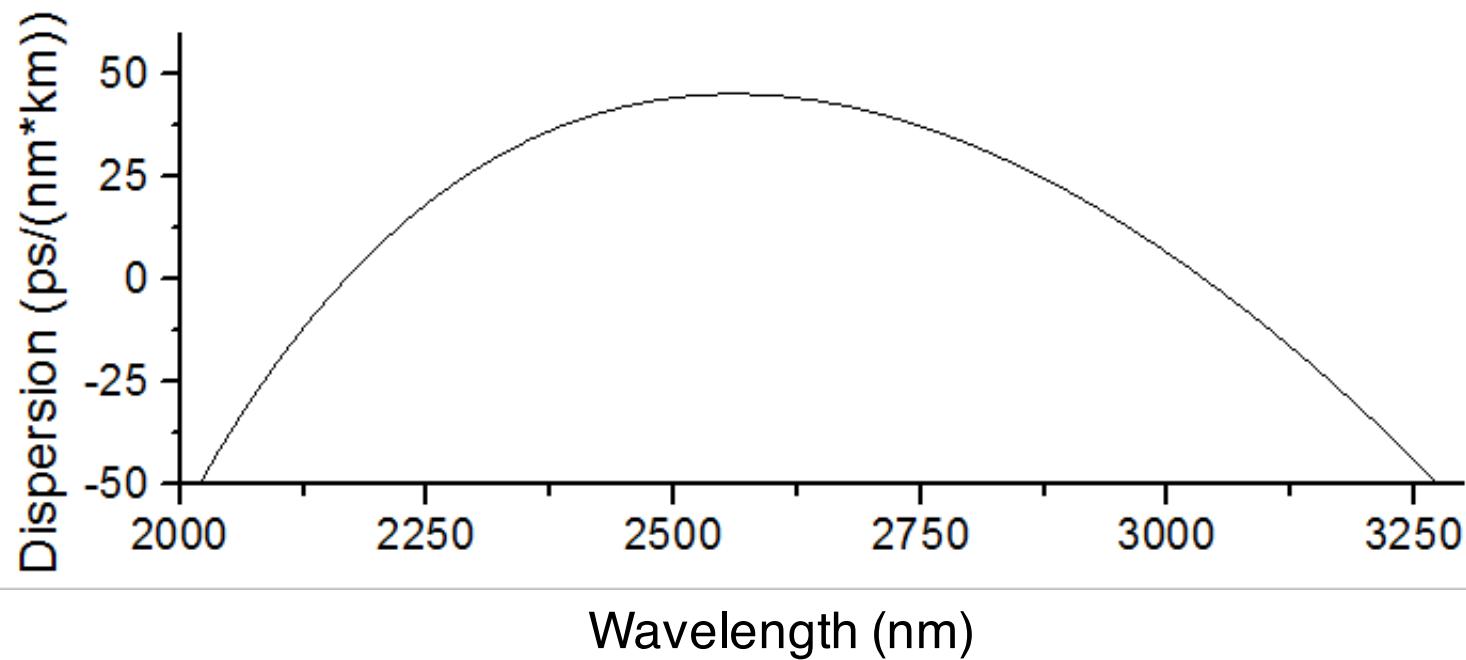
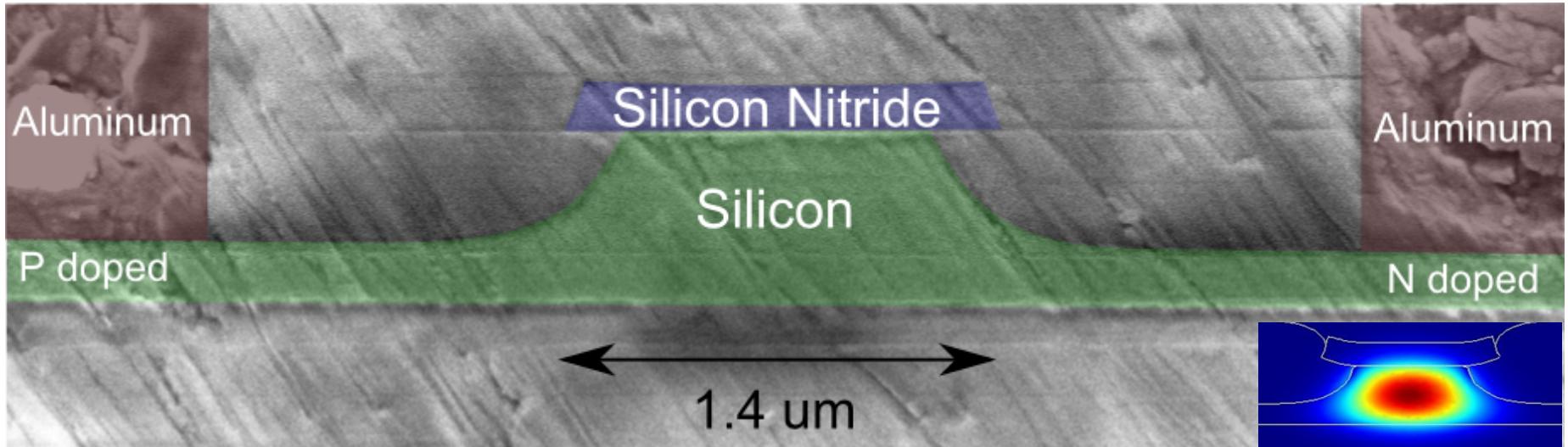
- Large 3rd order nonlinearity
- Transparent to $\sim 8 \text{ } \mu\text{m}$
- High refractive index

Problem:

- Need to pump $> 2 \text{ } \mu\text{m}$
- Three-photon absorption
- Significant above 1 Watt circulating power

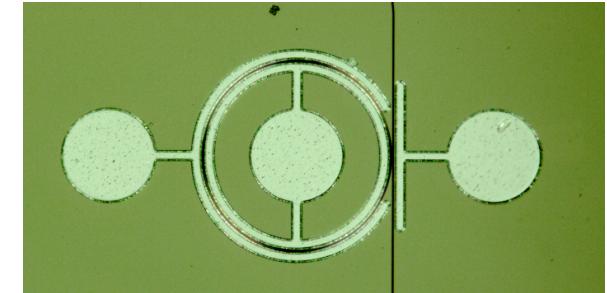


Fabricated Silicon Device

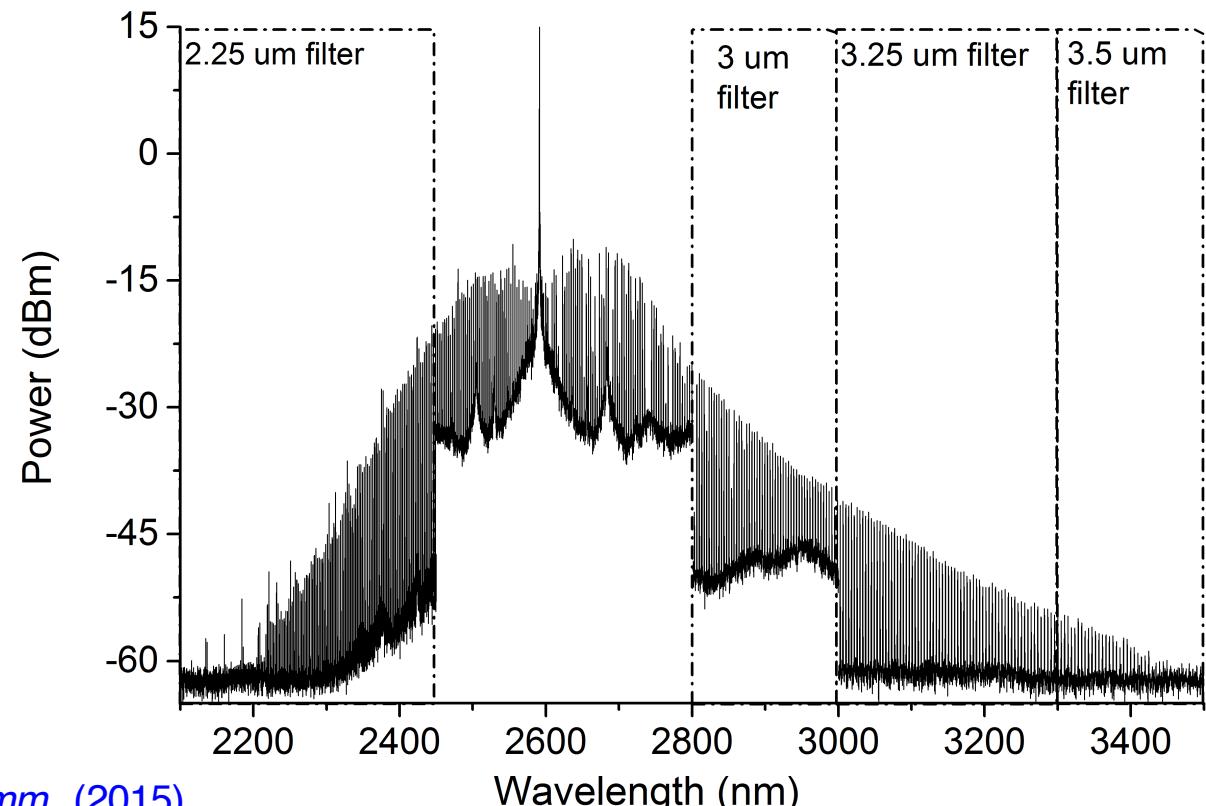


Mid-IR Parametric Frequency Comb

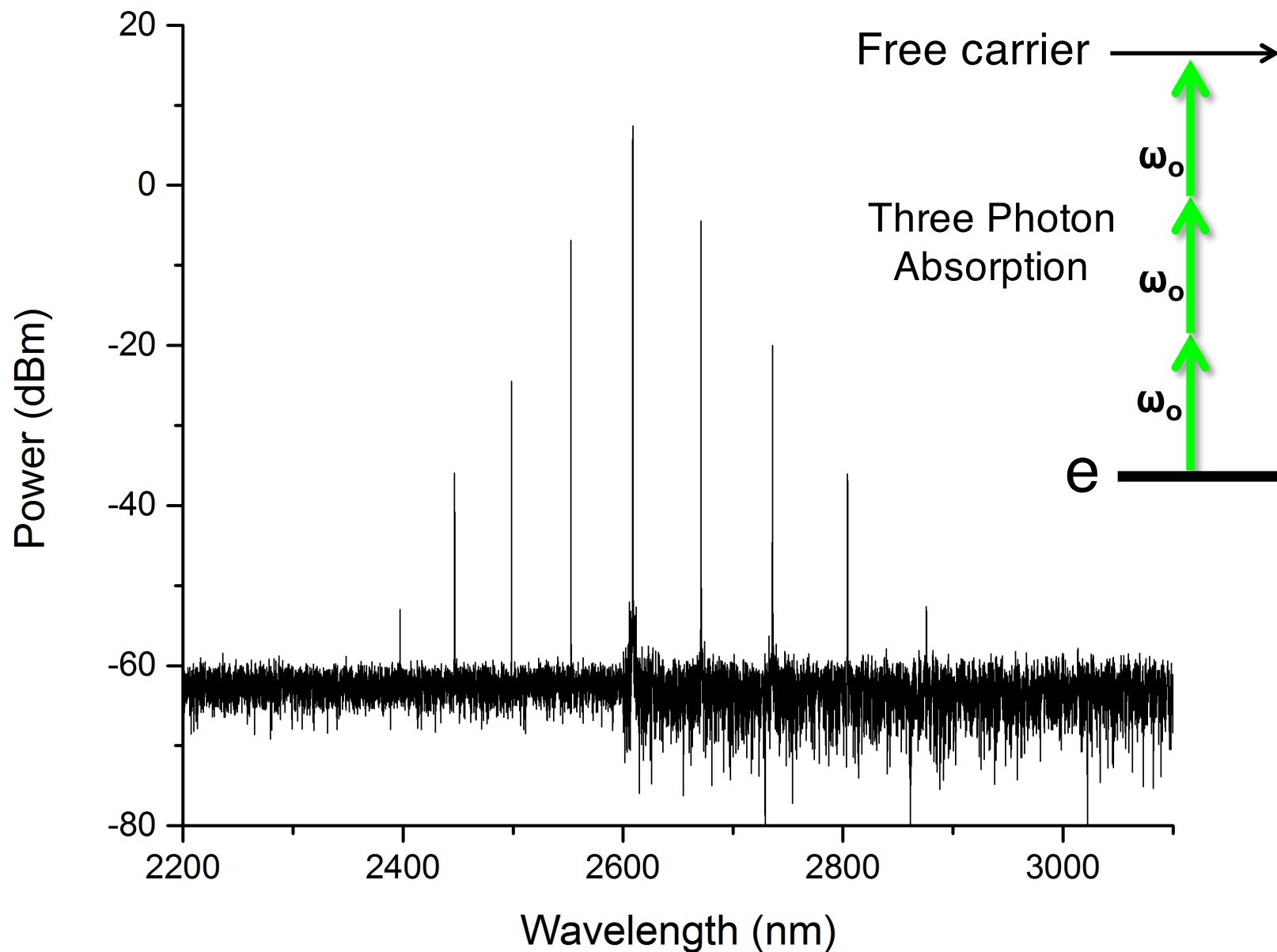
- **500×1400 nm etchless silicon microresonator with *p-i-n* structure**
- Q-factor $\sim 10^6$
- Measurement with FTIR OSA
→ Bandwidth limited by dynamic range of OSA



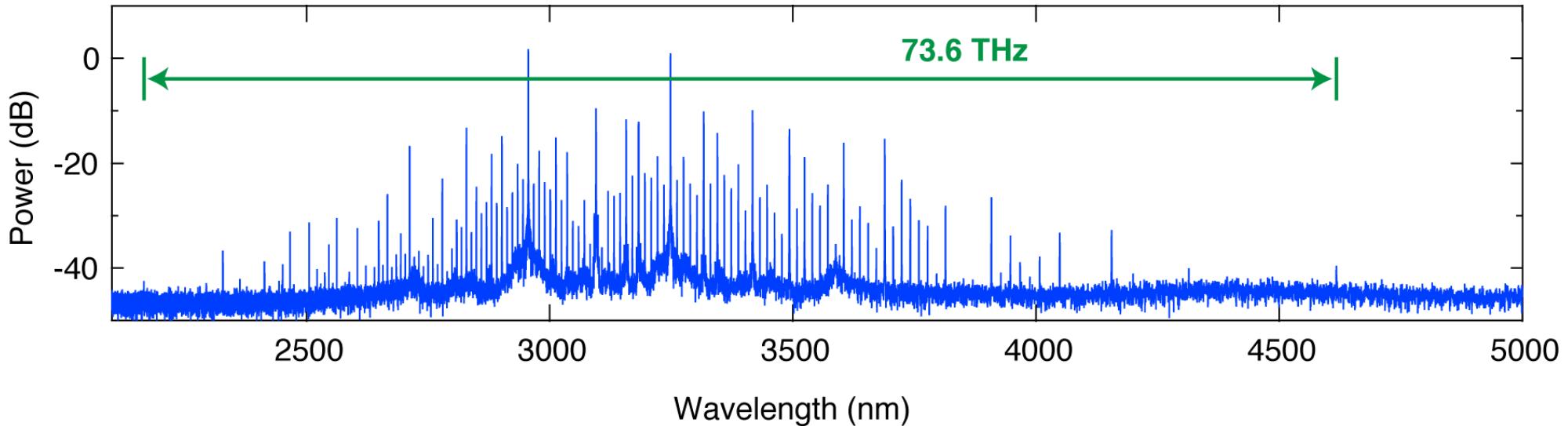
- 2608-nm pump
- 750-nm bandwidth
- 125-GHz FSR
($100 \mu\text{m}$ radius)



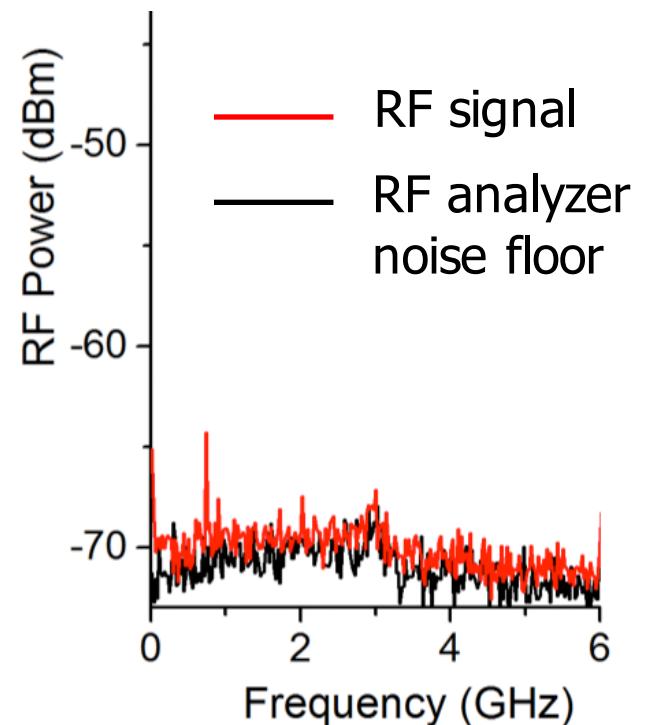
Comb Generation without Carrier Extraction



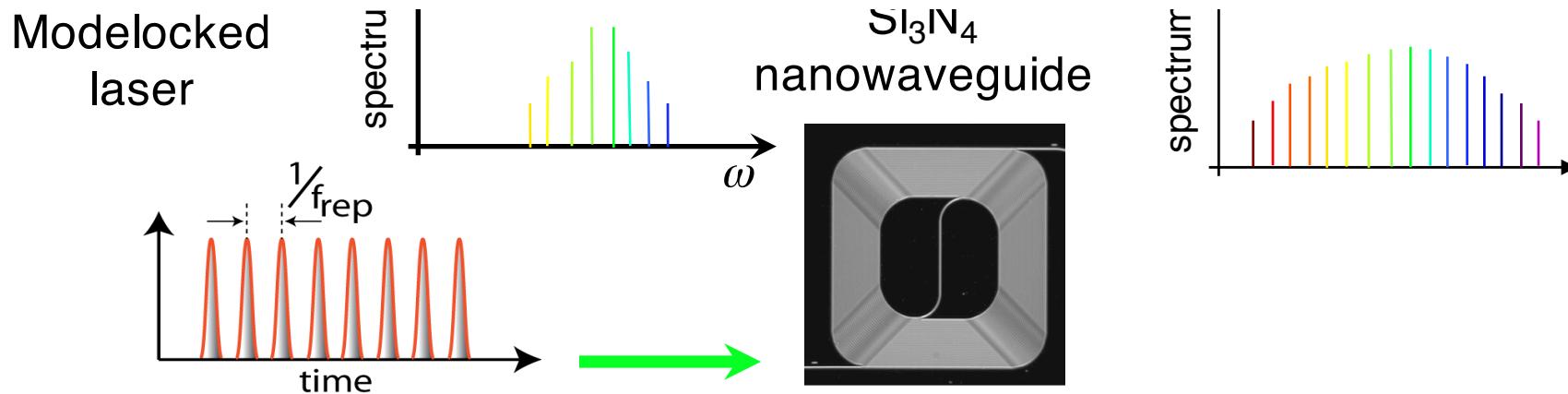
Near Octave-Spanning Mid-IR Comb Generation in Si Microresonator



- Pump wavelength 3095 nm
- Comb spans > octave
- Wavelength range: 2165 – 4617 nm
- Comb exhibits low RF noise



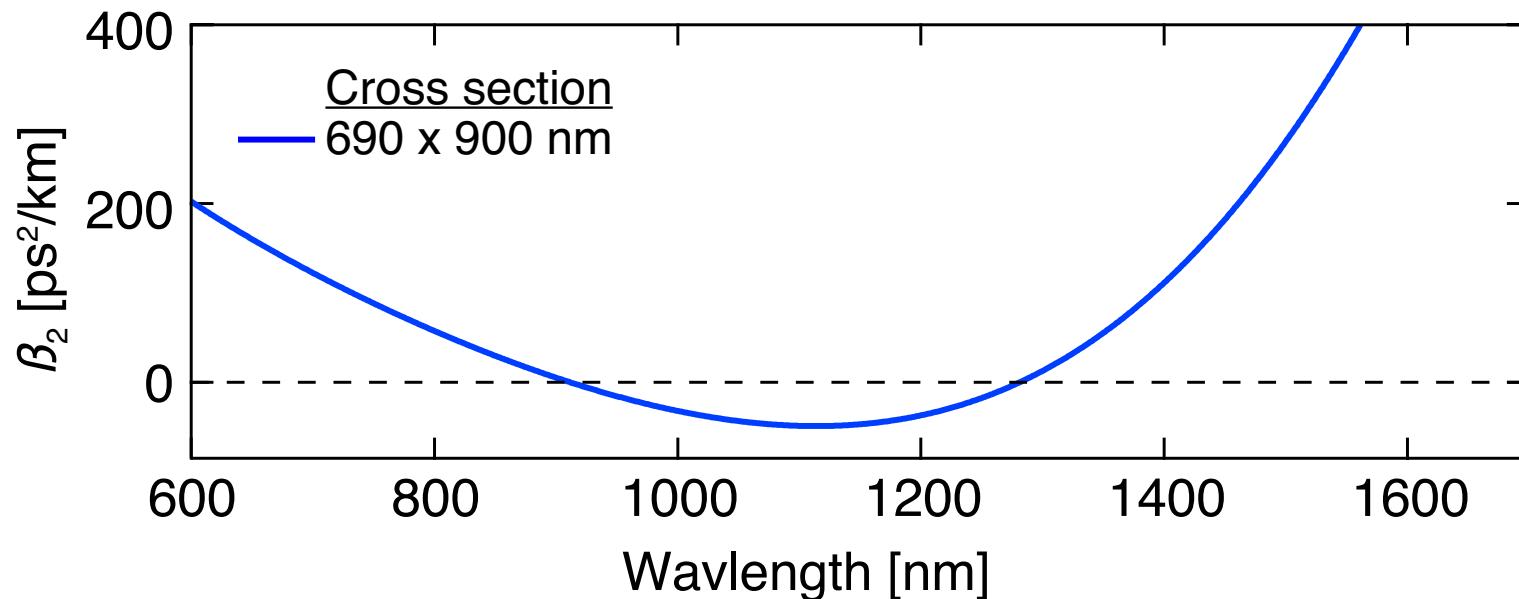
Chip-Based Comb Generation



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- Requires small anomalous group-velocity dispersion

Waveguide Design for Octave-Spanning Coherent SCG at 1 μm

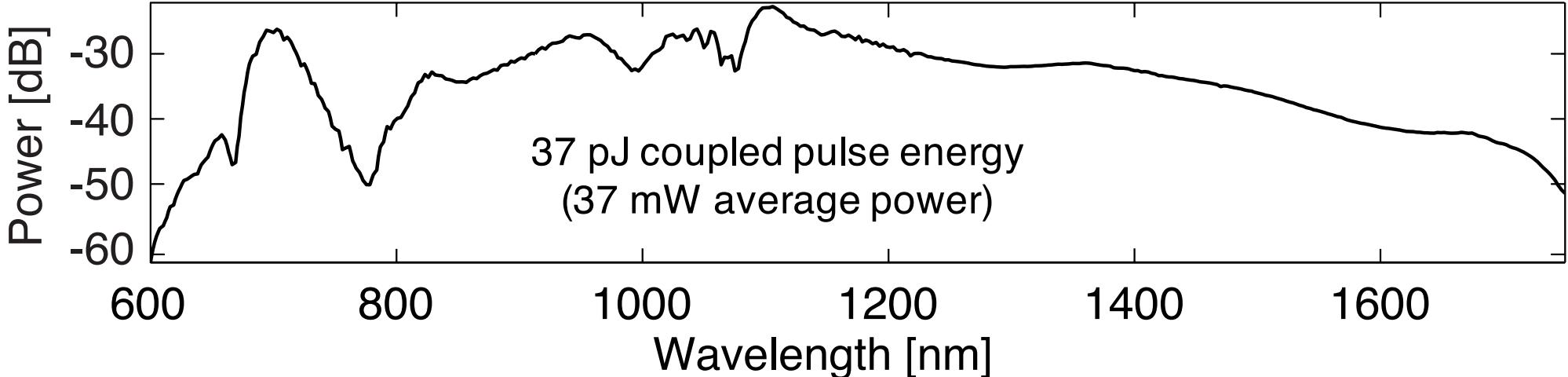
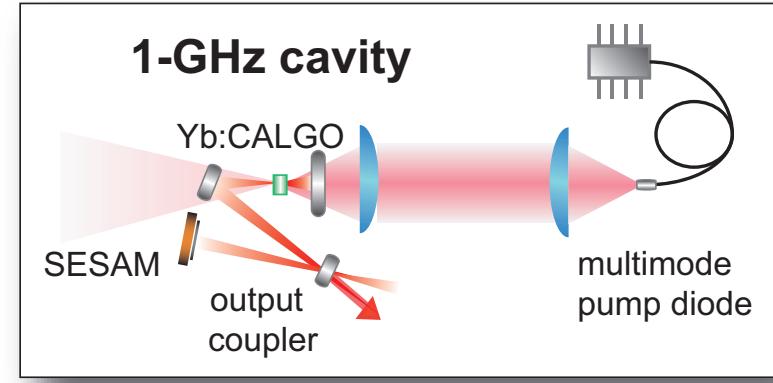
- Engineer dispersion by tailoring waveguide cross section
- Design broad region of anomalous group velocity dispersion (β_2) around 1- μm pump
- Coherent SCG with 100-fs pump through self-phase modulation and dispersive wave emission

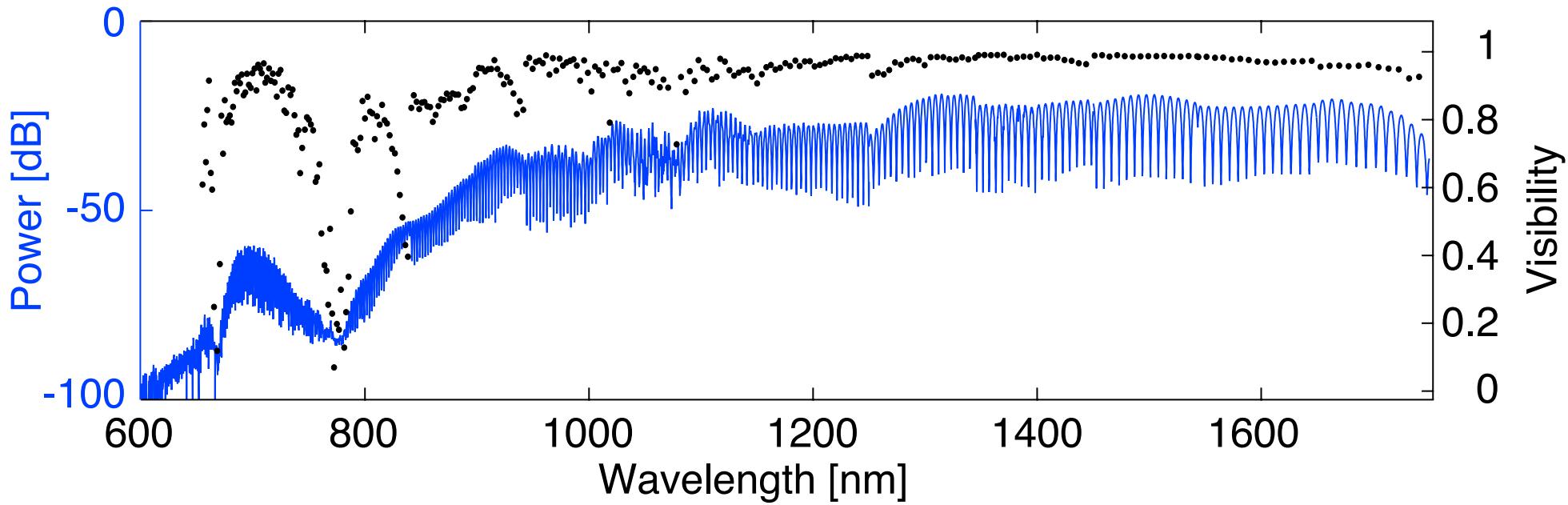


Supercontinuum Generation with Diode-Pumped Solid-State Laser

Collaboration w/ Ursula Keller's group (ETH-Zurich)

- Pump with 1-GHz repetition rate
SESAM-modelocked diode-pumped
Yb:CALGO laser [Klenner *et al.*, Opt. Express
(2014)]
- 92-fs input pulses, 1055 nm center
wavelength





- OSA sweep records ensemble average
- Coherence $|g_{12}^{(1)}|$ related to visibility $V(\lambda)$

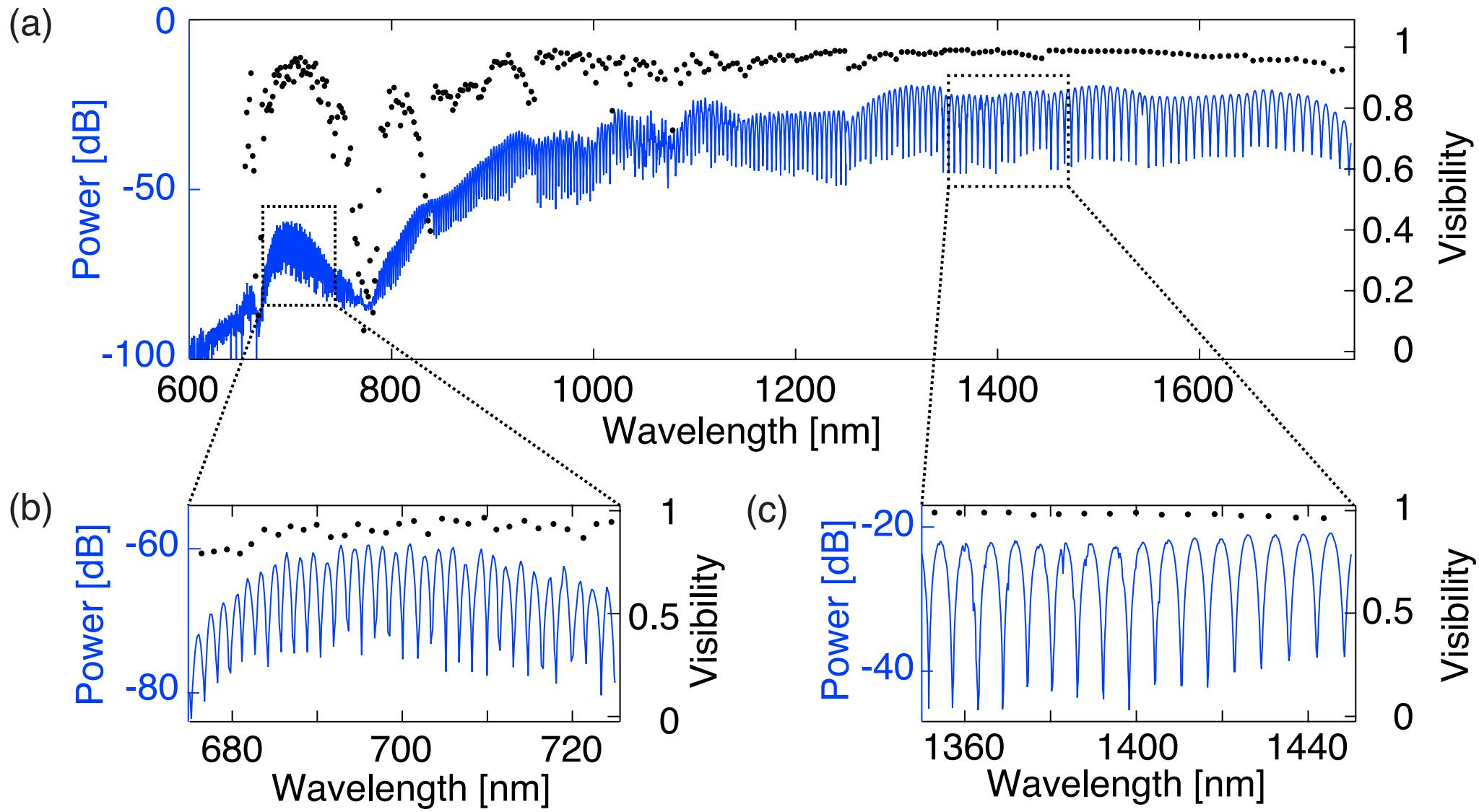
[Nicholson and Yan, Opt. Express (2004); Gu *et al.*, Opt. Express (2011)]

$$V(\lambda) = \frac{I_{\max}(\lambda) - I_{\min}(\lambda)}{I_{\max}(\lambda) + I_{\min}(\lambda)}$$

$$V(\lambda) = \frac{2|g_{12}^{(1)}| \left[I_1(\lambda) I_2(\lambda) \right]^{1/2}}{\left[I_1(\lambda) + I_2(\lambda) \right]}$$

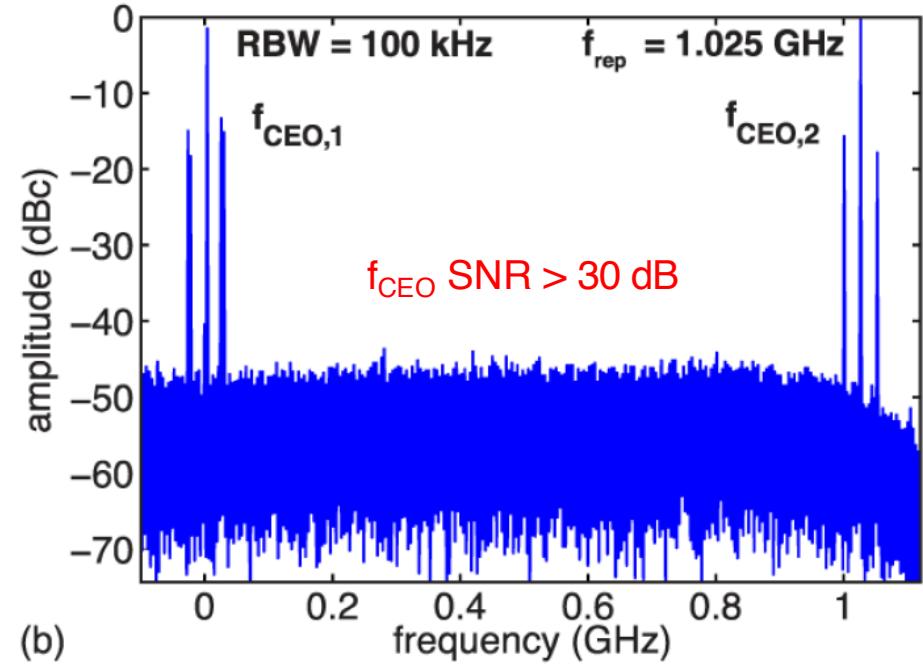
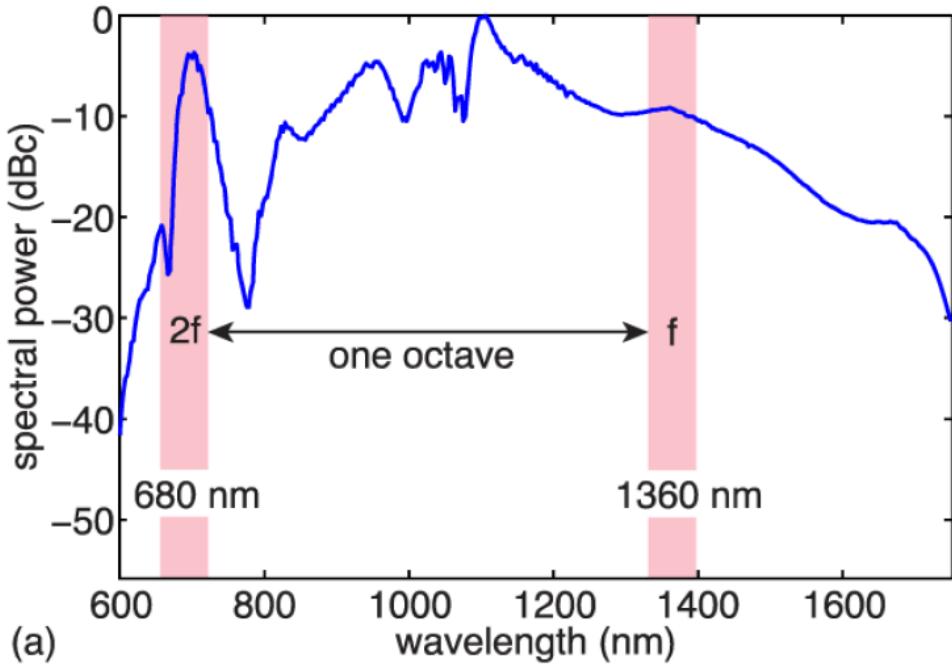
- Perform coherence measurement in 100-nm increments

Coherent Supercontinuum for f-to-2f Interferometry



Carrier Envelope Offset Frequency Detection Using Silicon Nitride Waveguide

- Carrier envelop offset frequency (f_{ceo}) beatnote from f -to- $2f$ interferometry
- Spectrum at 1360 nm is frequency doubled and overlapped with spectrum at 680 nm
- f_{ceo} signal-to-noise ratio > 30 dB
- Much lower noise level (10 dB) than w/ PCF

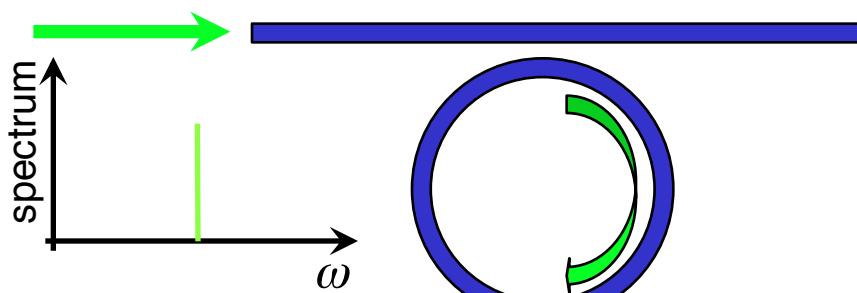


[Mayer *et al.*, Opt. Express (2015)]

Comparison of Comb Generation Schemes

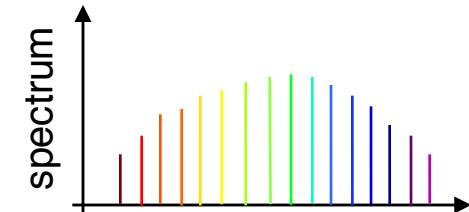
Pump Properties

- single-frequency
- $P > 200$ mW
- CEO control
- Tuning for modelocking (?)



Microresonator Properties

- Thermal issues important
- Comb spacing control (thermal)
- Modelocking (Thermal?)

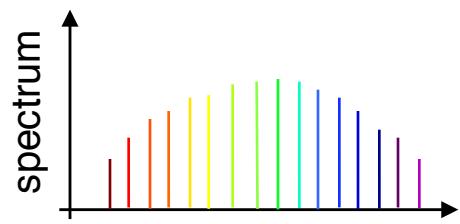
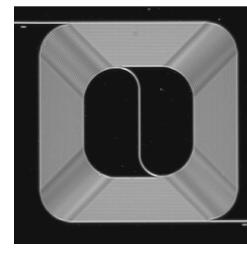
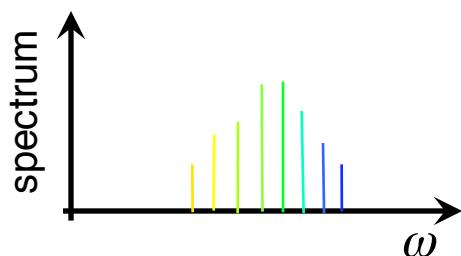


Comb Properties

- Spacing > 20 GHz
- > 200 $\mu\text{W}/\text{line}$
- Stabilized $\sim 2/3$ Octave
- Near-IR – mid-IR

Pump Properties

- Modelocked
- < 200 fs for coherent comb
- CEO & comb spacing control
- $P \sim 40$ mW



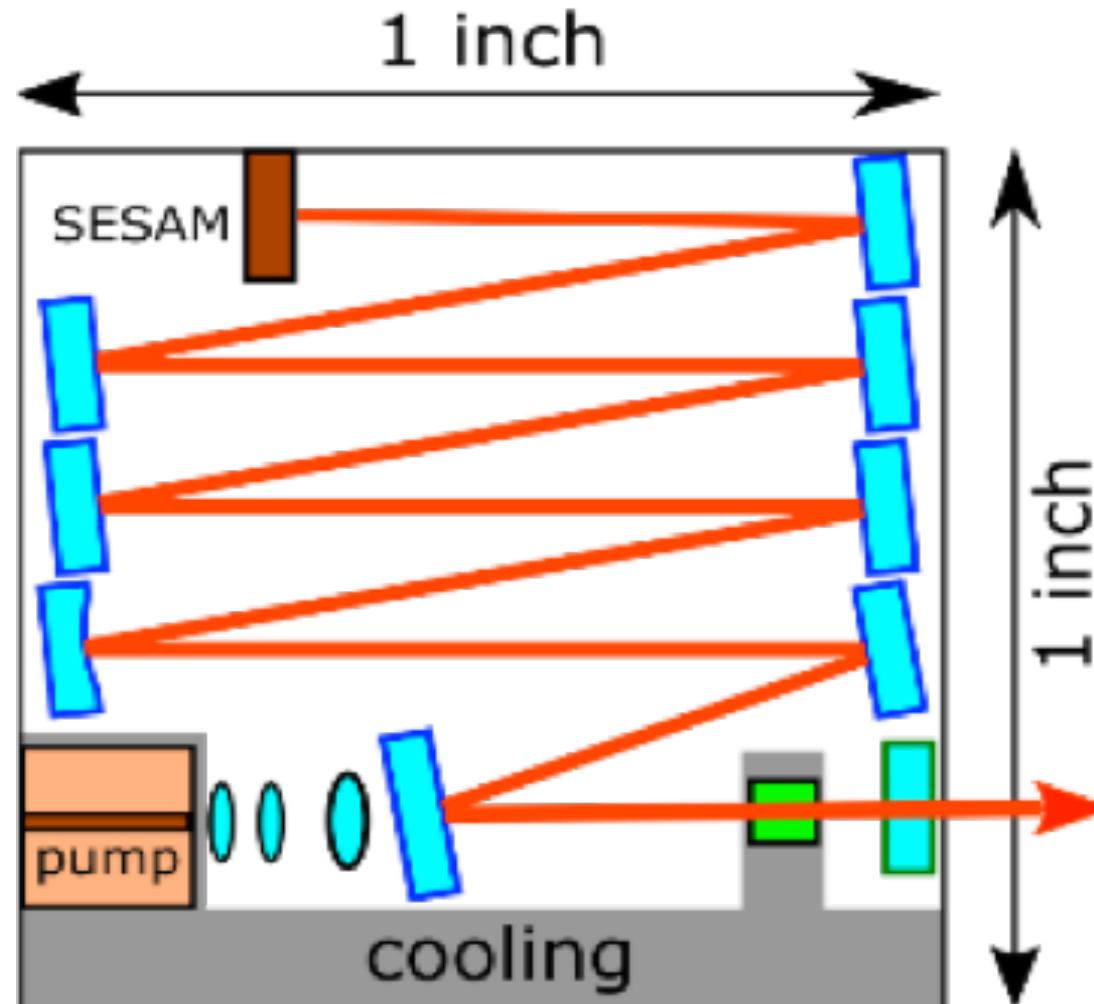
Nanowaveguide Properties

- Passive
- Waveguide dispersion tailored longitudinally

Comb Properties

- Spacing > 20 GHz
- > 100 nW/line
- Stabilized > Octave
- Visible – mid-IR

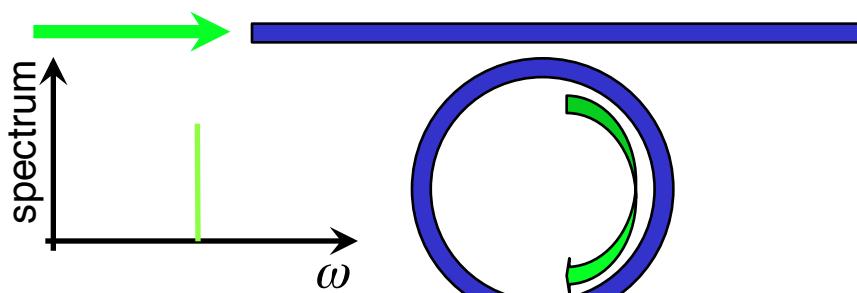
Compact Solid-State 5-GHz Modelocked Laser



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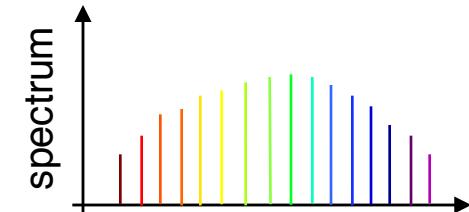
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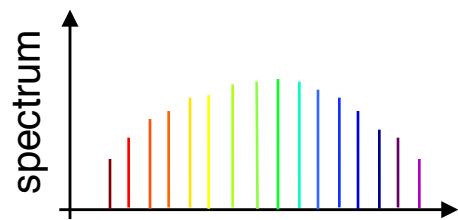
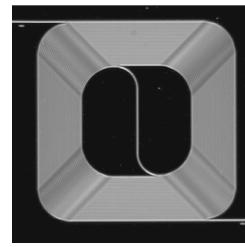
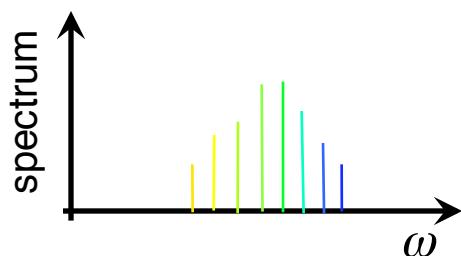


Comb Properties

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- 1 - 200 μW line
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Nanowaveguide Properties

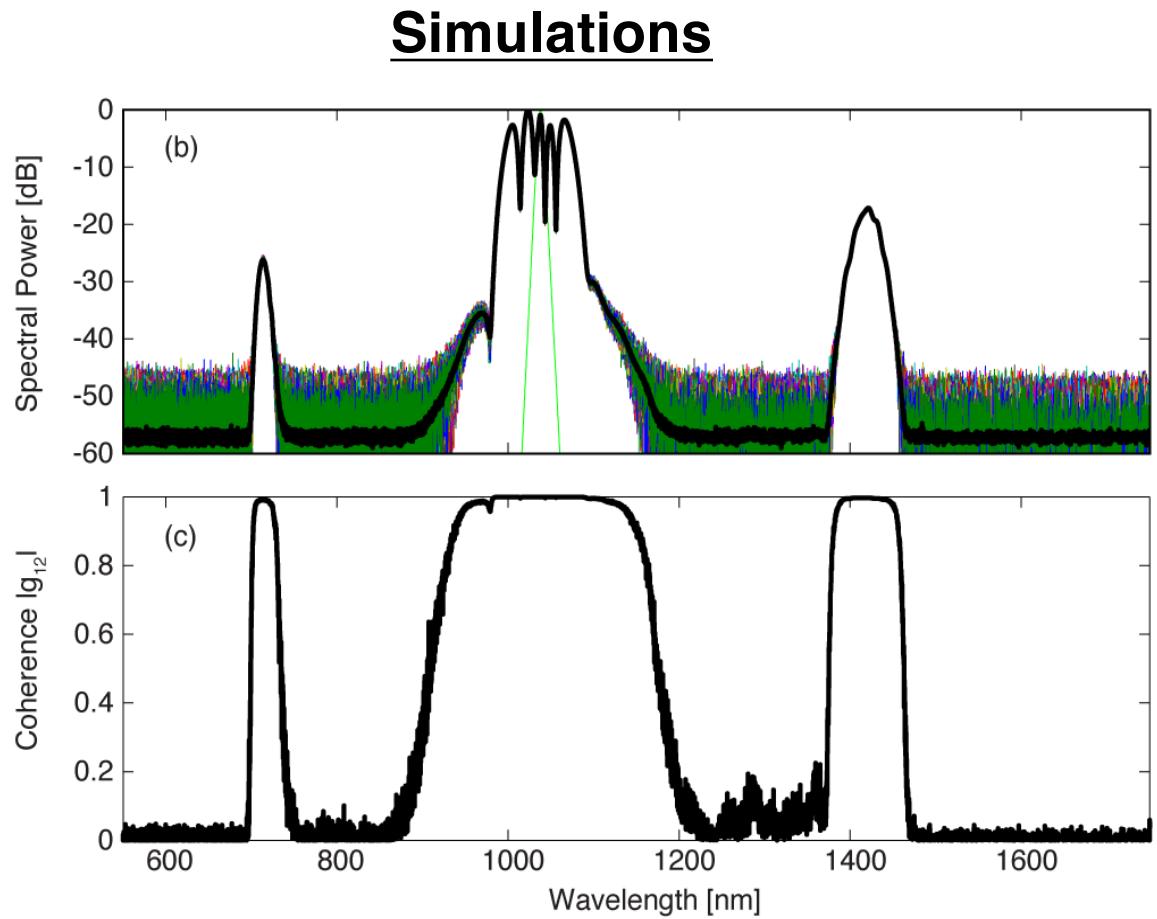
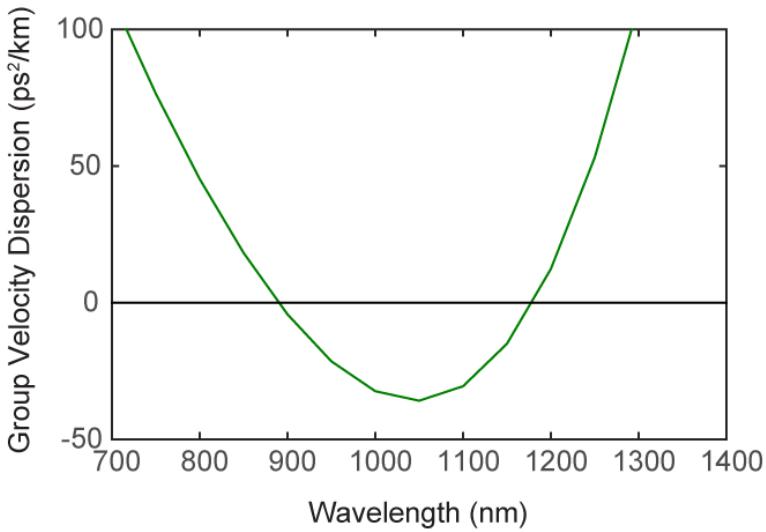
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- Stabilized > Octave
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Spectrally Efficient Octave-Spanning Spectrum

- For applications (e.g., frequency synthesizer) that are particularly power sensitive.

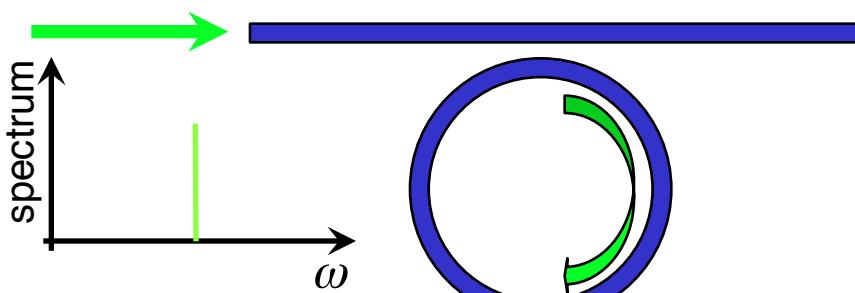


[Okawachi *et al.* Lipson & Gaeta (2015)]

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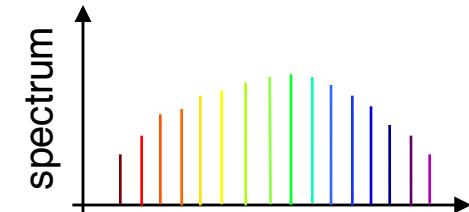
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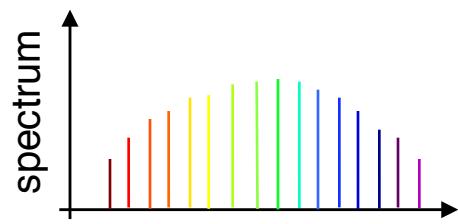
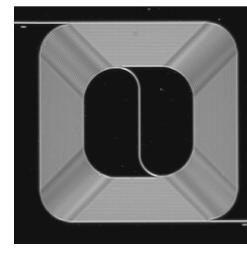
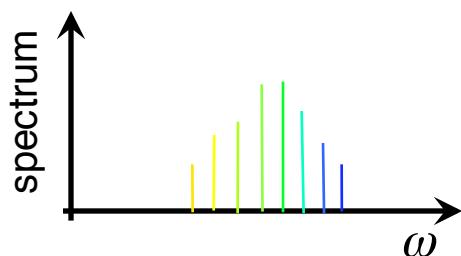


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- Stabilized $\sim 2/3$ Octave
- Near-IR – mid-IR

Pump Properties

- Modelocked
- < 200 fs for coherent comb
- CEO & comb spacing control
- $P \sim 40$ mW



Nanowaveguide Properties

- Passive
- Waveguide dispersion tailored longitudinally

Comb Properties

- Spacing > 20 GHz
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