Direct Multipixel Imaging and Spectroscopy of an Exoplanet with a Mission to the Focus of the Solar Gravitational Lens

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## BREAKTHROUGH

INITIATIVES

## A nice family portrait...

"The Earth is the cradle of bumanity, but mankind cannot stay in the cradle forever." Konstantin Tsiolkovsky







 THE CHART OF COSMIC EXPLORATION

## Our Stellar Neighborhood within 100 ly



The size does matter...

...and so does the distance: the tyranny of the diffraction limit...

## Our Challenge

## THE SOLAR GRAVITATIONAL LENS <br> Largest telescopes to date...



European Extremely Large Telescope 39 meters, Cbile (est. 2022)


The largest telescopes for the last 125 years to date, both on the ground and in space

## THE SOLAR GRAVITATIONAL LENS <br> Largest telescopes in space

Telescope sizes compared
Webb will be the largest astronomical telescope ever put into space. Spitzer, the current infrared telescope, is tiny


## THE SOLAR GRAVITATIONAL LENS <br> 1-pixel direct image of an exo-Earth...

The tyranny of the diffraction limit: To make a 1-pixel image of an exo-Earth at 100 light years, a telescope with a diameter of $\sim 90 \mathrm{~km}$ is needed...


## A (10k×10k)-pixels image of our Earth



This 2002 Blue Marble image features land surfaces, clouds, topography, and city lights at a maximal resolution of 1 km per pixel.
Composed from 4 months data from NASA's Terra satellite by R.Simmon, R. Stöckli.

## 1,000-pixel direct image of an exo-Earth...

The tyranny of the diffraction limit: To make a 1,000-pixel image of an exo-Earth at 100 light years, a telescope with a diameter of $\sim 90,000 \mathrm{~km}$ is needed...


Diameter of $90,000 \mathrm{~km}$ is $\sim 7$ diameters of the Earth

## SGL enables direct multipixel imaging

- Solar gravitational lens (SGL) offers:
- Magnification (at 1 um ) $\sim 2 \times 10^{-11} \&$ angular resolution: $\sim 0.5$ nanoarsec
- Overcoming the issue of a small target size:
- Consider an exo-Earth @ 30pc (100 l.y.) is $\sim 1.4 \times 10^{-11}$ rad;
- A diffraction-limited telescope needed to resolve an object with this size at such distance must have a diameter of $\sim 90 \mathrm{~km}$;
- To resolve the planet with 1,000 pixels one needs a telescope with a diameter of $90 \times 10^{4} \mathrm{~km}$ (or $\sim 14 R_{\oplus}$ ), which is impractical...
- Even more challenging is the integration time needed to reach SNR=10:
- a 50 m telescope would need an integration time of $t \sim 10^{6}$ years (zodi);
- with SGL's light amplification $\left(\sim 2 \times 10^{9}\right)$ we could do the job in $\sim 3$ month.
- Solving the parent start light contamination issue:
- Current exoplanet-imaging concepts detect light of a planet as a single pixel. Contamination from the parent star ( $\sim 0.1$ " off the planet) is a major problem;
- Due to the high angular resolution of the SGL ( $\sim 0.5$ nas), the parent star is resolved from the planet with its light amplified 0.01 AU away from the optical axis, making the parent star contamination issue negligible.



## Conventional techniques?

- Overcoming the issue of the long integration times:
- Let's calculate integration time to get SNR = 10 on the longest baseline for an interferometer that resolved an object with 1,000 pixels across:
- exo-Earth @ 30pc is an object of 32.4 mag;
- background is 1 exo-zodi of 22 mag/arcsec ${ }^{2}$;
- 10 m space telescope(s) with perfect coronagraphs;
- max baseline $\sim 45,000 \mathrm{~km}$;
- integration time is $t_{0} \sim 400$ million years...
- Assume the interferometer is phased to $<\lambda / 20$ during the integration and the coronagraph suppresses the parent star to below the exo-zodi level:
- To image with 1,000 pixels (pixel $=47$ mag), a million baselines are needed;
- If only 2 of 10 m telescopes are available, multiply the above $t_{0}$ by a million to get integration time of $t \sim 4 \mathrm{e} 14$ years;
- If more telescopes added, decrease integration time by \# telescopes...
- Integration time decreases rapidly with $D>10 \mathrm{~m}$ as $\sim D^{4}$;
- Array of $10^{3}$ of 100 m telescopes would take $t=4 \mathrm{e} 14 / 1 \mathrm{e} 7 \sim 40$ million years


Precision alignment between a Lens and the Earth is very unlikely...
$\alpha_{\text {Newton }}(b)=\frac{2 G M_{\odot}}{c^{2} b}=0.877\left(\frac{\mathcal{R}_{\odot}}{b}\right) \operatorname{arcsec}$


The Huntington Library, Pasadena, CA


George Ellery Hale Erwin Finlay-Freundlich (1868-1938)


- In 1913 Einstein wrote to Hale:
- "Is eclipse necessary to test this prediction?"
- Hale replied: "Yes, an eclipse is necessary, as stars near the Sun would then be visible, and the bending of light from them would show up as an apparent displacement of the stars from their normal positions."
- In 1914, the first attempt - a German expedition
- A German astronomer Finley-Freundlich led an expedition to test the Einstein's prediction during a total solar eclipse on Aug. 21, 1914 (in Russia);
- However, the First World War (July 28, 1914) intervened, and no observations could be made.


## The First Test of General Theory of Relativity



Gravitational Deflection of Light:

$$
\alpha_{\mathrm{GR}}(b)=\frac{2(1+\gamma) G M_{\odot}}{c^{2} b} \simeq 1.75\left(\frac{1+\gamma}{2}\right)\left(\frac{\mathcal{R}_{\odot}}{b}\right) \operatorname{arcsec}
$$



Campbell's telegram to Einstein, 1923

Solar Eclipse 1919:
Deflection $=0$;
Newton $=0.87$ arcsec;
Einstein $=2 \times$ Newton $=1.75 \mathrm{arcsec}$


Einstein and Eddington, Cambridge, 1930

# THE SOLAR GRAVITATIONAL LENS <br> Gravitational Deflection of Light is a Well-Known Effect Today 



IPL Tesmaneammanculas
L. Our solar system and tests of gravity


Techniques for Gravity Tests:

## Radar Ranging:

-Planets: Mercury, Venus, Mars
-s/c: Mariners, Vikings, Pioneers, Cassini, Mars Global Surveyor, Mars Orbiter, etc.
$-V L B I, G P S$, etc.

## Laser:

-SLR, LLR, interplanetary, etc.

## Dedicated Gravity Missions:

- LLR (1969 - on-going!!)
- GP-A,'76; LAGEOS,'76,'92; GP-B,'04; LARES,'12; MicroSCOPE,'16, ACES, '18; LIGO,'16; eLISA, 2030+(?)

New Engineering Discipline Applied General Relativity:

## The Nobel Prize in Physics 2017


© Nobel Media. III. N. Rainer Weiss Prize share: 1/2


Q Nobel Media. Il. N. Elmehed Barry C. Barish Prize share: $1 / 4$

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Kip S. Thorne Prize share: 1/4
"for decisive contributions to the LIGO detector and the observation of gravitational waves"

- Daily life: GPS, geodesy, time transfer;
- Precision measurements, deep-space navigation \& $\mu$ as-astrometry (Gaia)


General relativity is now well tested. Can we use it to build something?

Eshleman V.R., Science 205, 1133 (1979)

# Gravitational Lens of the Sun: Its Potential for <br> Observations and Communications over Interstellar Distances 


#### Abstract

The gravitational field of the sun acts as a spherical lens to magnify the intensity of radiation from a distant source along a semi-infinite focal line. A spacecraft anywhere on that line in principle could observe, eavesdrop, and communicate over interstellar distances, using equipment comparable in size and power with what is now used for interplanetary distances. If one neglects coronal effects, the maximum magnification factor for coherent radiation is inversely proportional to the wavelength, being 100 million at 1 millimeter. The principal difficulties are that the nearest point on the focal half-line is about 550 times the sun-earth distance, separate spacecraft would be needed to work with each stellar system of interest, and the solar corona would severely limit the intensity of coherent radiation while also restricting operations to relatively short wavelengths.


About 40 years ago, Einstein (I) published a short note in Science on the focusing of starlight by the gravitational field of another star. He emphasized the improbability of observing this phenomenon by the chance alignment of two stars and the earth. From concepts based on current technology and trends, however, it appears that gravitational focusing of electromagnetic radiation might be employed, by design, for highly directional observations and communications over interstellar distances.
In such use, the gravitational field of the sun could play several roles. First, it might be used to reduce fuel and time re-
$1+\nu$, where the refractivity $\nu=g / r$ at radius $r$. A ray is deflected through the angle $\alpha=2 g / a$, where $a$ is the ray impact parameter and $g$ is the gravitational radius $\left(g=2 G \mathrm{~m} / \mathrm{c}^{2}\right.$, where $G$ is the gravitational constant, $m$ is the mass of the central body, and $c$ is the speed of light). It is assumed throughout that $\alpha \ll 1$. An observer at position $z$ behind the lens and $x$ from the center line, as illustrated, would see an energy density lessened by defocusing in the plane of propagation, but increased by focusing due to the curved limb normal to this plane. The relative single-ray intensity $I=F_{\mathrm{h}}{ }^{2} F_{\mathrm{v}}{ }^{2}$, where in ray optics $F_{\mathrm{h}}{ }^{2}=$
nel scales along the circumference of a circle at the ray-impact radius. Using also the wave number $k=2 \pi / \lambda$, the maximum intensification of the coherent sig. nal is simply

$$
\begin{equation*}
I_{\max }=2 \pi k g \tag{2}
\end{equation*}
$$

As an approximation, let the focal "spot" radius $x_{s}$ be the value of $x$ where $I$ falls to $I_{\max } / 4$, so that $x_{s}=$ $(2 / \pi k)(z / 2 g)^{1 / 2}$. Thus the angular resolution for distinguishing two adjacent coherent sources by a corresponding change in intensity is $x_{s} / z$ radians. (The first null off the center line is at $x=\pi^{2}$ $x_{3} / 2$, and the first sidelobe is twice this distance with intensity $I_{\max } / \pi^{2}$.) The periapsis or minimum radius of the ray relative to the center of mass is $a-g$, or essentially $a$, and this must be greater than $r_{0}$, the physical radius of the spherical mass. Thus $\alpha_{\max }=2 g / r_{0}$ and the focal line begins at $z_{\min }=r_{0}^{3} / 2 g$.
Now consider the focusing at $z>z_{\text {min }}$ of incoherent radiation from a uniformly bright, circular, extended source of radius $r_{\mathrm{p}}$ and distance $z_{\mathrm{p}} \gg z$. This is the problem considered by Einstein (I) and more completely by others, notably Liebes (4). The gain factor $A$ of the gravitational lens for the intensity observed from the two individual imase com. from the two individual imase com. , Powell, Ohio, 6-115 (1986) Maccone C., many papers, 1999-present $\quad$ Turyshev \& Andersson, MNRAS 341, 577 (2003)

# THE SOLAR GRAVITATIONAL LENS <br> The Solar Gravitational Lens (KISs study, 2015) 

## The Interstellar Medium

Heliosphere



Interaction Zone

The Local Interstellar Cloud .
Interstellar Wind
$\stackrel{\longleftarrow}{\longleftarrow}$

## Interstellar Medium

The G Cloud
Oort
Cloud



Solar Gravity Lens As Veiwed from the Focal Line
Cloud

Interstellar Wind

$\alpha_{0}=\frac{2 r_{g}}{R_{\odot}} \approx 8.5 \mu \mathrm{rad} \quad \rightarrow \quad \alpha(b)=\alpha_{0} \frac{R_{\odot}}{b}$
$\mathcal{F}_{0}=\frac{R_{\odot}}{\alpha_{0}}=\frac{R_{\odot}^{2}}{2 r_{g}} \approx 547 \mathrm{AU} \quad \rightarrow \quad \mathcal{F}(b)=\mathcal{F}_{0} \frac{b^{2}}{R_{\odot}^{2}}$
region of interference


Different regions of the SGL


Caustic formed behand the Sun

Herlt \& Stephani, IJMP 15, 45 (1976)

- Major brightness increase:
- For small departures from the optical axis, $\rho$, magnification of the SGL is:
$\mu_{z}(\rho, z, \lambda) \cong 4 \pi^{2} \frac{r_{g}}{\lambda} J_{0}^{2}\left(2 \pi \frac{\rho}{\lambda} \sqrt{\left.\frac{2 r_{g}}{z}\right)}{ }_{\rho}\right.$
- Max value of $G(\rho, \lambda)$ is on axis:

$$
\mu_{z}(0, z, \lambda) \cong 4 \pi^{2} \frac{r_{g}}{\lambda}
$$

Point-spread



Turyshev \& Toth, Phys. Rev. D 96, 024008 (2017)
Gain of the SGL as seen in the image plane as a function of possible observational wavelength

## Point spread function \& gain of the SGL






Turyshev \& Toth, Phys. Rev. D 96, 024008 (2017)


## Properties of the Solar Gravity Lens



- Important features of the SGL (for $\lambda=1 \mu \mathrm{~m}$ ):
- Major brightness magnification: a factor of $10^{11}$ (on the optical axis);
- High angular resolution: ~0.5 nano-arcsec. A 1-m telescope at the SGL collects light from a $\sim(10 \mathrm{~km} \times 10 \mathrm{~km})$ spot on the surface of the planet, bringing this light to one 1-m size pixel in the image plane of the SGL;
- Extremely narrow "pencil" beam: entire image of an exo-Earth ( $\sim 13,000 \mathrm{~km}$ ) at 100 l.y. is included within a cylinder with a diameter of $\sim 1.3 \mathrm{~km}$.
- Collecting area of a 1-m telescope at the SGL's focus:
- Telescope with diameter $d_{0}$ collects light with impact parameters $\delta b \simeq d_{0}$;
- For a 1 -m telescope at 750AU, the total collecting area is: $4.37 \times 10^{9} \mathrm{~m}^{2}$, which is equivalent to a telescope with a diameter of $\sim 80 \mathrm{~km} . .$.


# THE SOLAR GRAVITATIONAL LENS <br> Do not point at the Sun!!!! 


of solar surface


A solar flare

Coronal
mass ejection

© ఒ- Approx. size of Earth

## Effects of gravity \& solar plasma




Gravity, no plasma


Gravity and plasma

## Solar corona brightness



- The instrument:
- A diffraction-limited high-resolution spectrograph, enabling Doppler imaging techniques;
- The SGLF telescope needs a coronagraph to block the Sun's light:
- To block the solar light to the level of solar corona;
- At $1 \mu \mathrm{~m}$, the gain of the SGL is $\sim 110 \mathrm{~dB}$ ( 27.5 mag ), so an exoplanet, which is 32.4 mag object, will become a $\sim 4.9$ mag object;
- When averaged over a 1 m telescope (the gain is $\sim 2 \times 10^{9}$ ), it would be 9.2 mag, which is sufficiently bright (even on the solar background);
- To derive an image with the SGLF, including solar corona brightness (the parent star will be resolved), zodiacal light, instrument, and s/c systematics;
- Perhaps several small spacecraft?
- We could rely on a swarm of small spacecraft, lunched together each moving at a slightly different trajectory parallel to the optical axis.


## Coronagraph study: sun disc \& solar corona

Ext Src: (uniform) Sun disc + Sun corona



Occulter mask; $\sim 81 \%$ trans @ E-ring


C, pk = 1.9e-06; @ E-ring (~1.21 Rsun) =2.0e-07



Deep Space Climate Observatory (NOAA, Feb. 11, 2015):
Earth Polychromatic Imaging Camera (EPIC)


epic_1b_20160321 epic map reconstruction


High SNR allows for

- High-resolution spectroscopy
- Allows reconstruction of a 2-D albedo map from annual variation of the disk-integrated scattered light using technique of spin-orbit tomography (i.e., rotational deconvolution)
- Next step is a direct deconvolution


Accretion disk around a black hole as a test object for convolution by the PSF of the SGL.

$$
\begin{gathered}
I\left(\mathbf{x}_{\mathbf{2}}, \lambda\right)=O(\mathbf{x}, \lambda) \otimes P S F_{\mathrm{diff}}\left(\mathbf{x}_{\mathbf{2}}, \lambda\right) \\
P S F_{\mathrm{diff}}\left(\mathbf{x}_{\mathbf{2}}, \lambda\right) \simeq J_{0}\left(\frac{\pi|\mathbf{x}| r_{0}}{\lambda f}\right) \otimes \frac{r_{0}}{\left|\mathbf{x}_{\mathbf{2}}\right|}
\end{gathered}
$$

- $r_{0}$ - impact parameter,
- $\left|\mathbf{x}_{2}\right|$ - distance in the image plane,
- $\otimes$-2D convolution operator.


Image obtained after convolution. Photon noise is added, corresponding to $100 \mathrm{ph} / \mathrm{pixel}$


De-convolved image using the SGL' PSF. Lowpass filtering in spatial frequencies is applied

## The a priori properties of the target

- We want to image Earth 2.0, around a G star, which is not transiting:
- Once habitability is confirmed ("big TPF" for spectra), the next step is to image it.
- We will rely on astrometry, RV, spectroscopy, and direct imaging to obtain:
- orbital ephemeris: to ~mas accuracy and precision;
- rotation: from temporal monitoring of the spectroscopy;
- atmosphere: temperature, structure, chemical composition, and albedo, from non-spatially-resolved spectroscopy;
- understanding of cloud \& surface properties from Doppler imaging.
- This information will help us to point the s/c:
- Time to reach $550 \mathrm{AU} \sim 10$ years, enough to observe the parent star's location $\sim 100$ times with $1 \mu$ as precision, so that its position would be known to $0.1 \mu \mathrm{as}$;
- The parent star's position would be known to $\sim 45 \mathrm{~km}$ at a distance of 30 pc ;
- Orbital period to $<1 \% \Rightarrow$ the semi-major axis is known to $\sim 0.7 \%$ ( $\sim 1$ million km );
- If face-on, the radial distance to $\sim 1$ million km , with tangential error $\sim 6$ larger;
- Earth's diameter is $13,000 \mathrm{~km}$, so we will search the $(80 \times 500)$ grid on the sky;
- Once SGLFM detects the planet $\Rightarrow$ scan a smaller area to define the "edges".


## Imaging with SGL

- Imaging is done on a pixel-by-pixel basis:
- The image of an exo-Earth occupies $\sim(1.3 \mathrm{~km} \times 1.3 \mathrm{~km})$ area from the optical axis.
- Each pointing corresponds to a different impact parameter: 1 image $\Leftrightarrow 1$ pixel.
- Between the adjacent pixels the impact parameter changes, brings light from adjacent surface areas on the planet $\Rightarrow$ a raster scan moving the spacecraft;
- To build a $\left(10^{3} \times 10^{3}\right)$ pixels image, we would need to sample the image pixel-bypixel, while moving in the image plane with steps of $\sim 1 \mathrm{~km} / 10^{3}=1 \mathrm{~m}$ :
- Pointing: Inertial navigation and 3 laser beacon spacecraft in heliocentric orbit in the plane of the Einstein's ring (for precision pointing \& comm).
- Contamination from the parent star is negligible for an SGL scenario.
- Exoplanet imaging requires several key technologies that are challenging:
- determination of an exoplanet astrometric orbit at $\sim 10$ nas,
- motion \& stabilization of the s/c over millions of pointings with limited power.
- Perhaps even spectroscopy or even spectro-polarimetry of the exoplanet?
- Potentially a spectrally resolved image over a broad range of wavelengths: atmosphere, surface material characterization, biological processes.


Center of the Sun shown as dots monthly from 1944 to 2020 with actual size of the sun shown at its average position, during this time period


Astrometric displacement of the Sun due to Jupiter as at it would be observed from 10 parsecs, or about 33 light-years.

## Trajectories (Measure vs Control)

- Pointing precision (between three objects):
- Needs to be maintained to ~ few $\mu$ as for proper operation of the SGL.
- Knowledge is needed at $1 \mu$ as level, control is at the $\sim 100 \mu$ as.
- The motion is unfortunately complex (1-m of motion at $600 \mathrm{AU} \sim 1 \mu$ as of angle seen from Earth)
- Simple motions (straight lines):
- Motion of the target star around the galaxy; the Sun around the galaxy
- More complex motions:
- Motion of the exoplanet around its host star (Keplerian)
- Motion of our Sun around the solar system barycenter.
- Dominated by the orbits of Jupiter, Saturn.
- Jupiter $\Rightarrow 75$ million m motion of the Sun (12yr orbit)
- Saturn $\Rightarrow 50$ million $m$ of motion of the Sun (29 yr)
- Earth $\Rightarrow 450,000 \mathrm{~m}$ (1 yr)
- Propulsion system must compensate for the reflex motion of the Sun
- Due to most of the planets in the solar system. (perhaps many of the big asteroids in the main belt) Uranus and Neptune's motion over a short time may be just a straight line (need to calculate for sure).


## Direct Multipixel Imaging and Spectroscopy of an Exoplanet with a Solar Gravity Lens Focus (SGLF) Mission

## An imaging mission to SGLF appears to be feasible, but needs further study

## Concept

- SGLF provides a major gain ( $\sim 10^{11}$ at 1 um ), resolution of $10^{-9}$ arcsec in a narrow FOV;
- A 1-m telescope at $\sim 750 \mathrm{AU}$ has a collecting area equivalent $\sim 80 \mathrm{~km}$ aperture in space;
- A mission to the SGLF could image Earth 2.0 up to 30 pc away with resolution to $\sim 10 \mathrm{~km}$ to see surface features;
- A small s/c with electric propulsion (or solar sails) can reach the SGLF in <35-40 yrs.


## Proposed Study and Approach

- Define baseline design, sub-syst components;
- Define mission science goals \& requirements;
- Develop system and subsystem requirements;
- Study mission architecture and con-ops;
- Assessment of feasibility (cluster) small-sats;
- Identify technology development needs;
- Study instruments \& systems: power, comm, pointing, s/c, autonomy, coronagraph, nav, propulsion, raster scan in the image plane, etc.


## Benefits

- A breakthrough mission concept to resolve a habitable exoplanet at modest cost/time;
- Could find seasonal changes, oceans, continents, life signatures on an exo-Earth;
- Small-sat \& fast exit from the solar system;
- Electric propulsion for raster-scanning the image using tethered s/c (or cluster);
- SLGF is valuable for other astrophysics and cosmology targets.


Earth with resolution of $(1000 \times 1000)$ pixels.

## Comments on NLAC Pbase II proposal (March 2018):

The concept continues to demonstrate unexplored and exciting aspects of value to investigate over the Phase I study. Analysis completed in Phase I is credible. However, unknowns remain that are not readily determined, thereby warranting further study.

If successful, the concept will enable wholly new missions, offer a significant advantage to previously studied work, or provide a great leap in capabilities for NASA or the greater aerospace community. Based on results from the Phase I study, the concept continues to generate enthusiasm for a mission and potential to build advocacy to support it within NASA or in the greater aerospace community.

